

Reproduction leads to higher population fitness: as simple as that

Tommaso Brotto

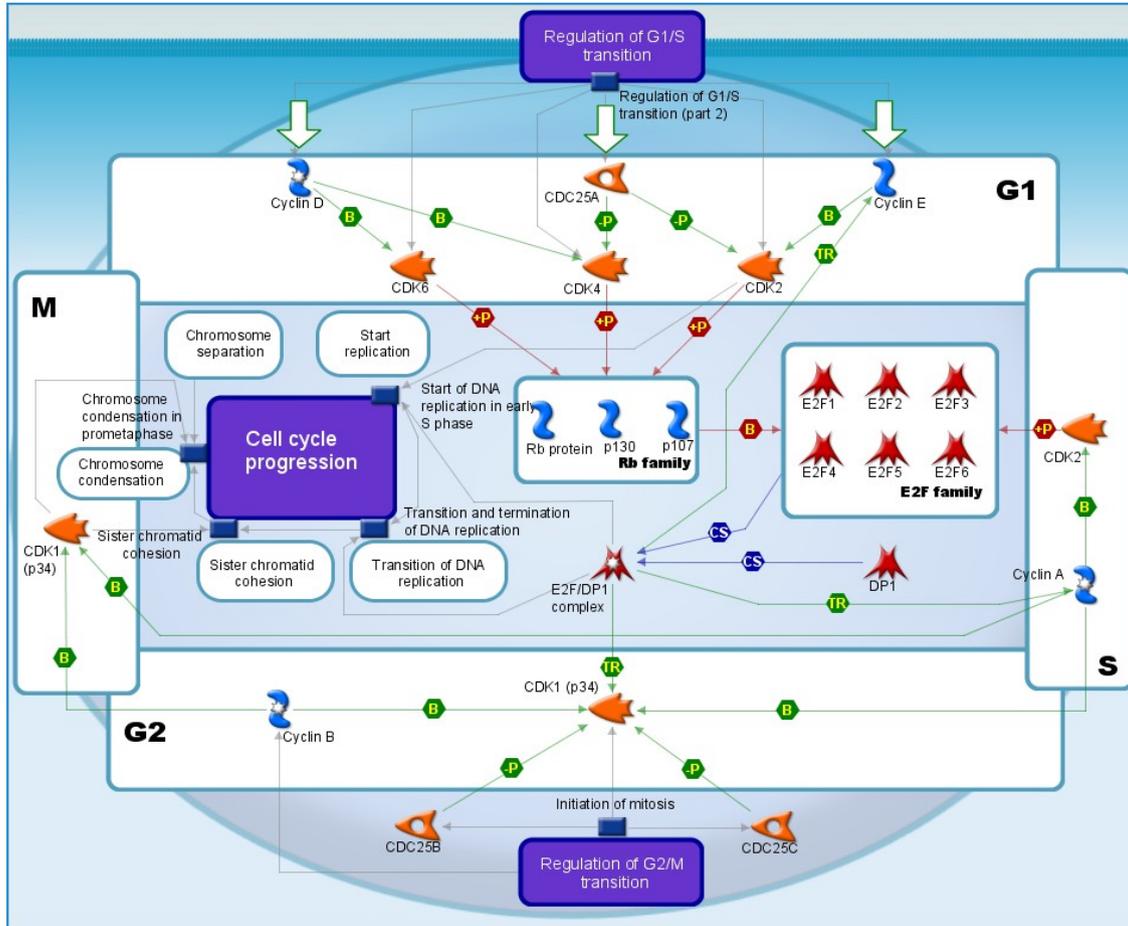
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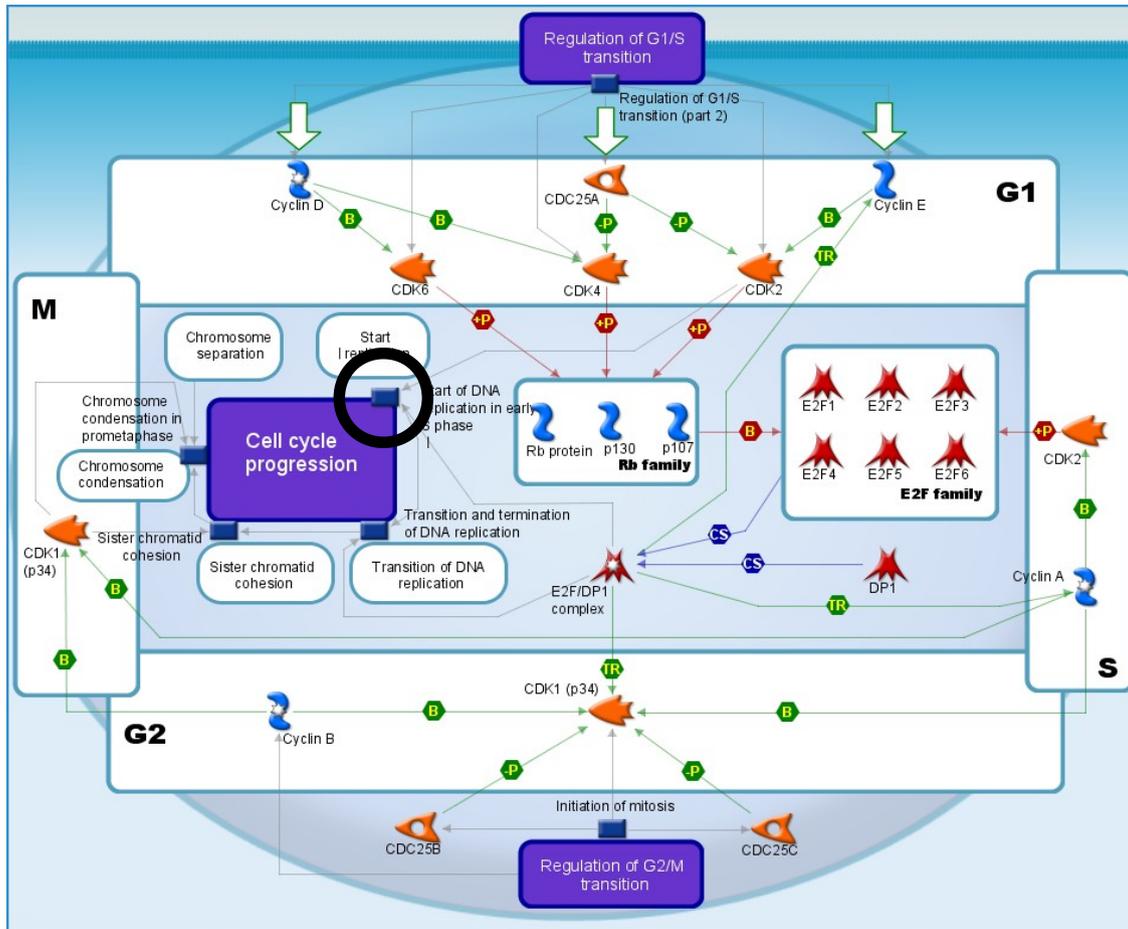
Prof. Sergio Caracciolo

Prof. Jorge Kurchan

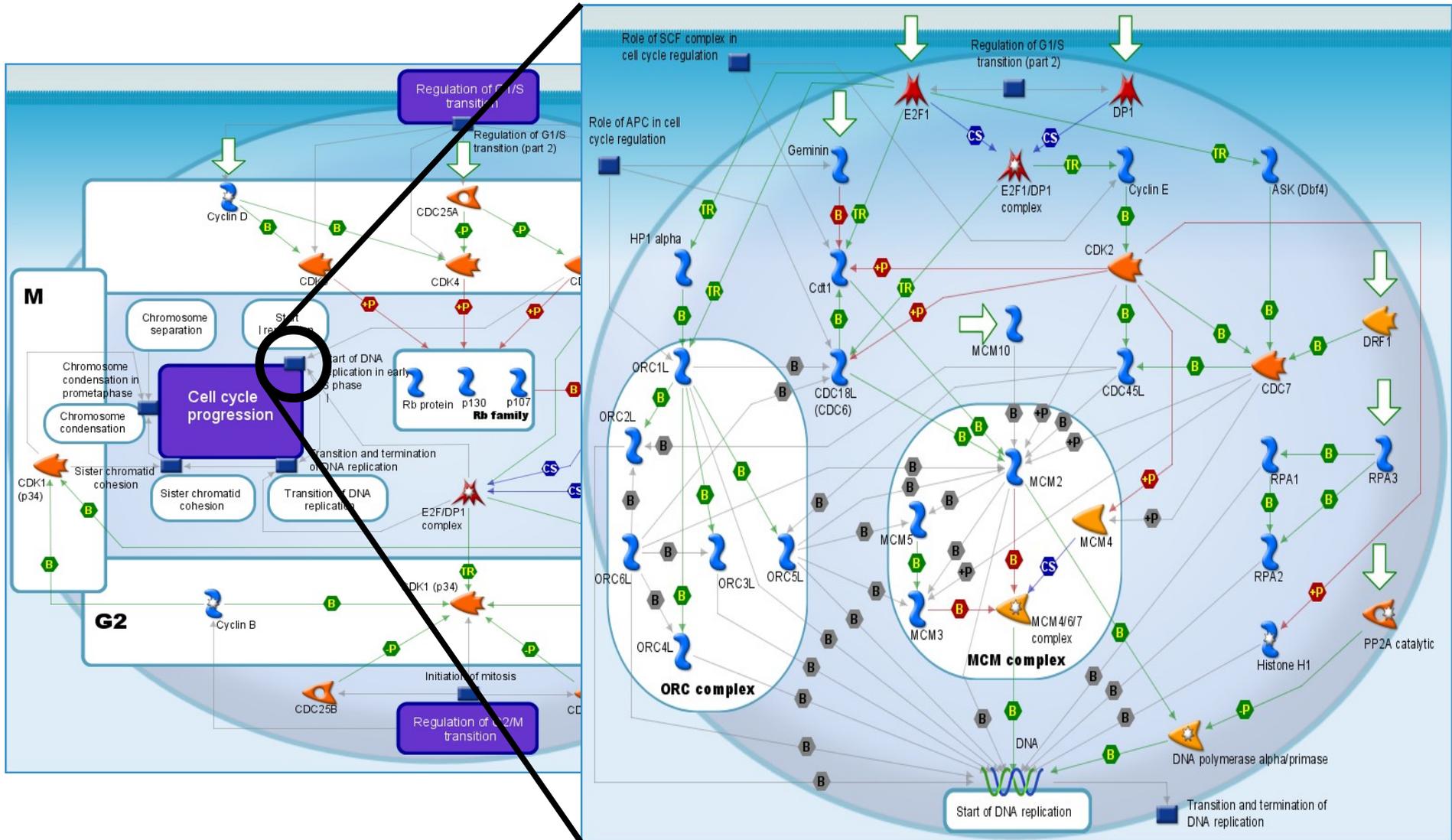
Biological processes are complex!



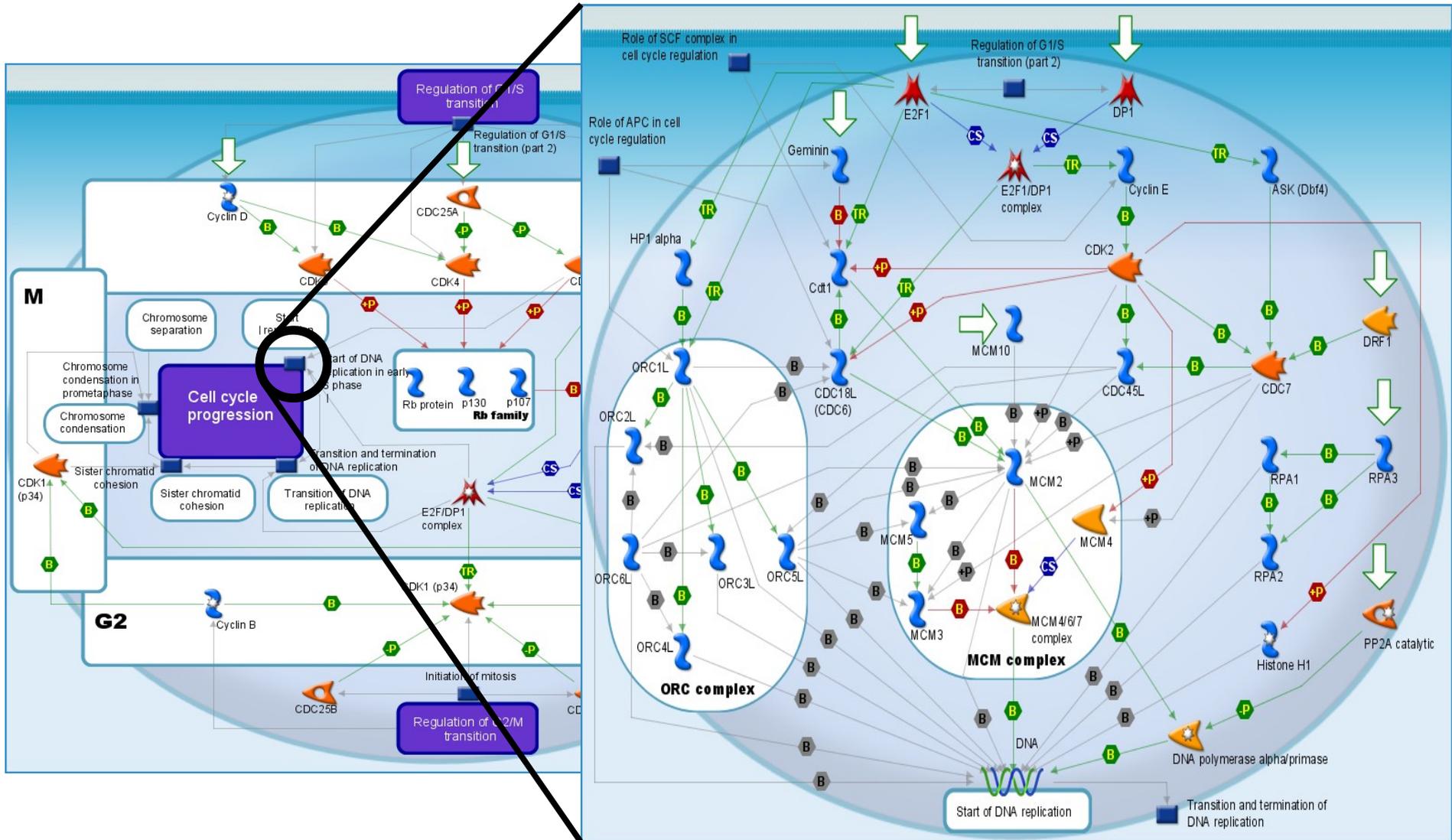
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Do we really need to take **everything** into account?

What is really essential?

A cell can:

- ▶ Reproduce = create offsprings with same traits
- ▶ Mutate = change traits

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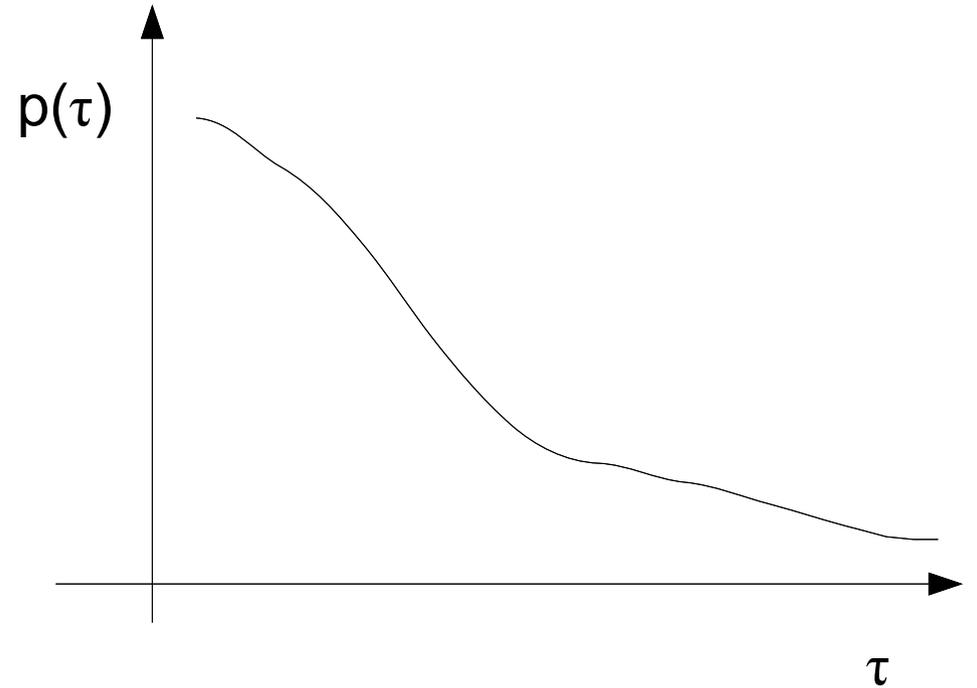
Traits:

λ = fitness (ability to generate offsprings)

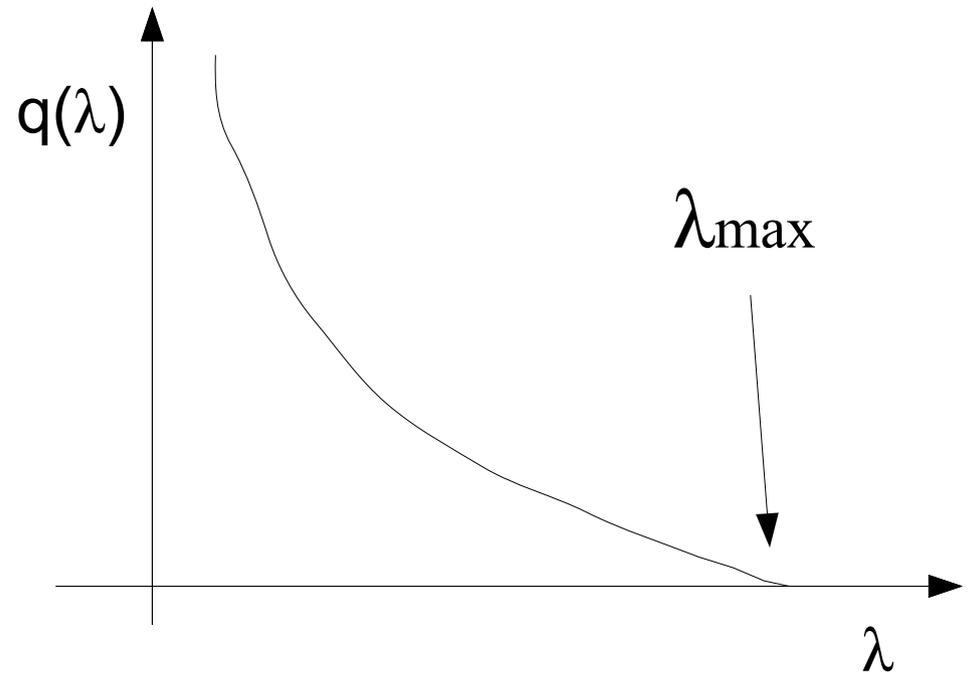
τ = mutation time

Create N cells,
with random τ , λ

τ follows $p(\tau)$



λ follows $q(\lambda)$

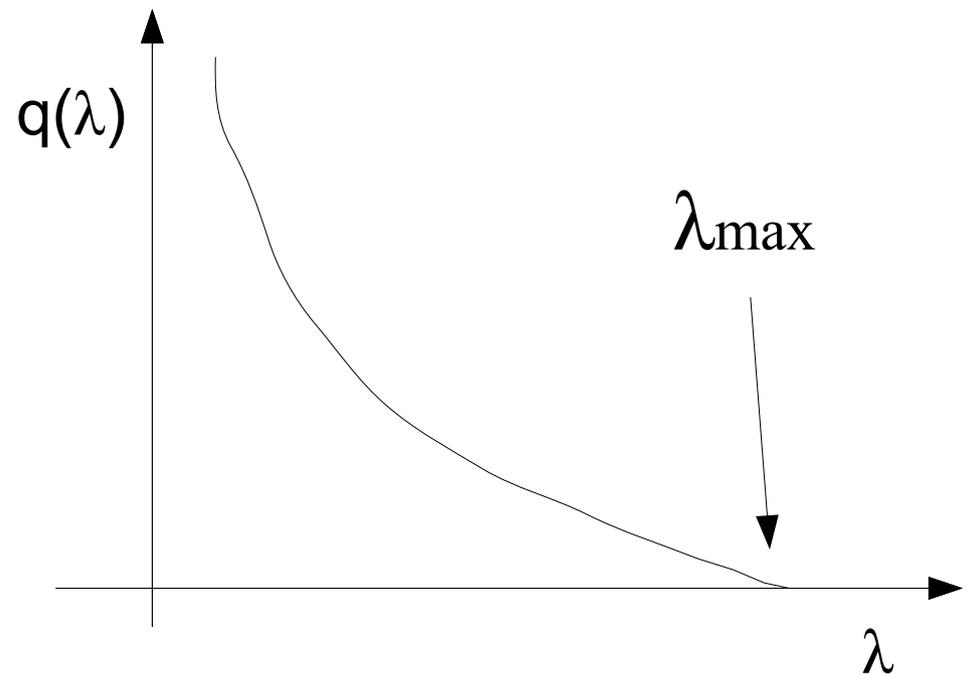
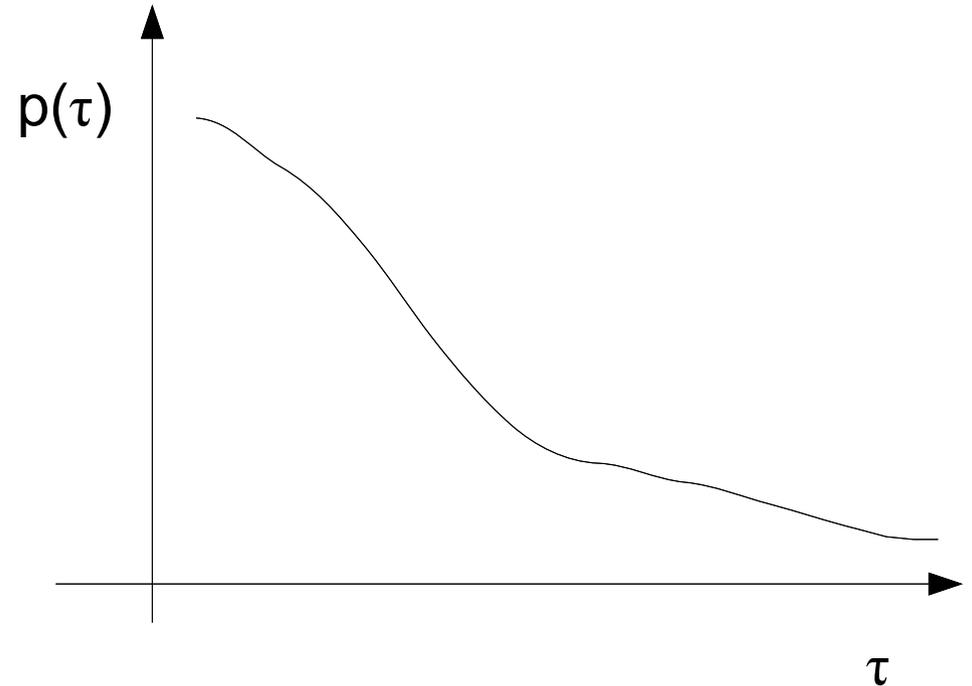


Create N cells,
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τ follows $p(\tau)$

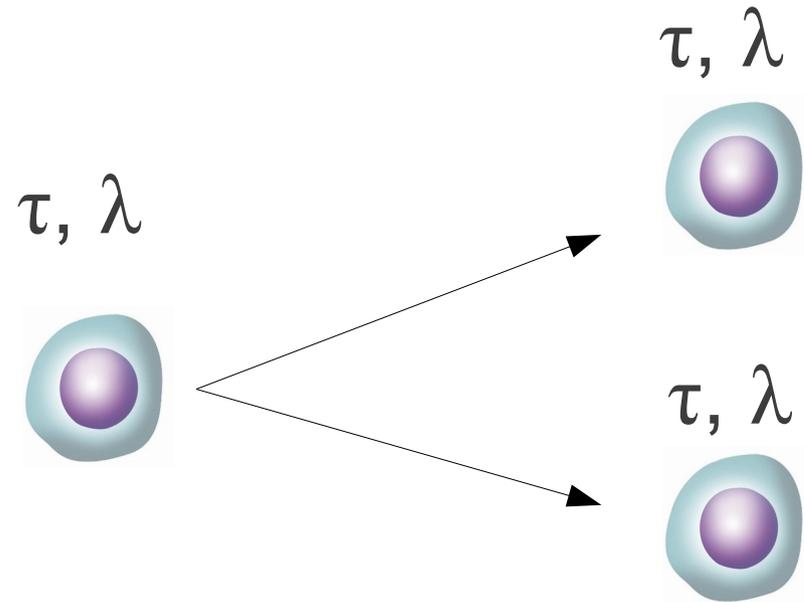
τ and λ are
not correlated

λ follows $q(\lambda)$



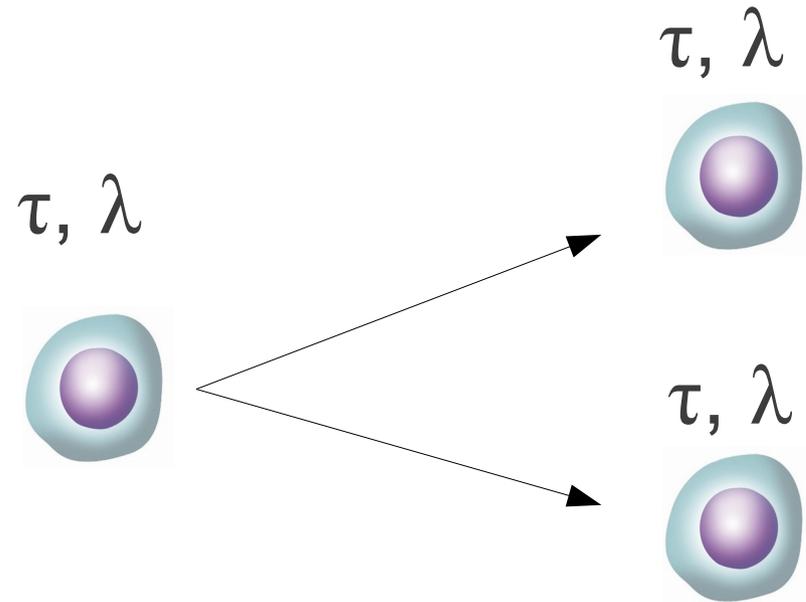
Each time step, each cell:

Reproduction,
with rate λ



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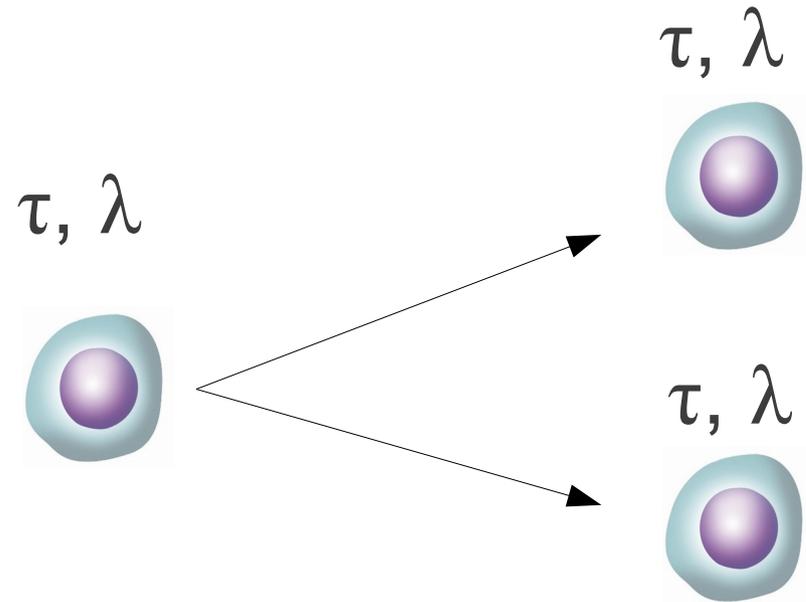


Mutation,
with rate $1/\tau$



Each time step, each cell:

Reproduction,
with rate λ



Mutation,
with rate $1/\tau$

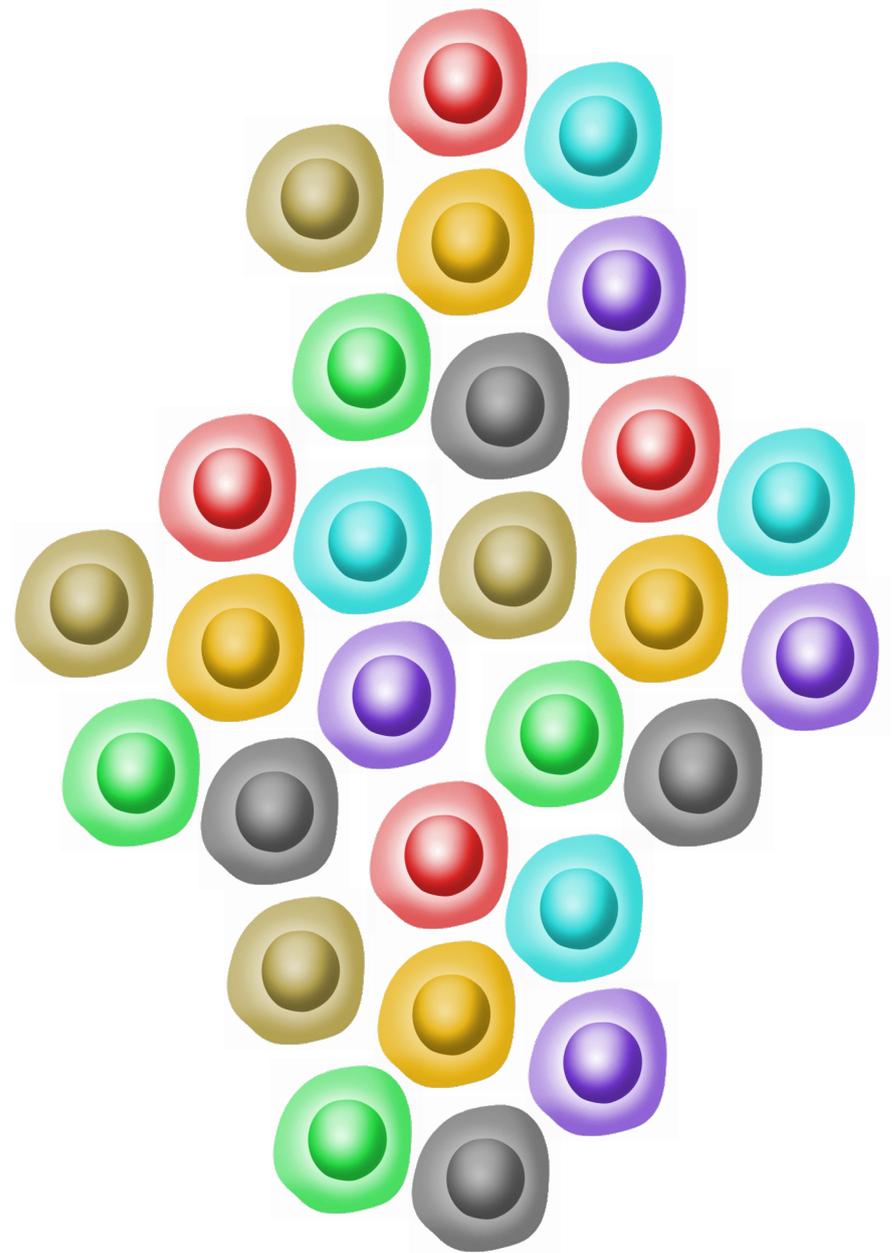


To preserve N , kill randomly



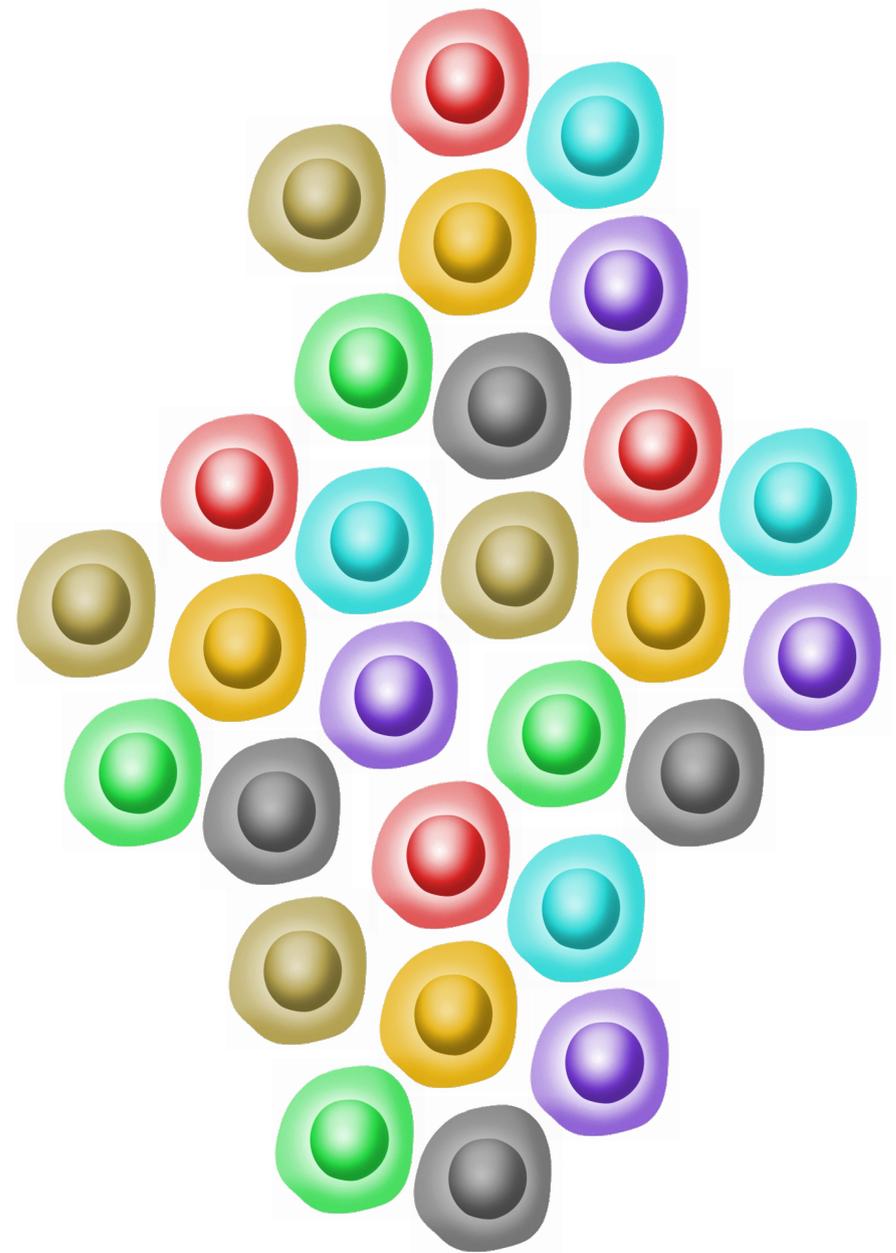
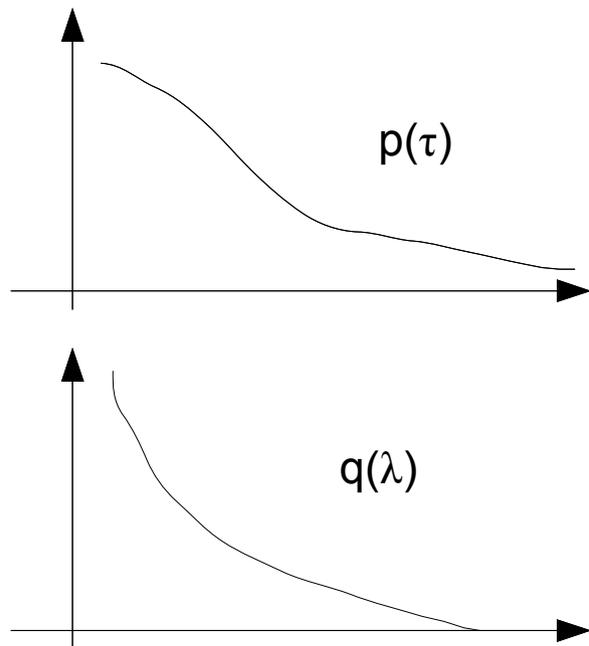
What happens: sketch

First phase:
Randomness



What happens: sketch

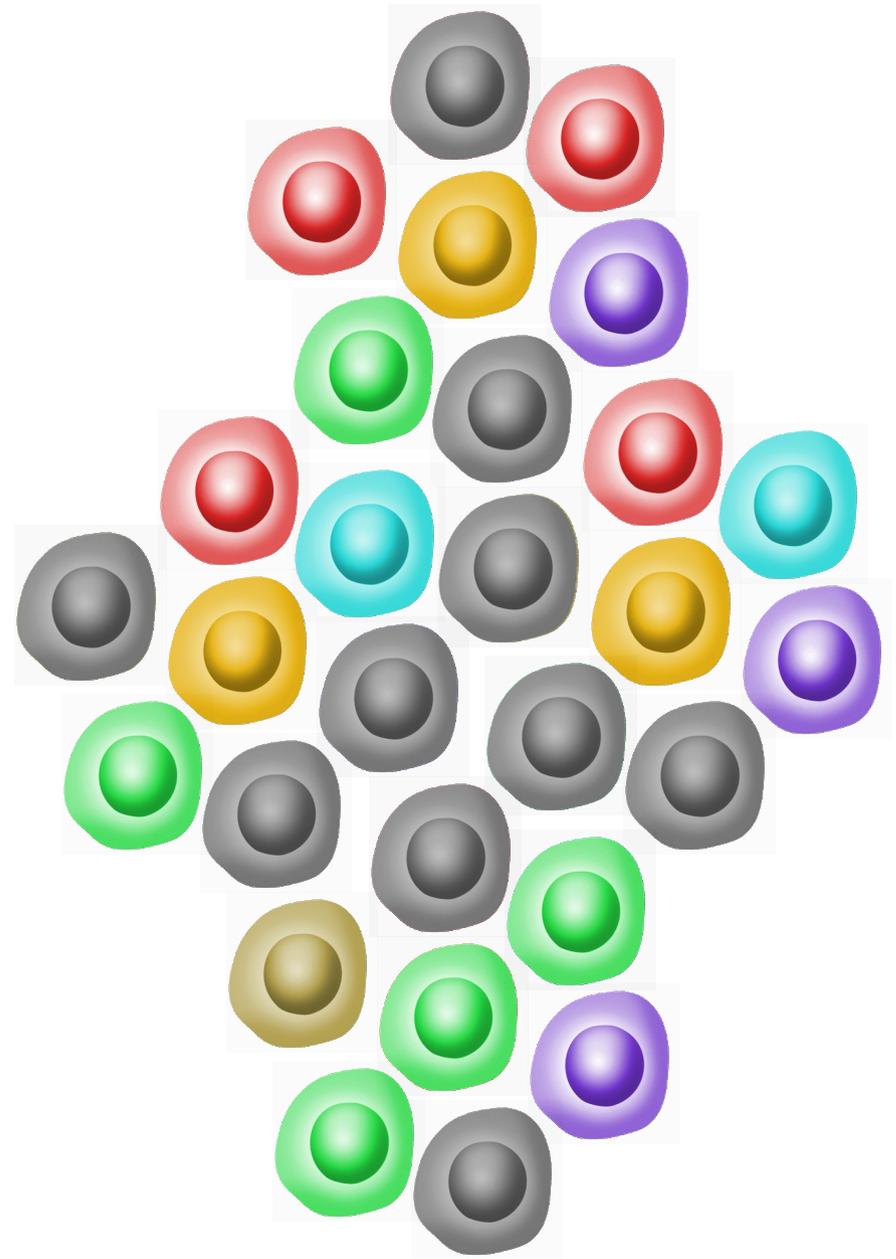
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First phase:
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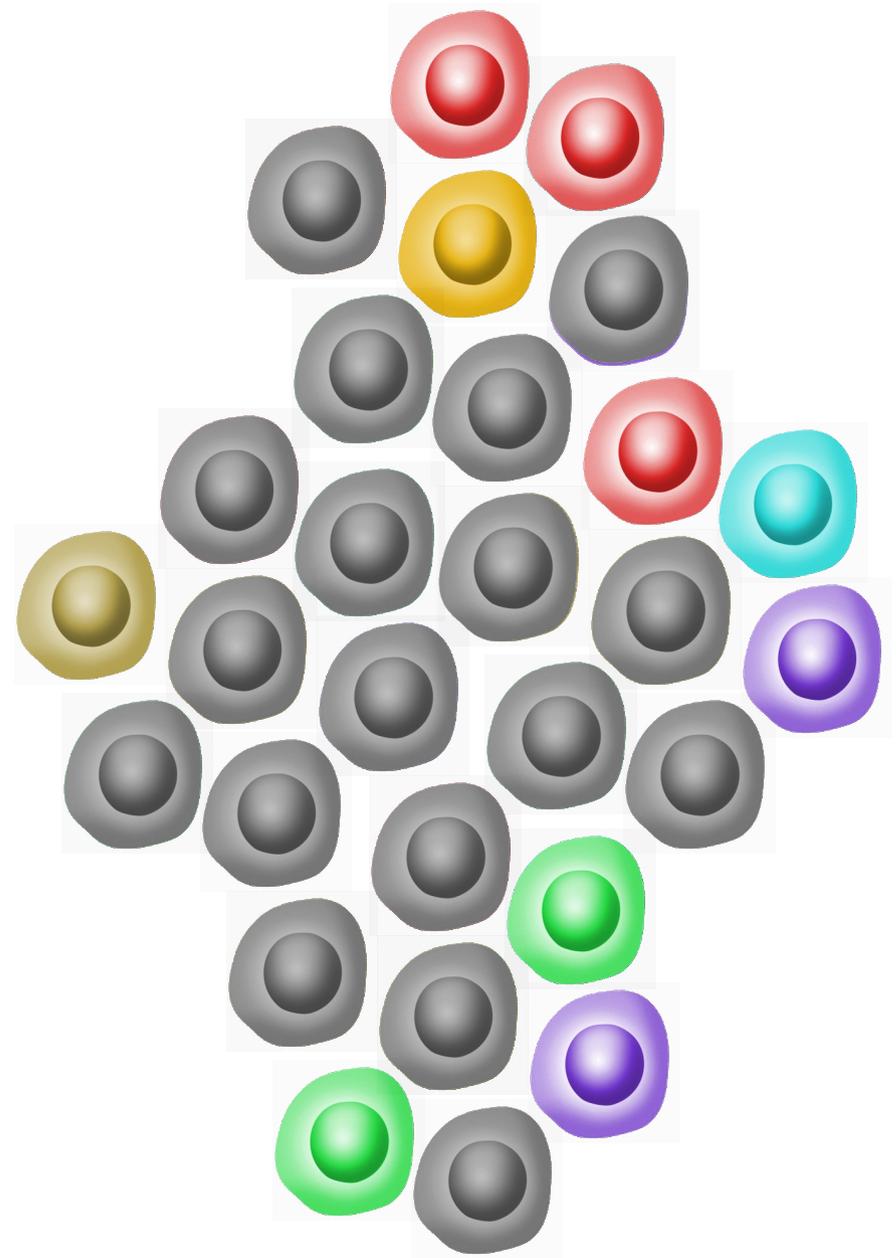
Second phase:
Condensation



What happens: sketch

First phase:
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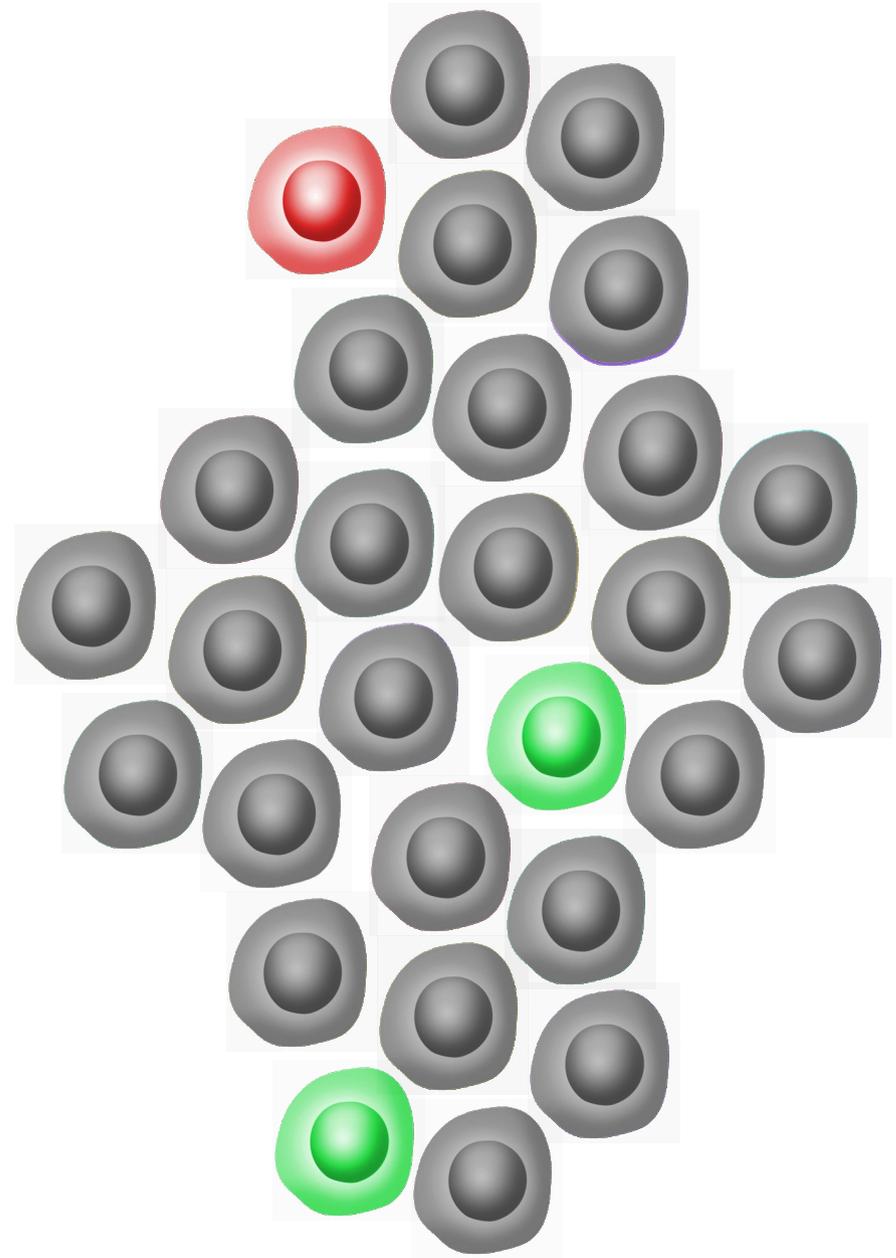
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What happens: sketch

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Second phase:
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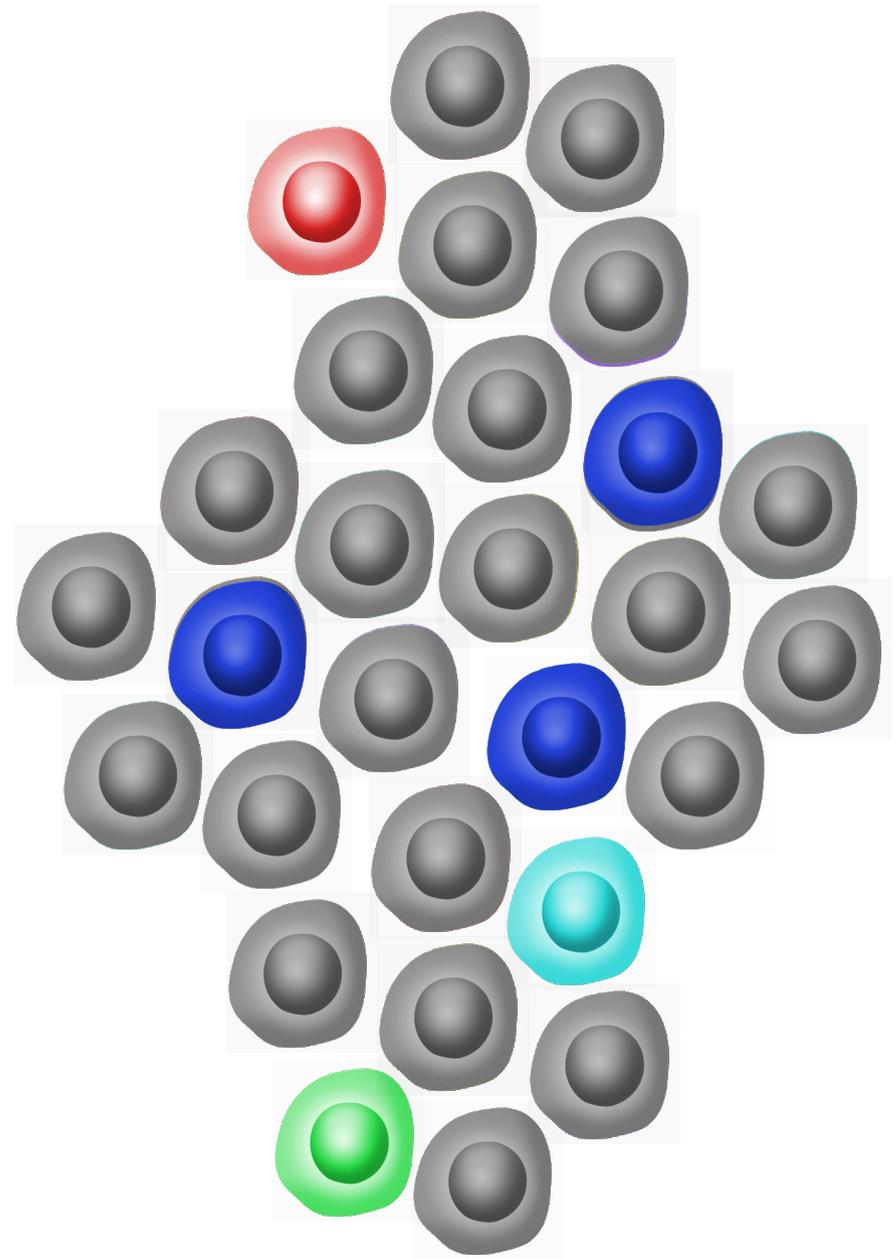


What happens: sketch

First phase:
Randomness

Second phase:
Condensation

Third phase:
Takeovers

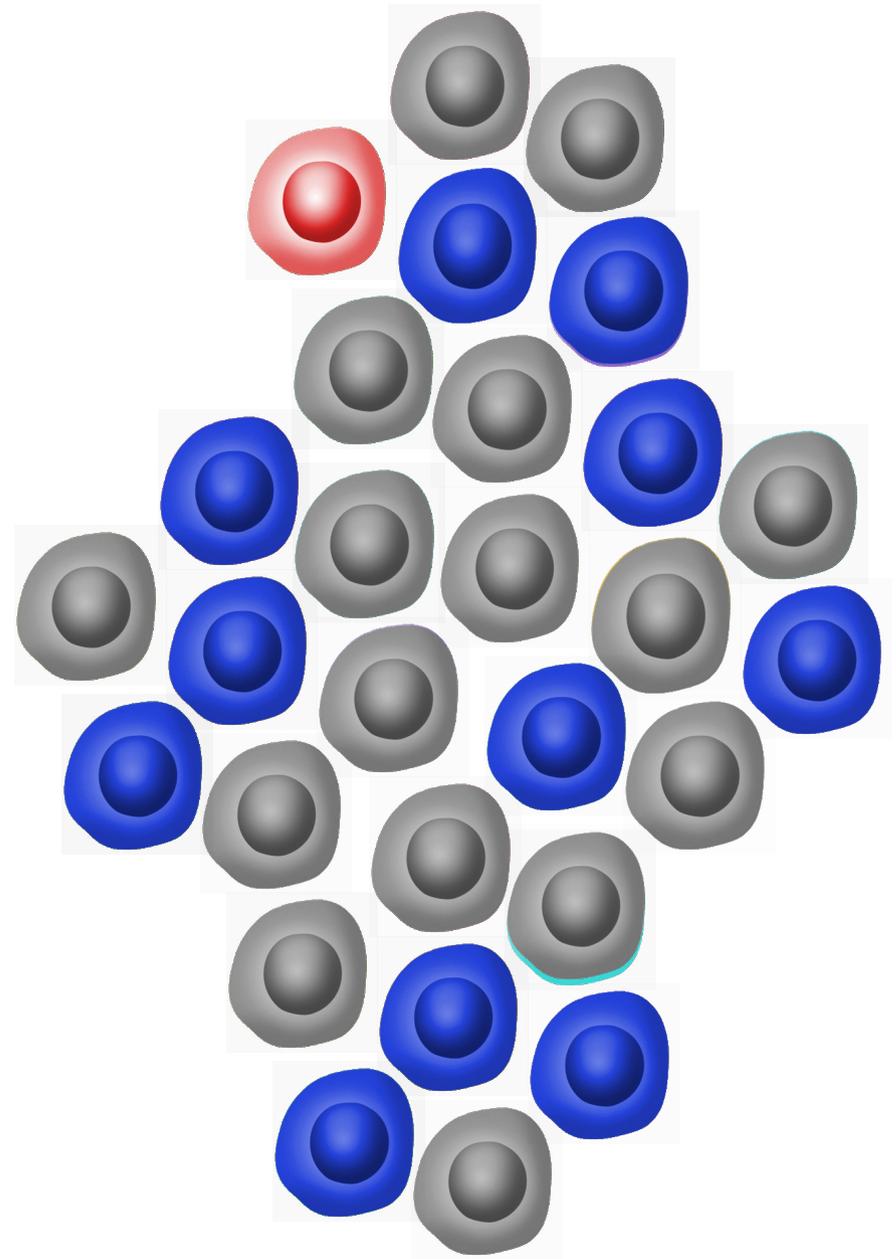


What happens: sketch

First phase:
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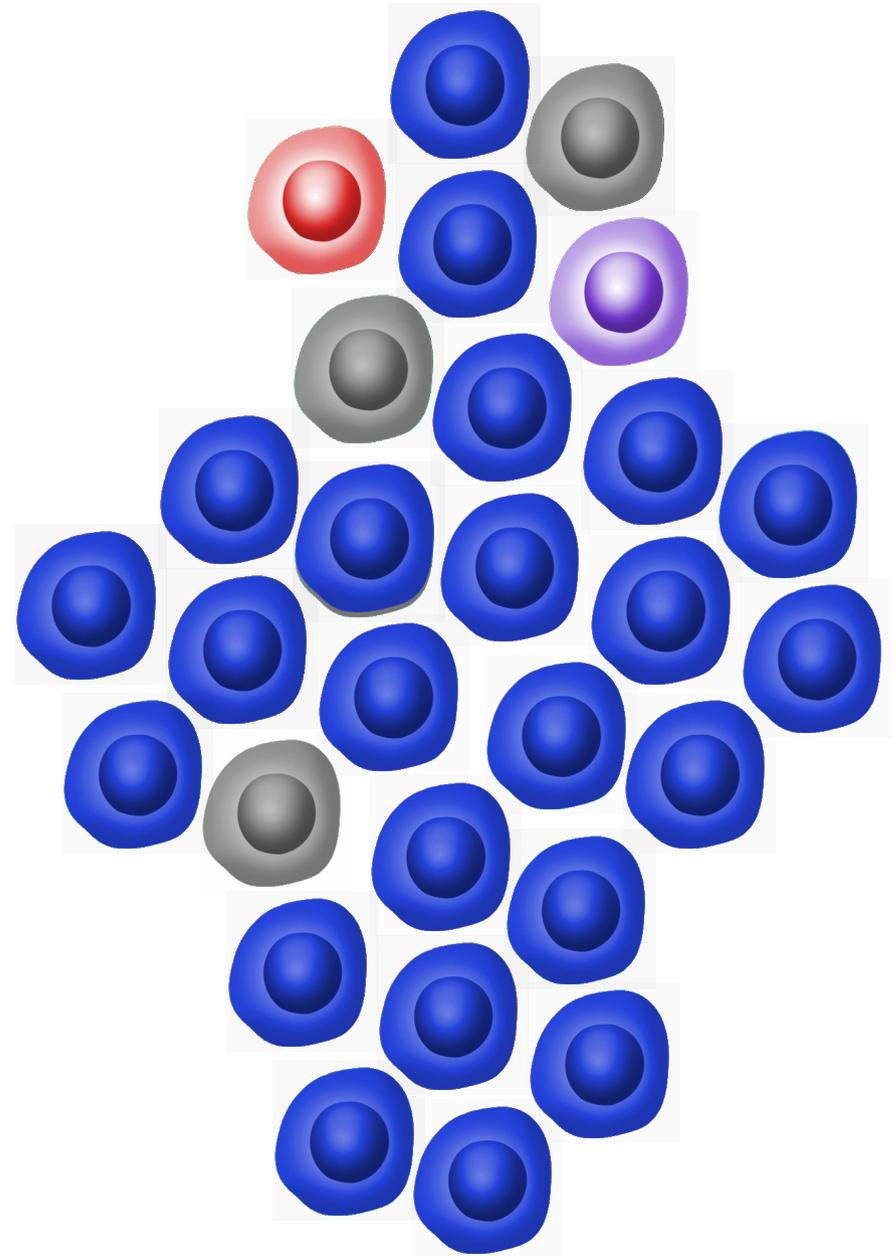


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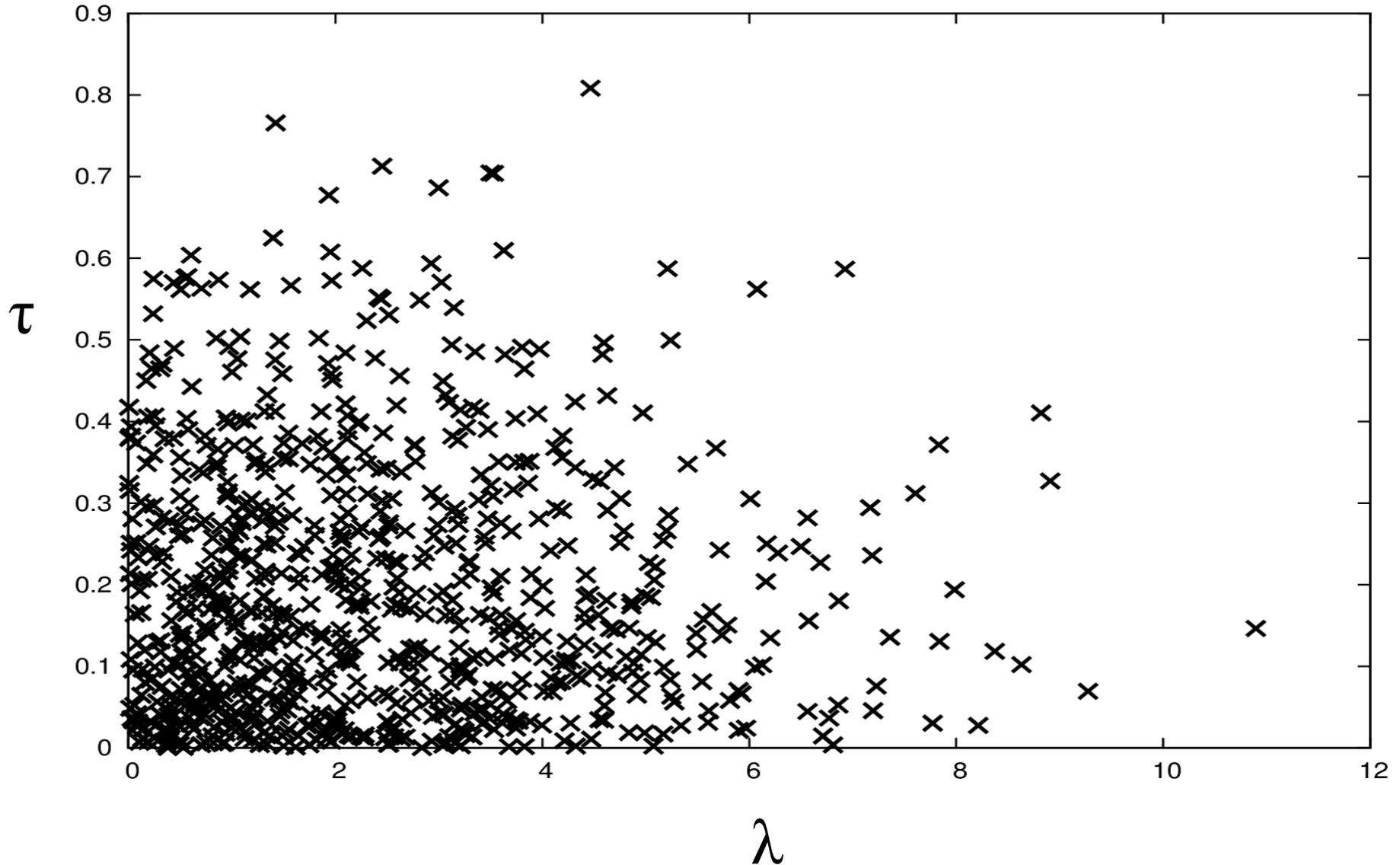
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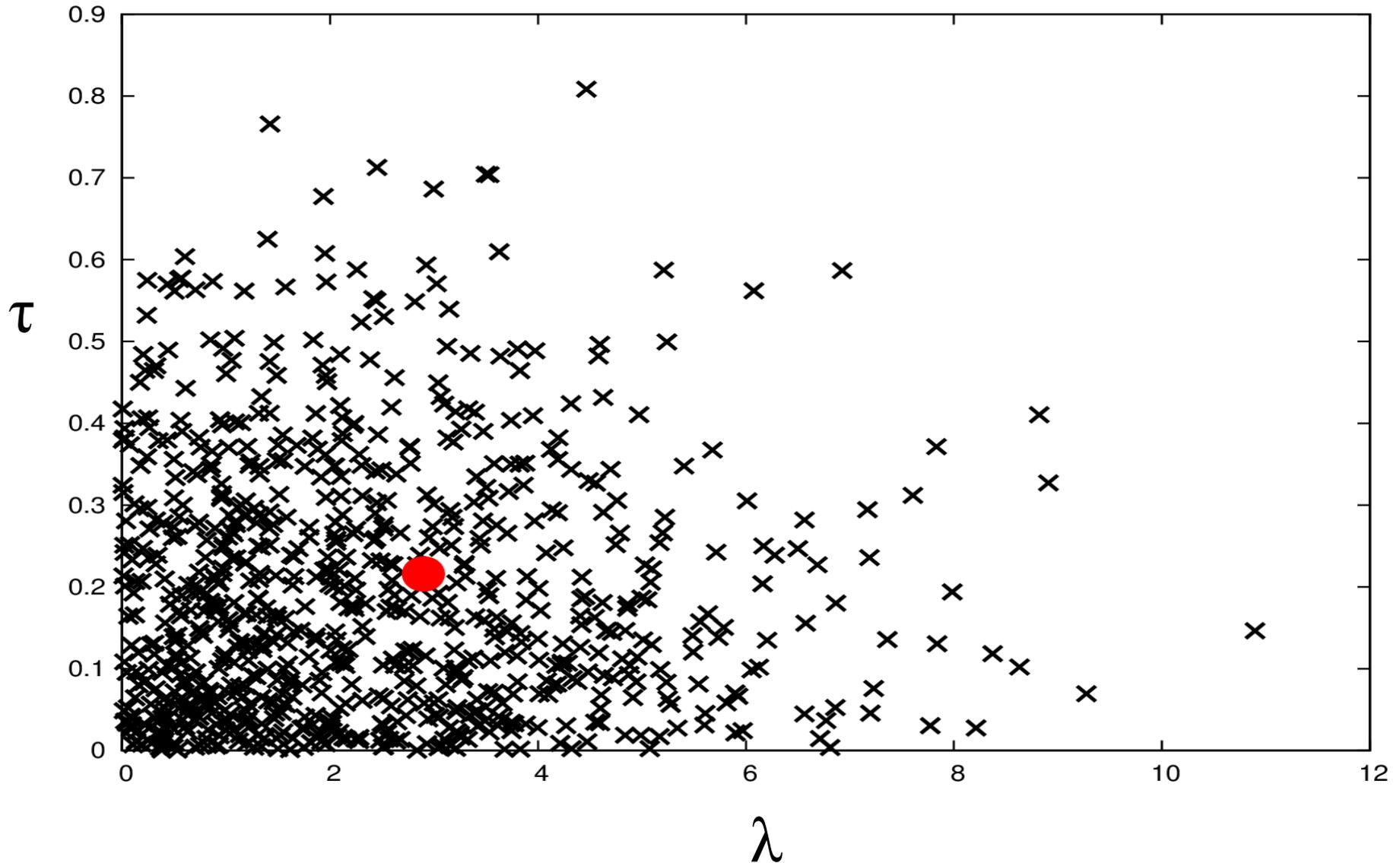
Cells become fitter
but also **more stable**:
lower $1/\tau - \lambda$

Effect due to **reproduction**
(collective)



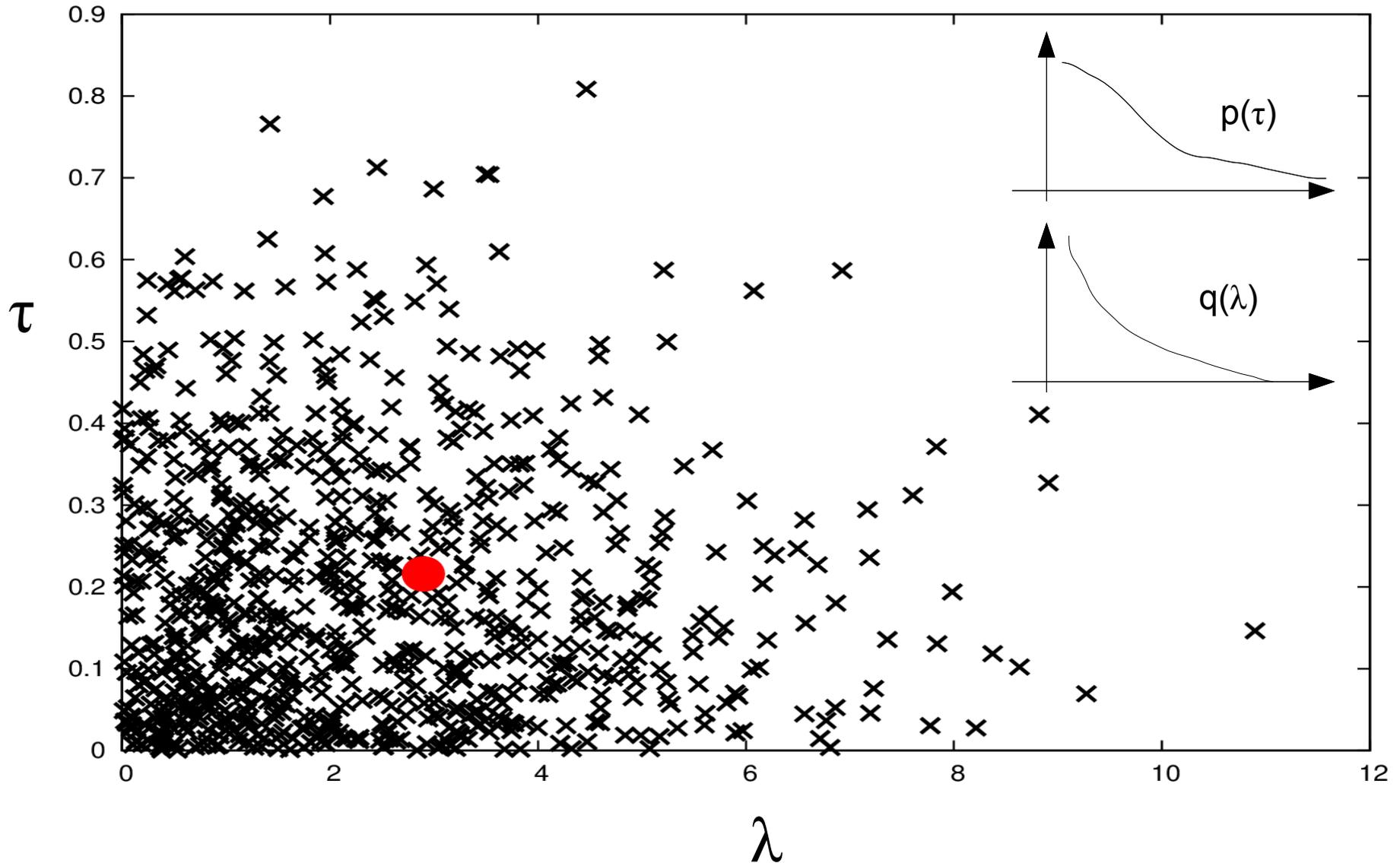
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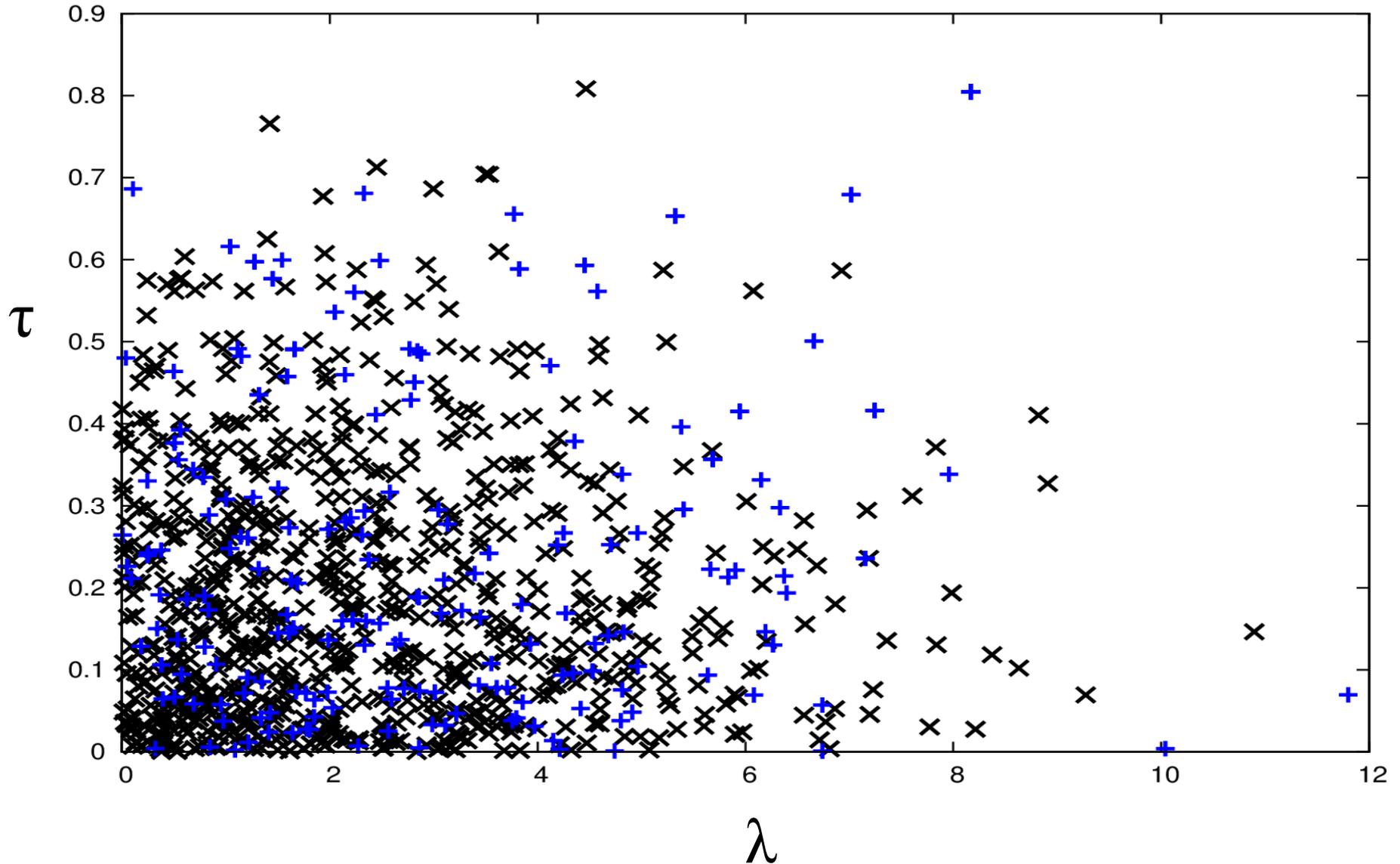
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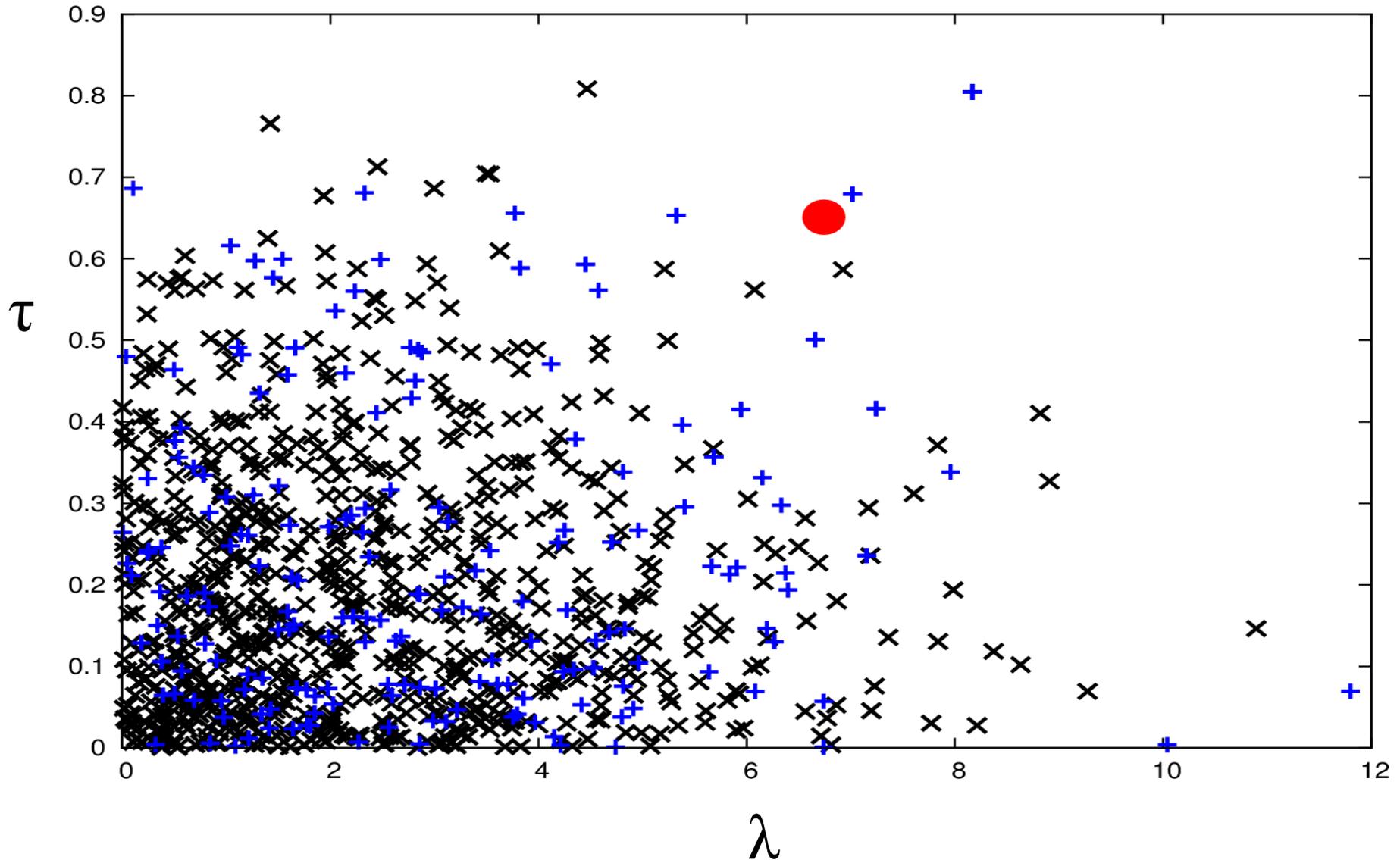
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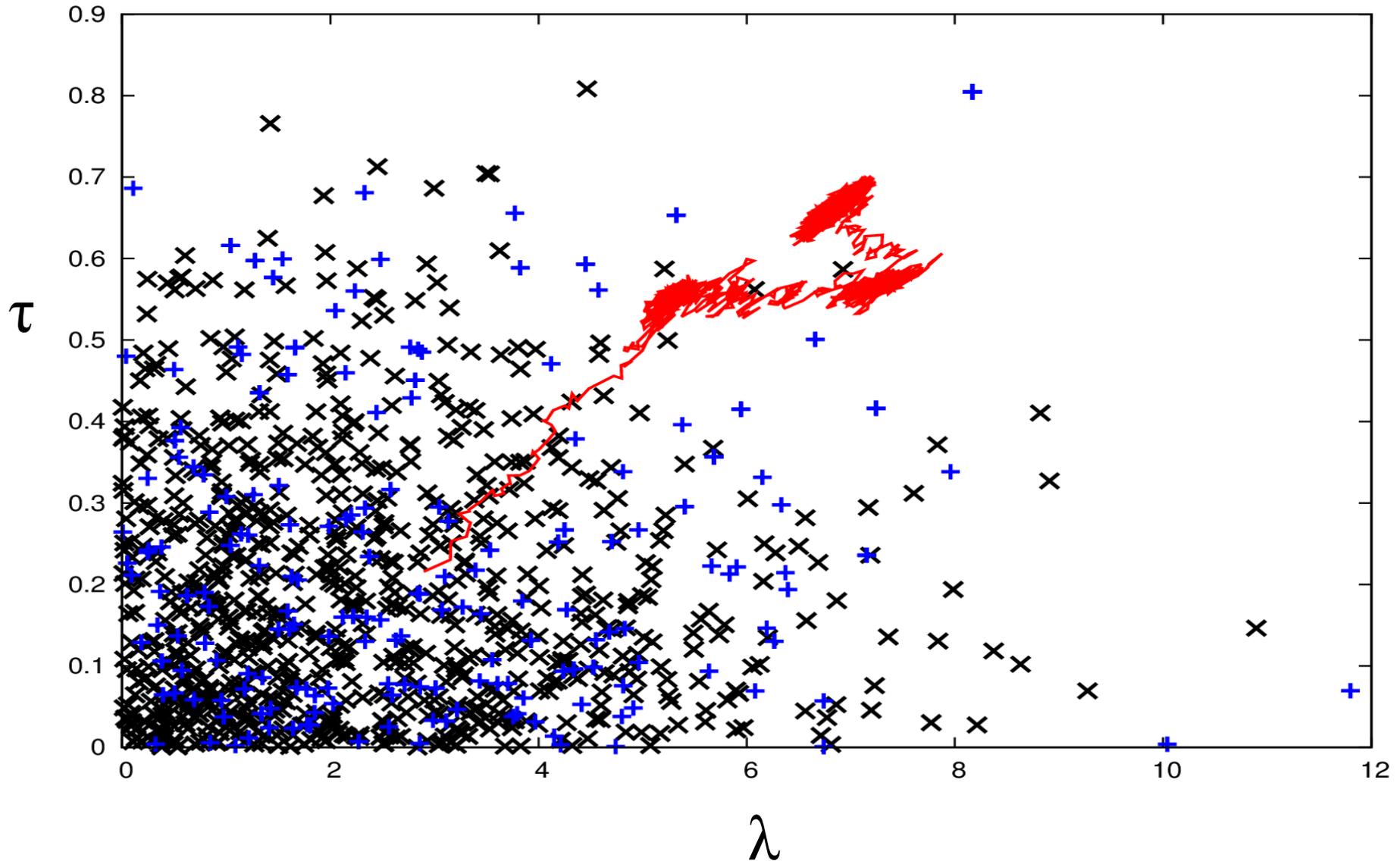
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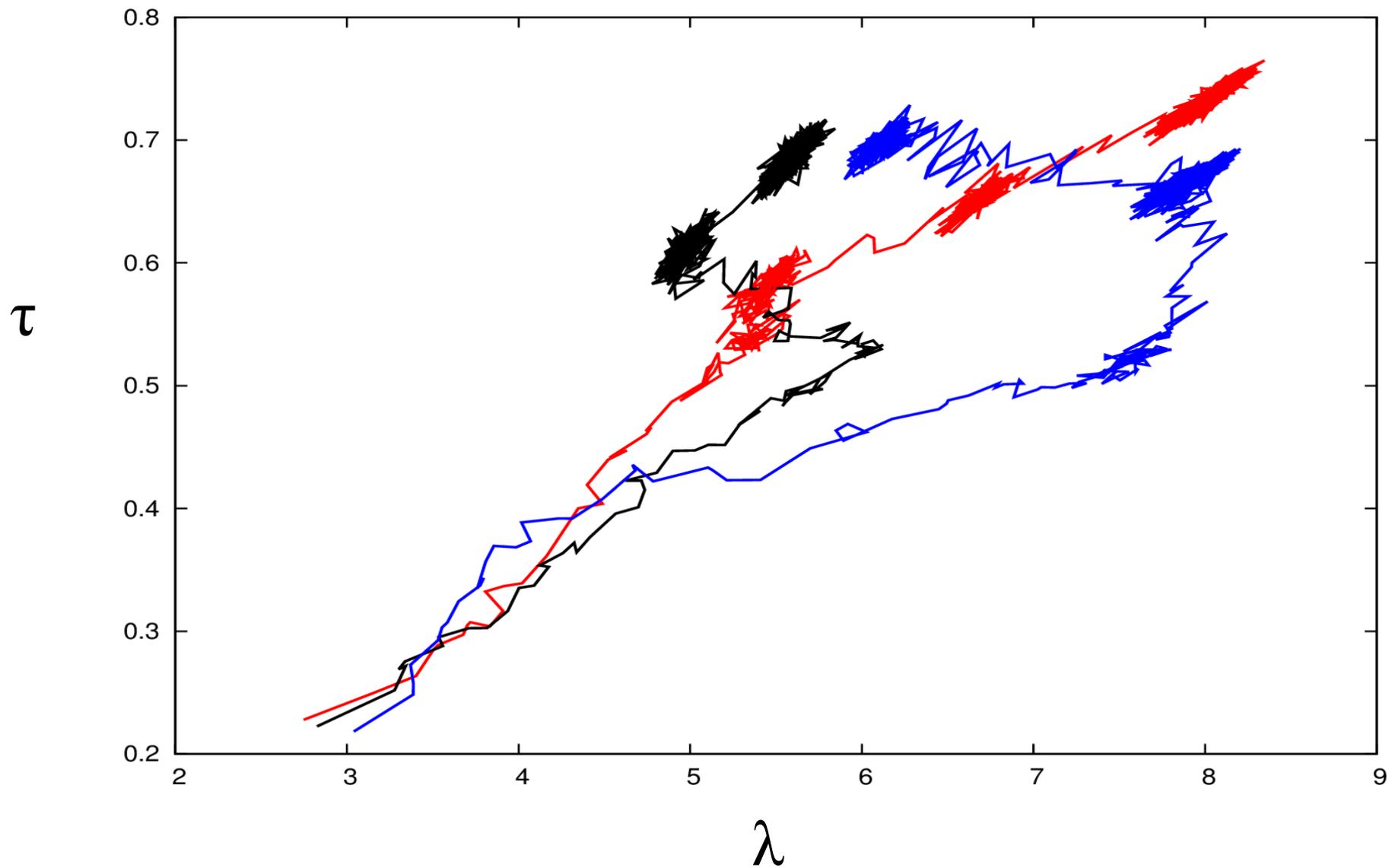
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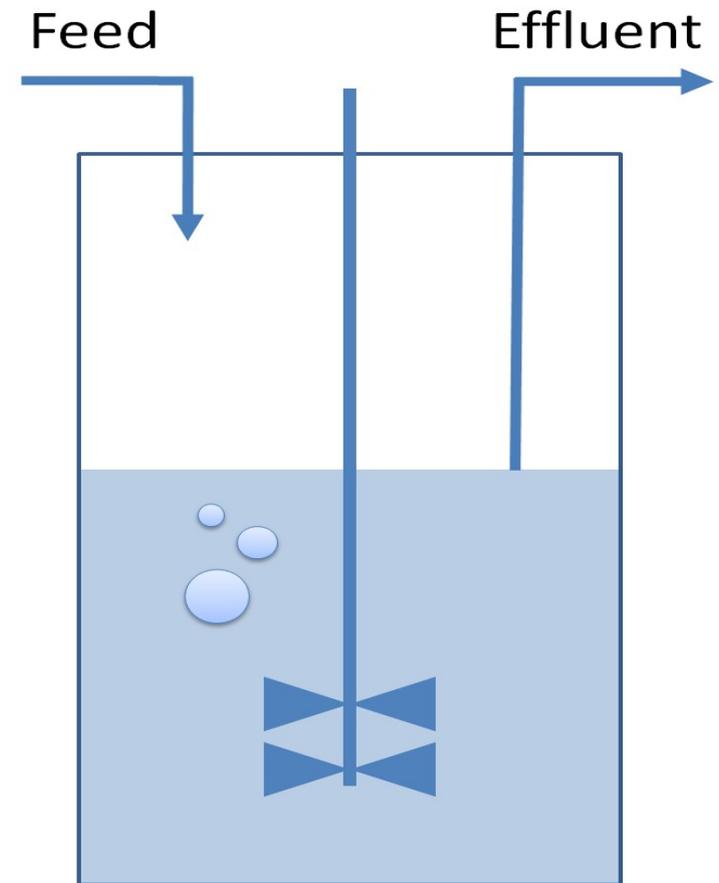


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The model works for well-mixed, fully-connected environment
(e.g. chemostat)



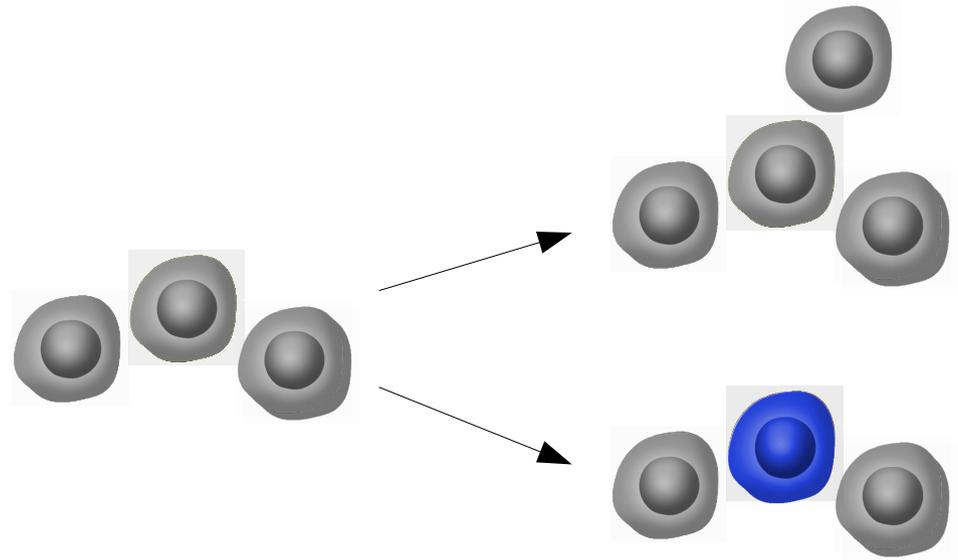
What about space?

Process in two dimensions: Petri Dish

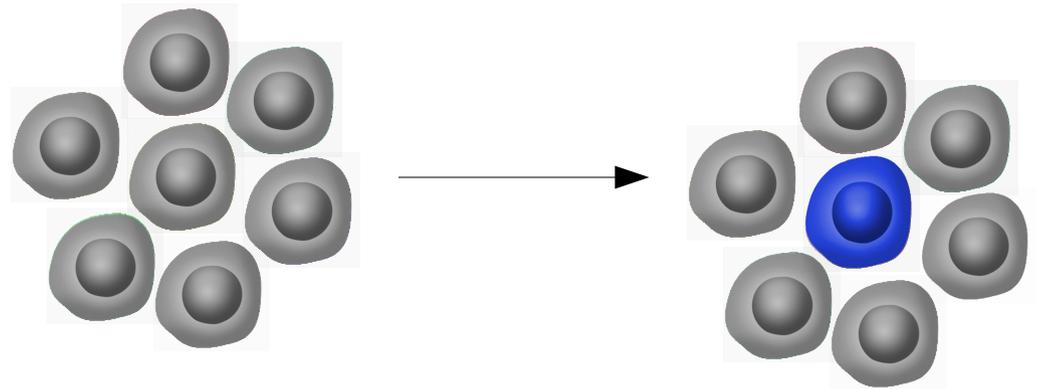


The model

Free space:
reproduce/mutate

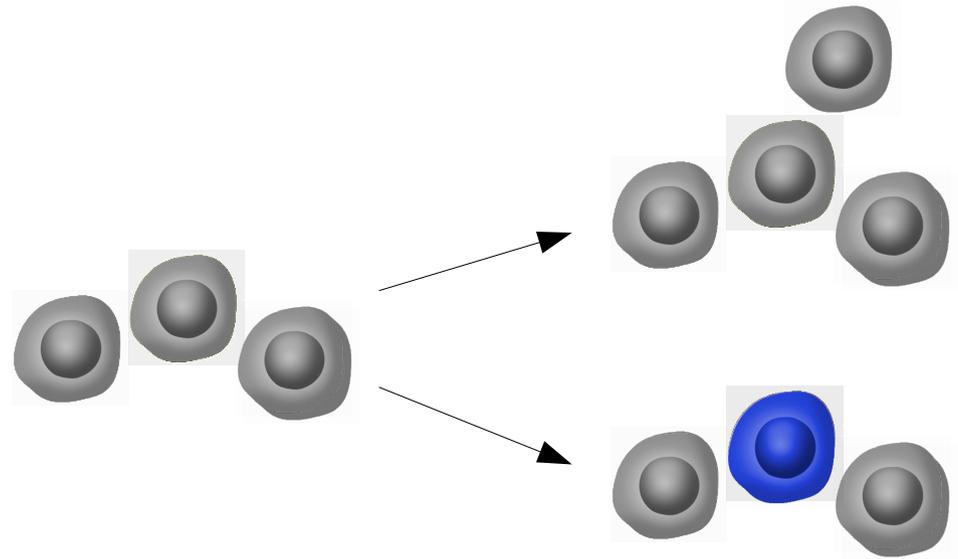


No free space:
mutate only

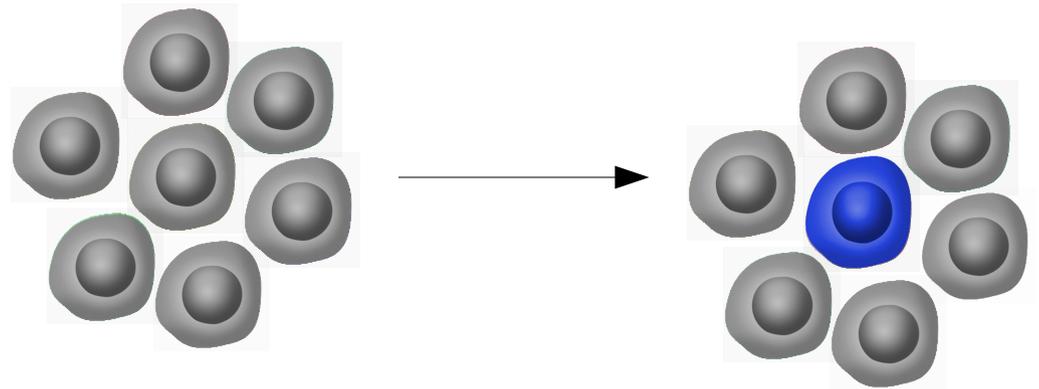


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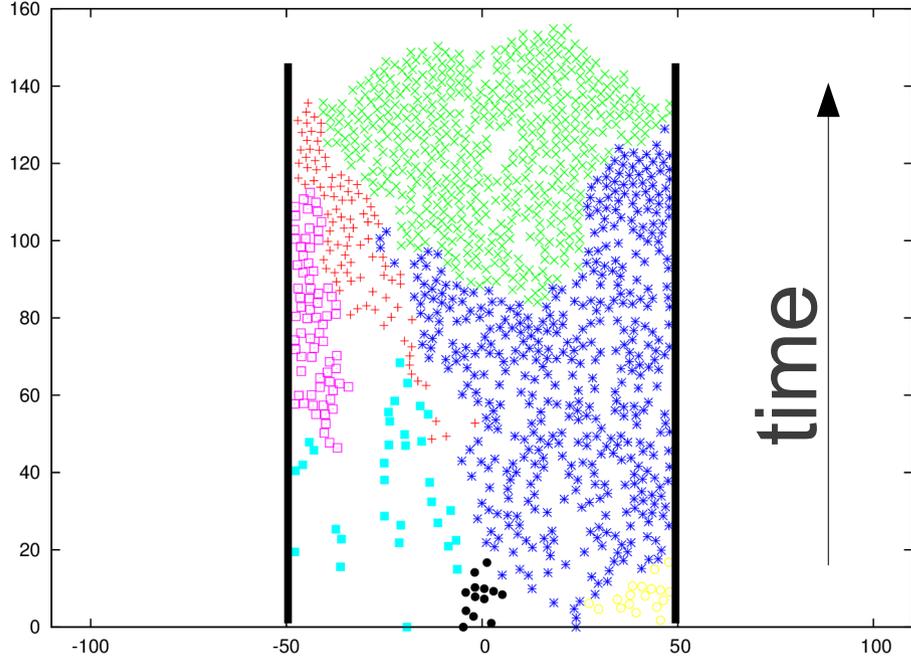
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Results:

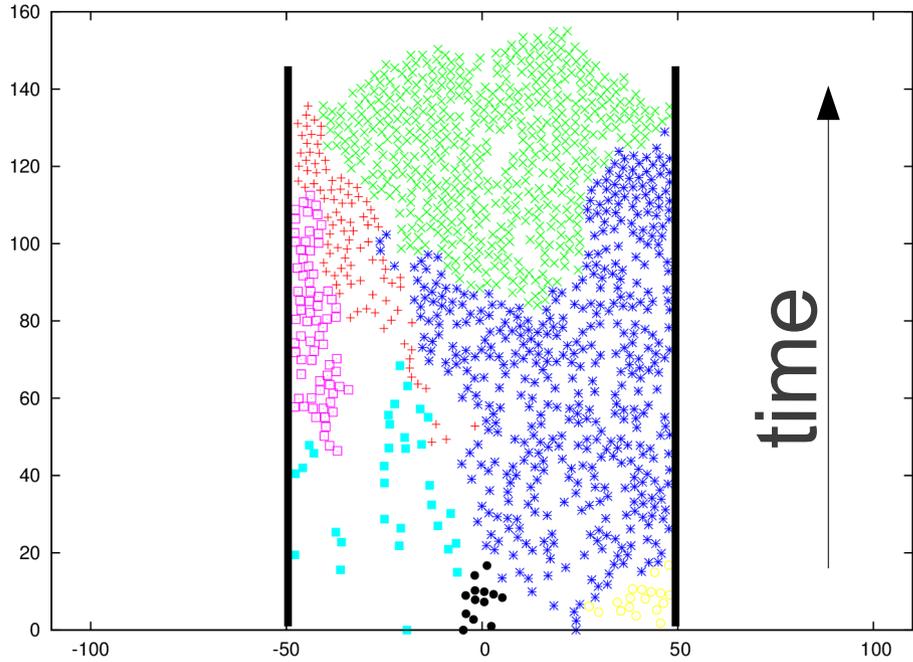
Longer times to
reach condensation

Selection only while
reproduction is active

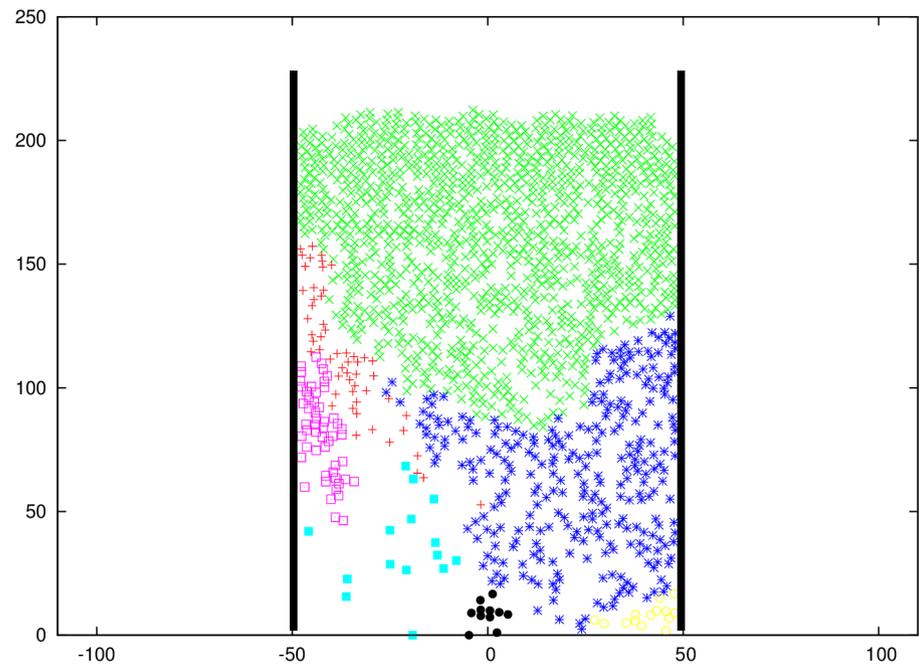


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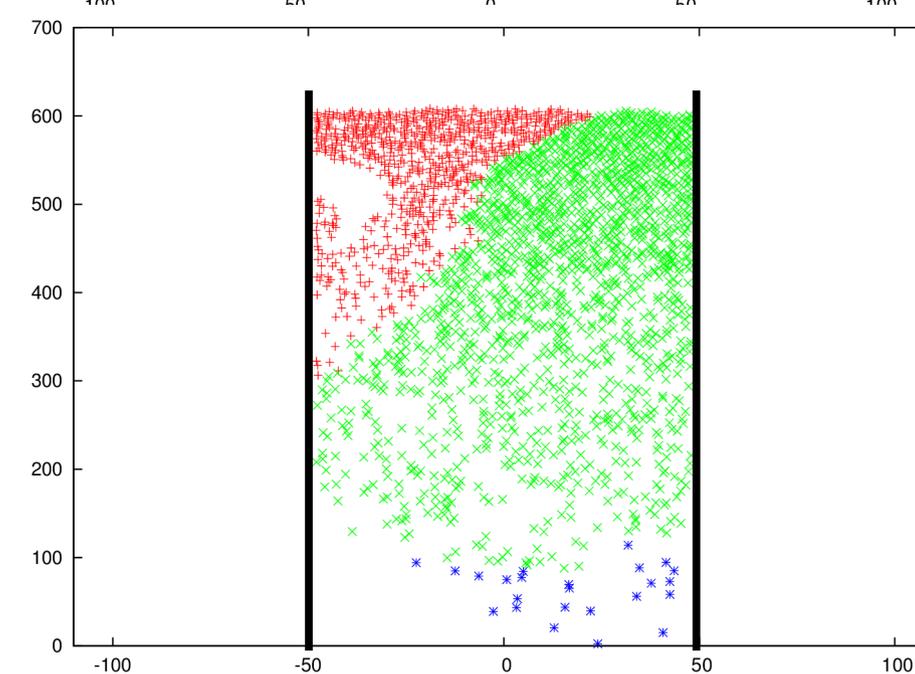
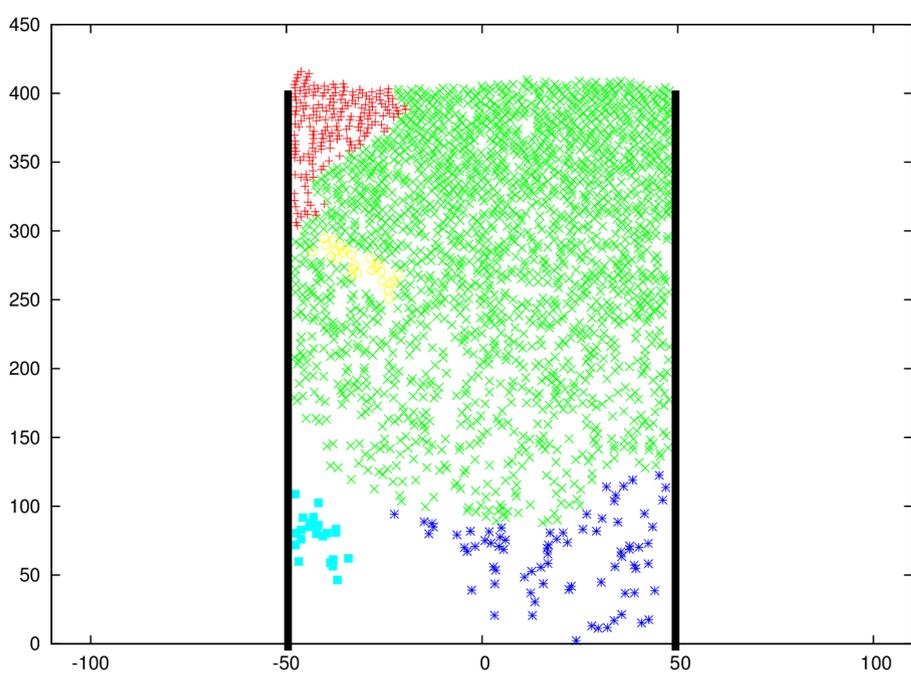
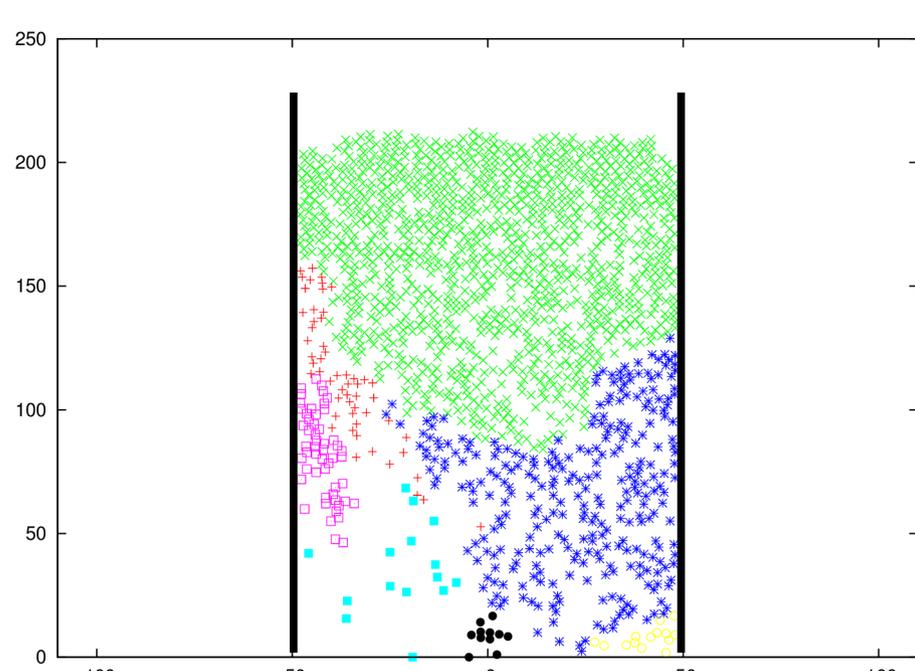
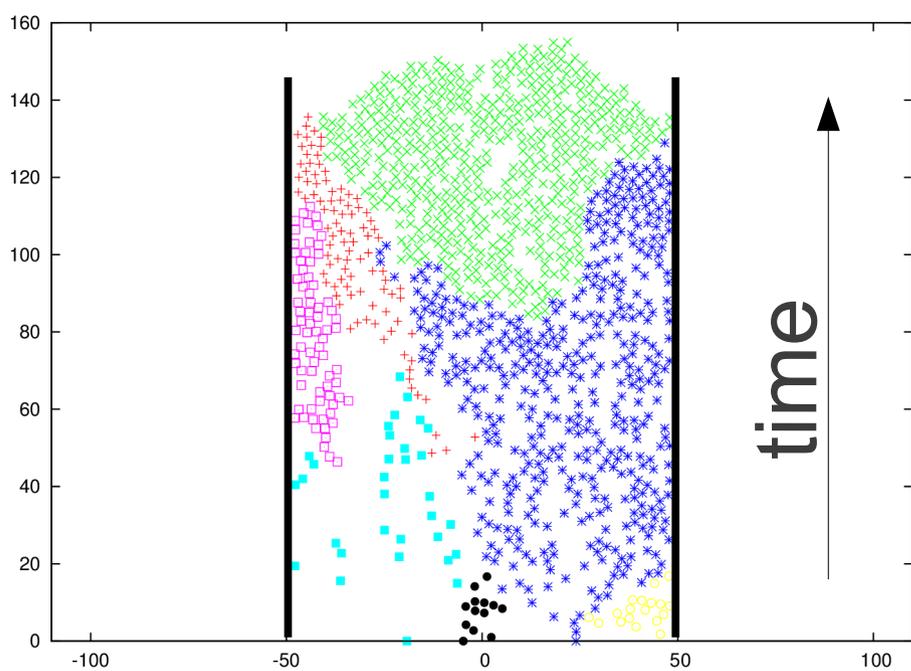
Selection only while
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Longer times to reach condensation



Selection only while reproduction is active



Longer times to
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Selection only while
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And much more...

Thank you.