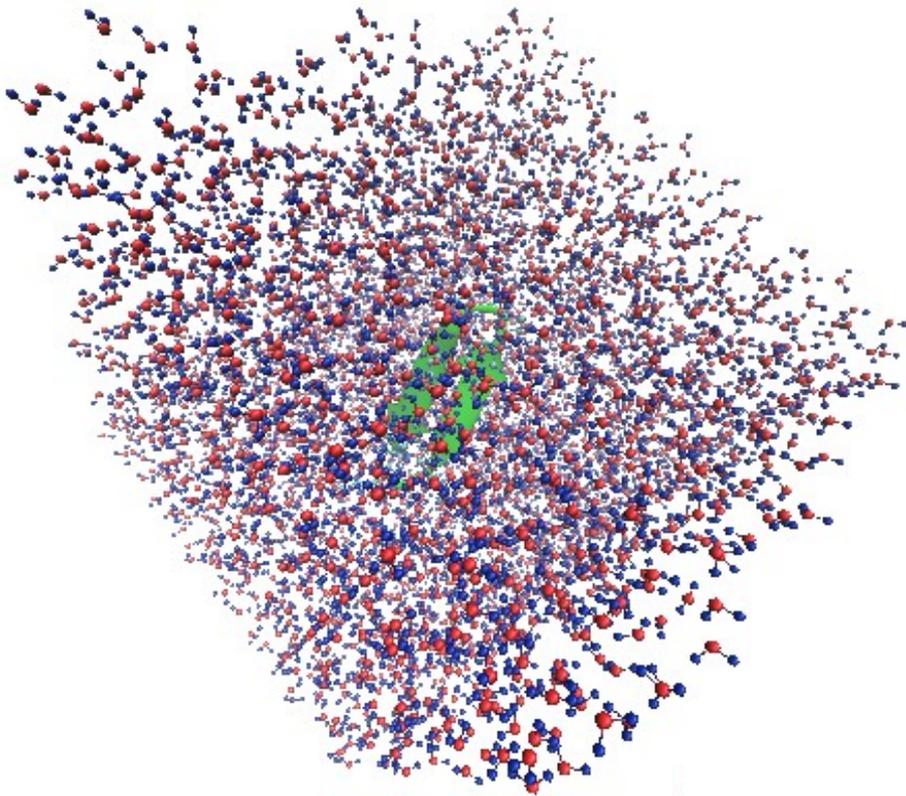


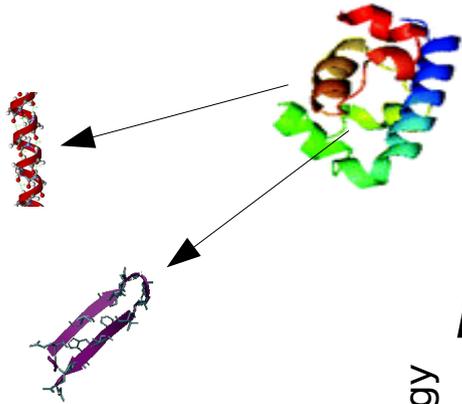
# Computational studies of protein elements in different denaturing conditions



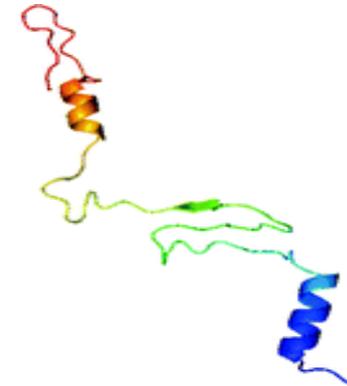
Roberto Meloni

*Milano*  
*18 November 2014*

# Proteins: two-state systems

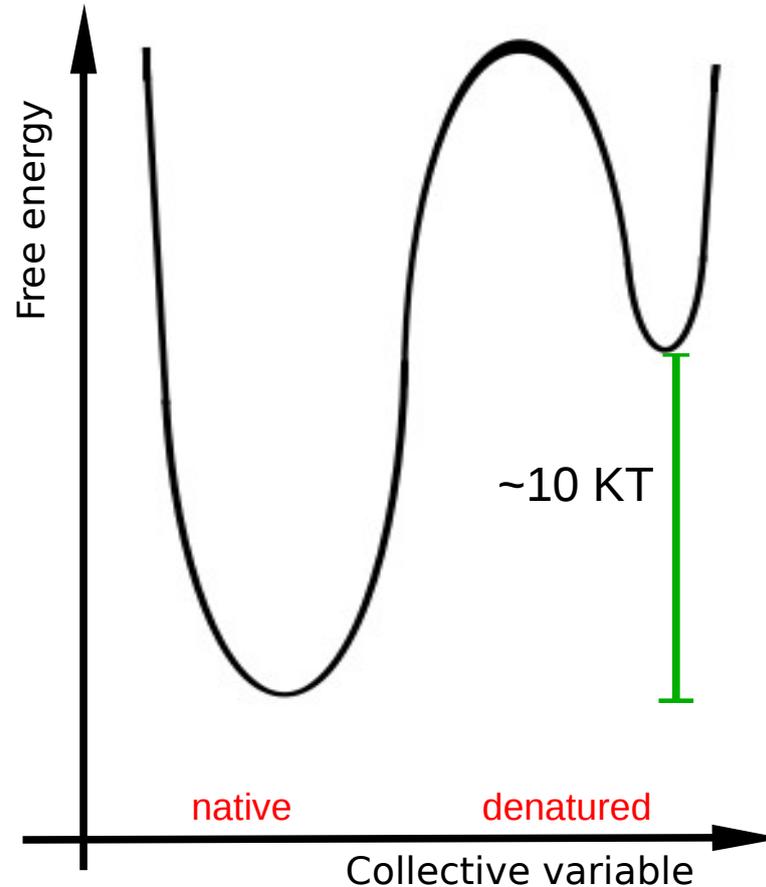


$$\tau \sim 10^{-3} - 10 \text{ s}$$



## NATIVE STATE

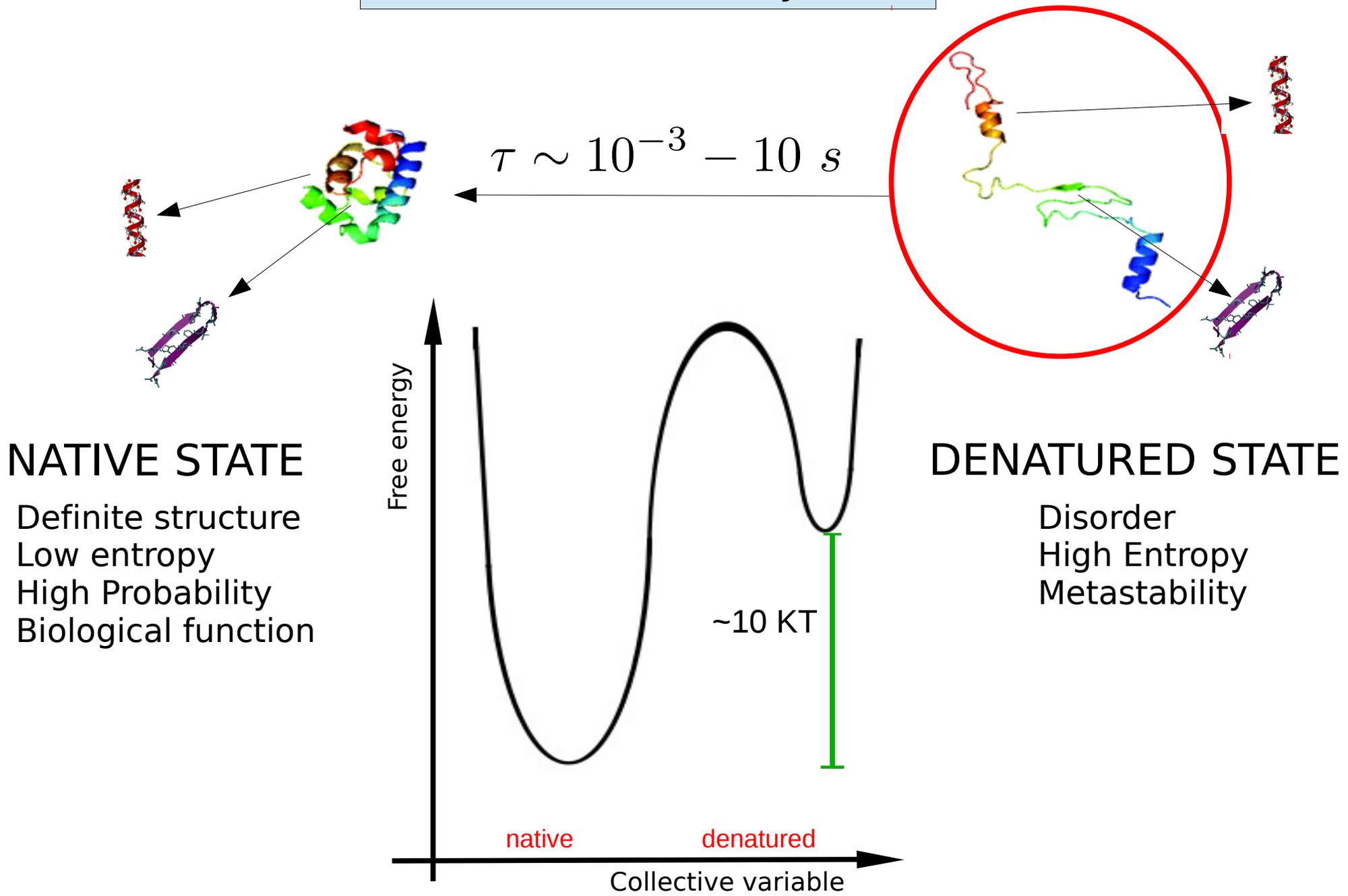
Definite structure  
Low entropy  
High Probability  
Biological function



## DENATURED STATE

Disorder  
High Entropy  
Metastability

# Proteins: two-state systems



# Proteins: two-state systems

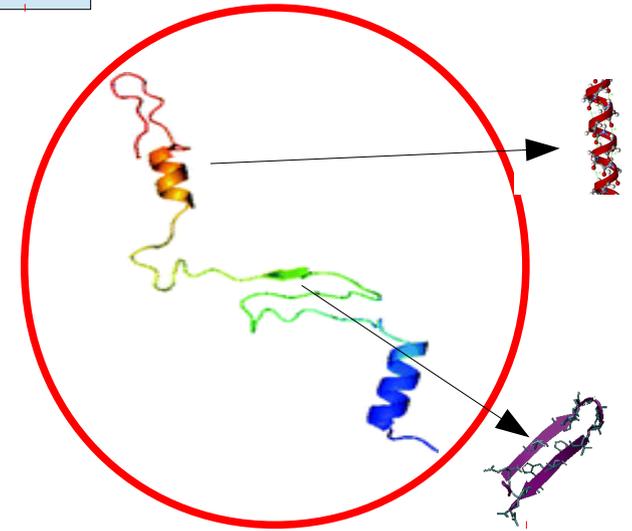
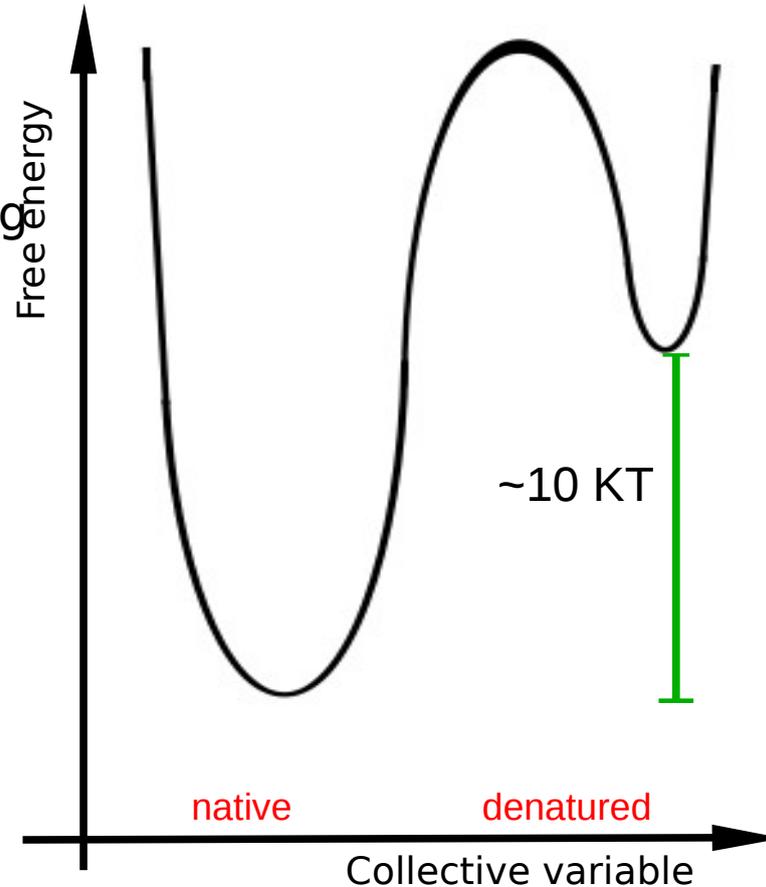
## DENATURED STATE

Mean life:  $\tau \sim 10^{-3} - 10 \text{ s}$



can be achieved by using

- HIGH TEMPERATURE
- CHEMICAL DENATURING AGENTS (urea, guanidine hydrochloride..)



# Proteins: two-state systems

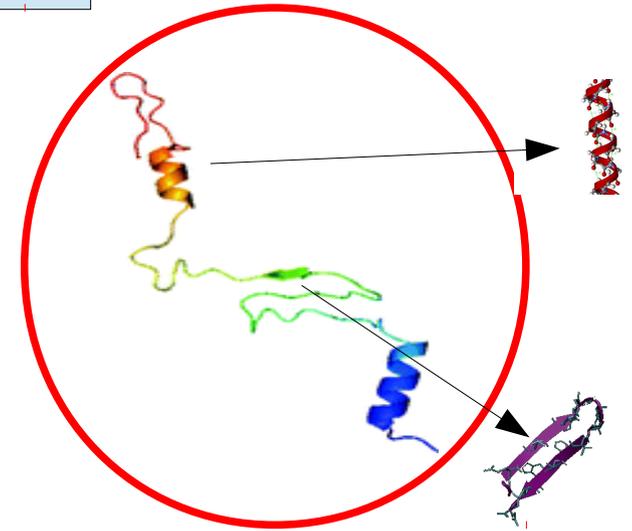
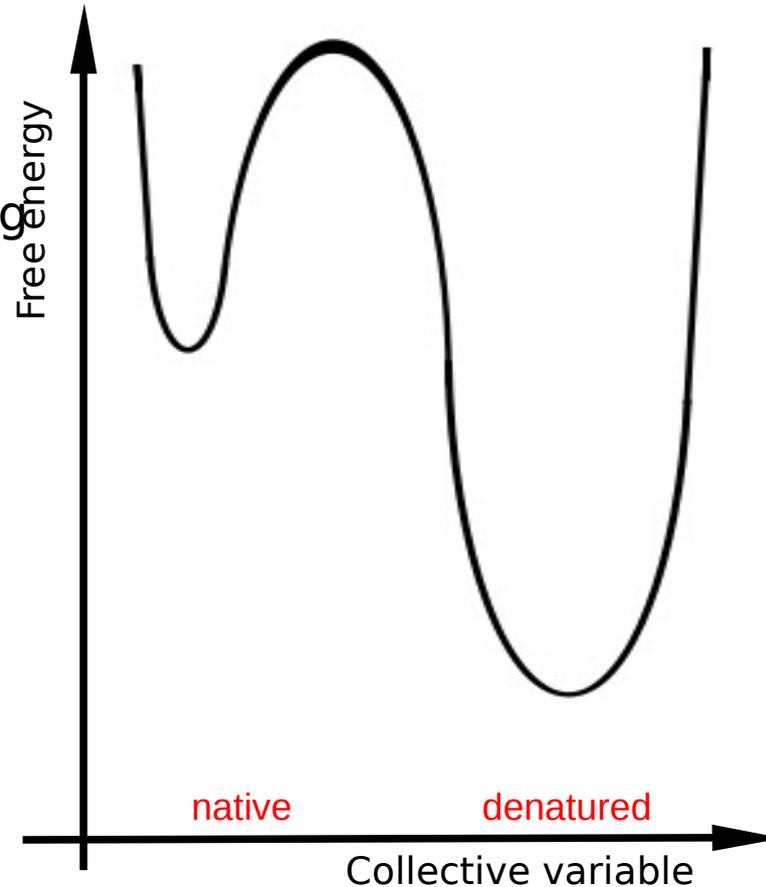
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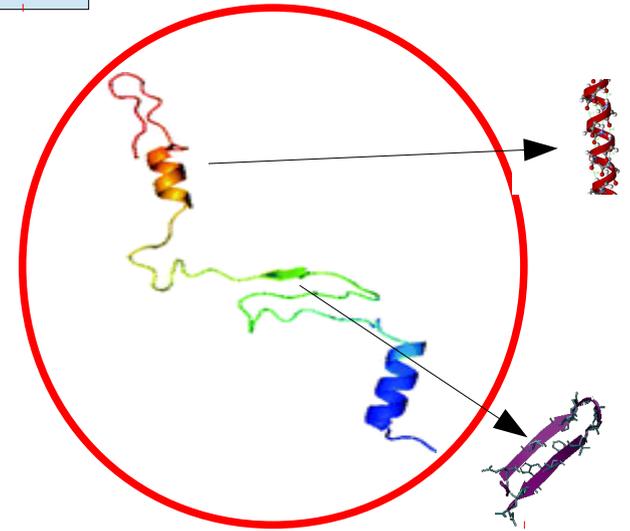
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# Proteins: two-state systems

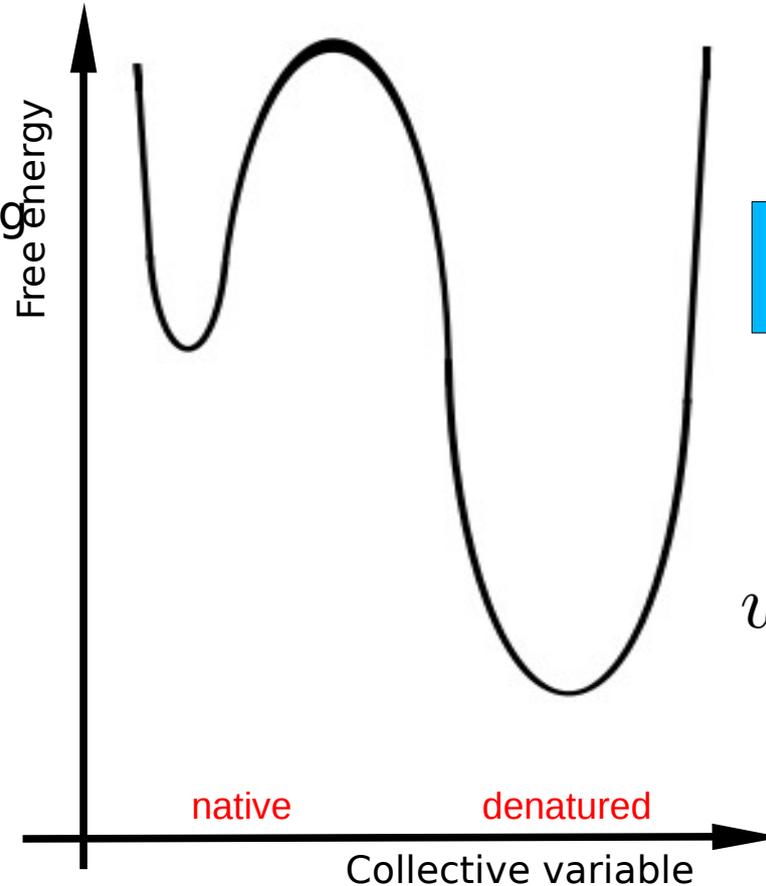
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- HIGH TEMPERATURE
- CHEMICAL DENATURING AGENTS (urea, guanidine hydrochloride..)



in physiological conditions?  
300 K, water

TROUBLE

*water*  $\neq$  *urea*  
*guanidine*

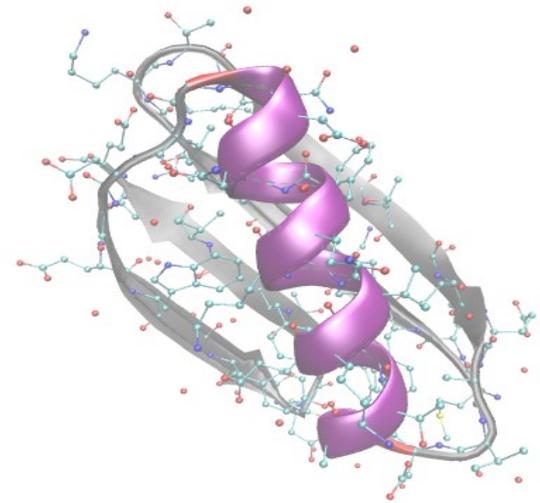
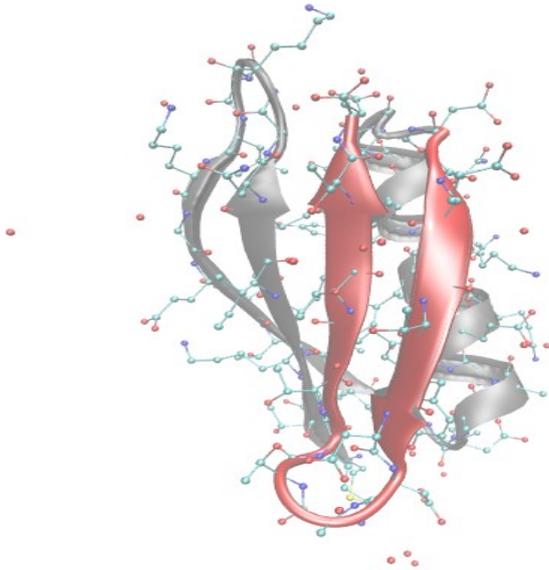
Simplify the question  
working on the building blocks

Every different protein has its own thermodynamic properties..

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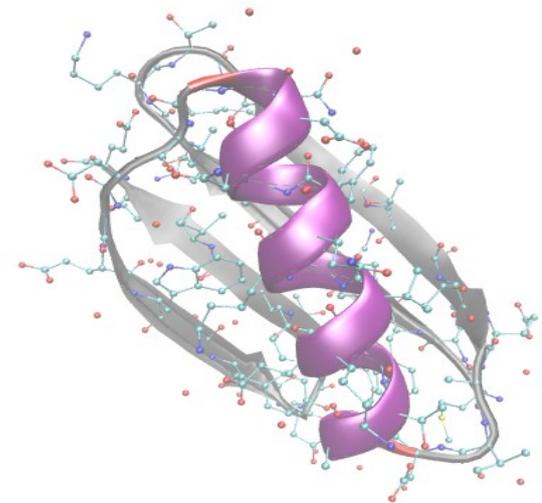
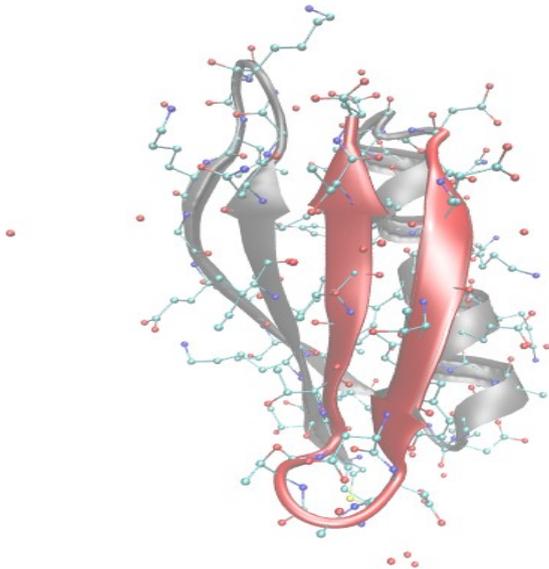
..but quite everyone is made of  $\alpha$ -helices and  $\beta$ -sheets.



## Simplify the question working on the building blocks

Every different protein has its own thermodynamic properties..

..but quite everyone is made of  $\alpha$ -helices and  $\beta$ -sheets.



Work on the “building blocks” of proteins and analyse their behaviour in different chemical conditions.

- Water
  - Urea
  - Guanidine
- ▶ PHYS. CONDITIONS
- } DENATURING AGENTS

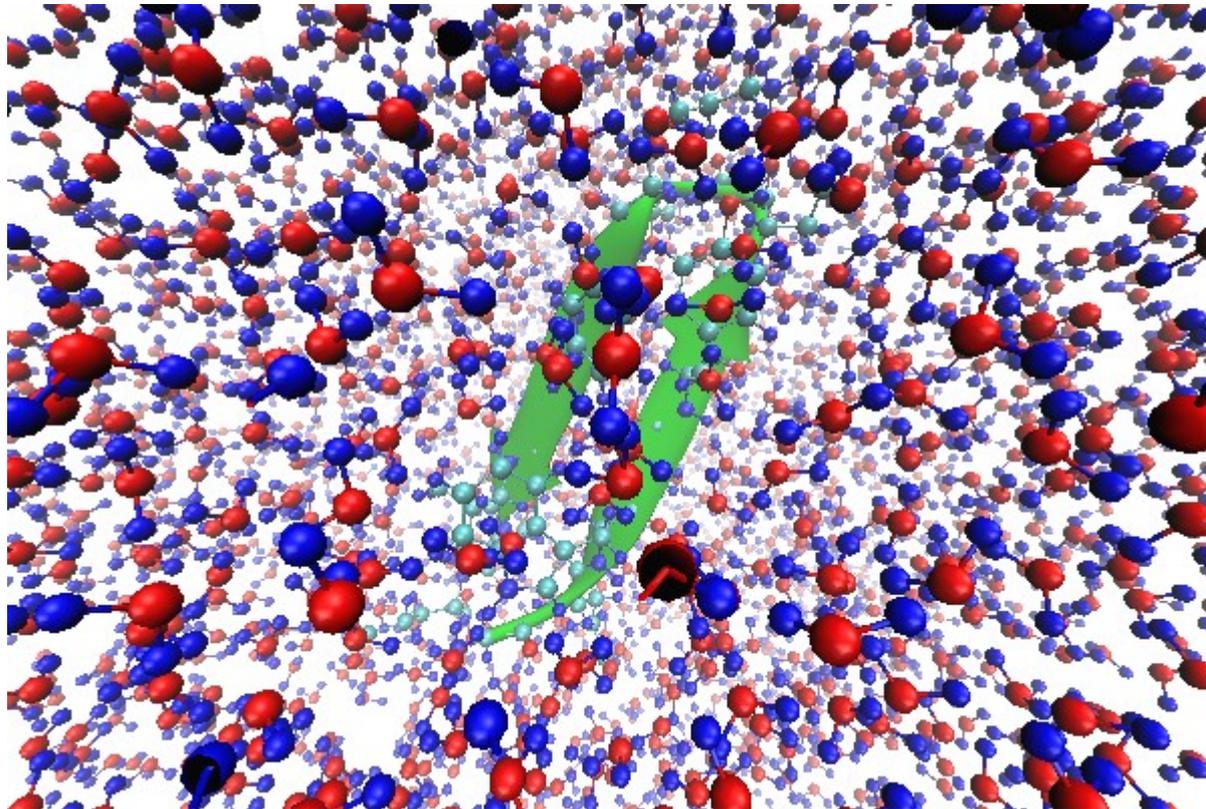
# Molecular dynamics simulations

NVT ensemble at 300 K

Cubic box, side:  $\sim 5$  nm

$\sim 11$ - $17$ k atoms per simulation (explicit solvent)

$$H_0 = T + V_{coul} + V_{vdw} + V_{bonds} + V_{angles} + V_{torsion}$$



# TROUBLES

1) overcoming of free energy barriers

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we want to perform equilibrium averages

EFFICIENT  
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EQUILIBRIUM

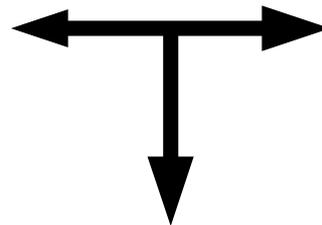
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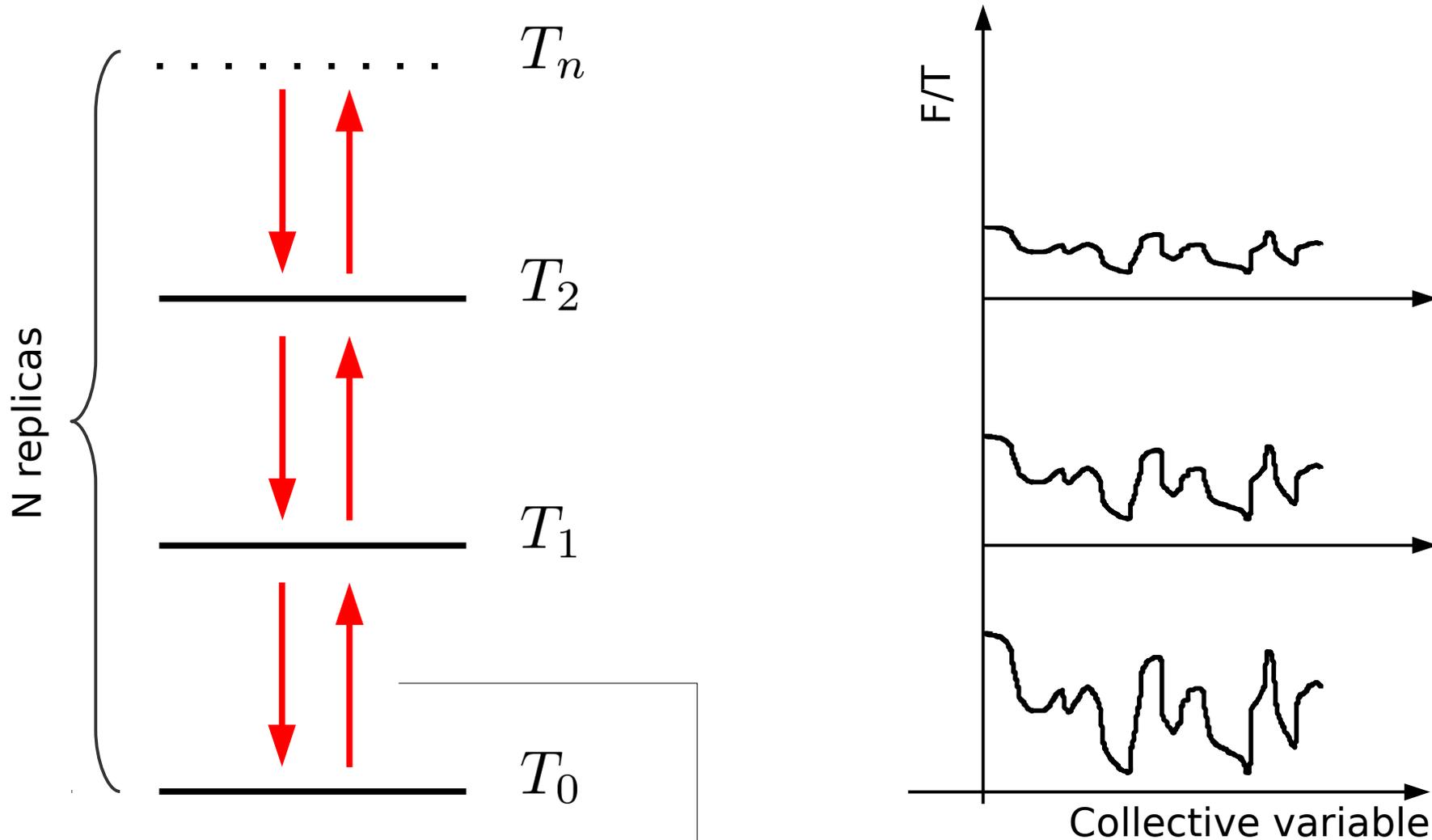
EQUILIBRIUM

a lot of computational time is needed to achieve these goals

→ must find some trick to speed up the simulation

1

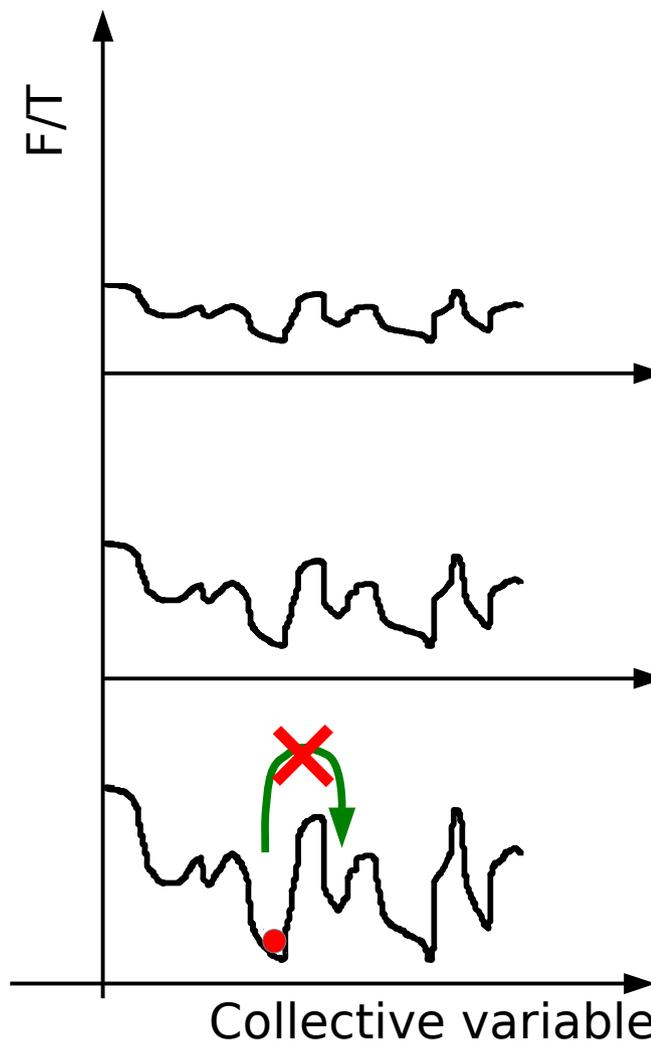
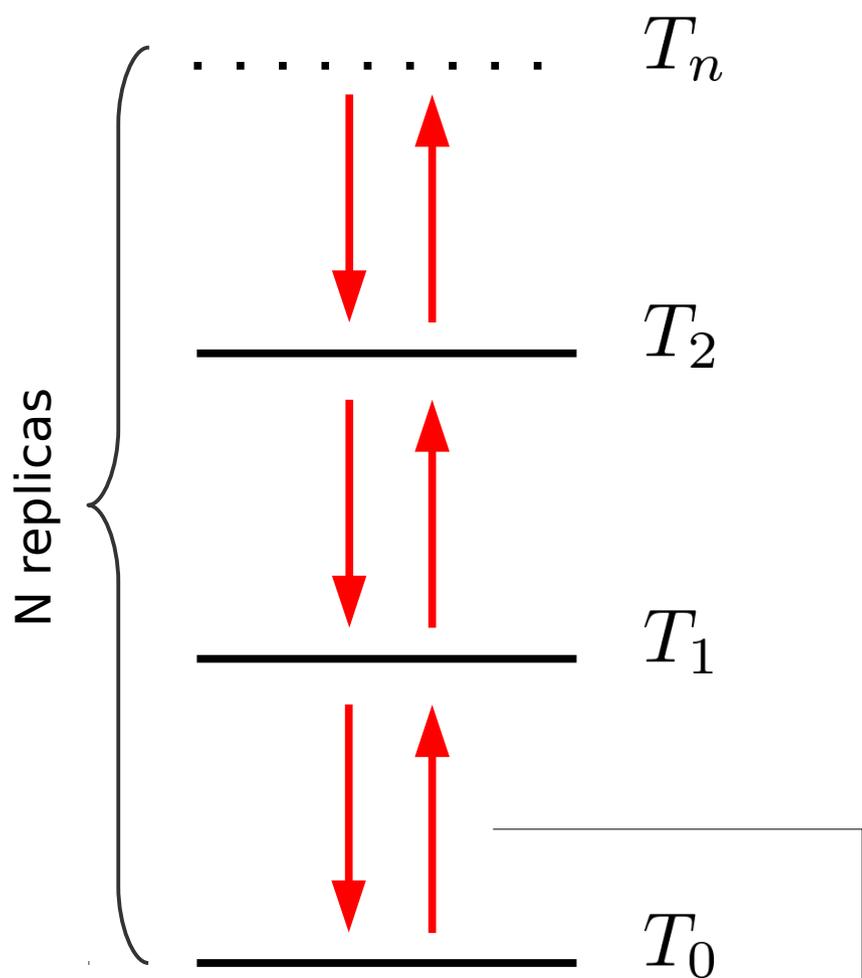
Advanced sampling methods:  
usual replica-exchange scheme



Metropolis criterion  
keeps every replica in its  
canonical ensemble

1

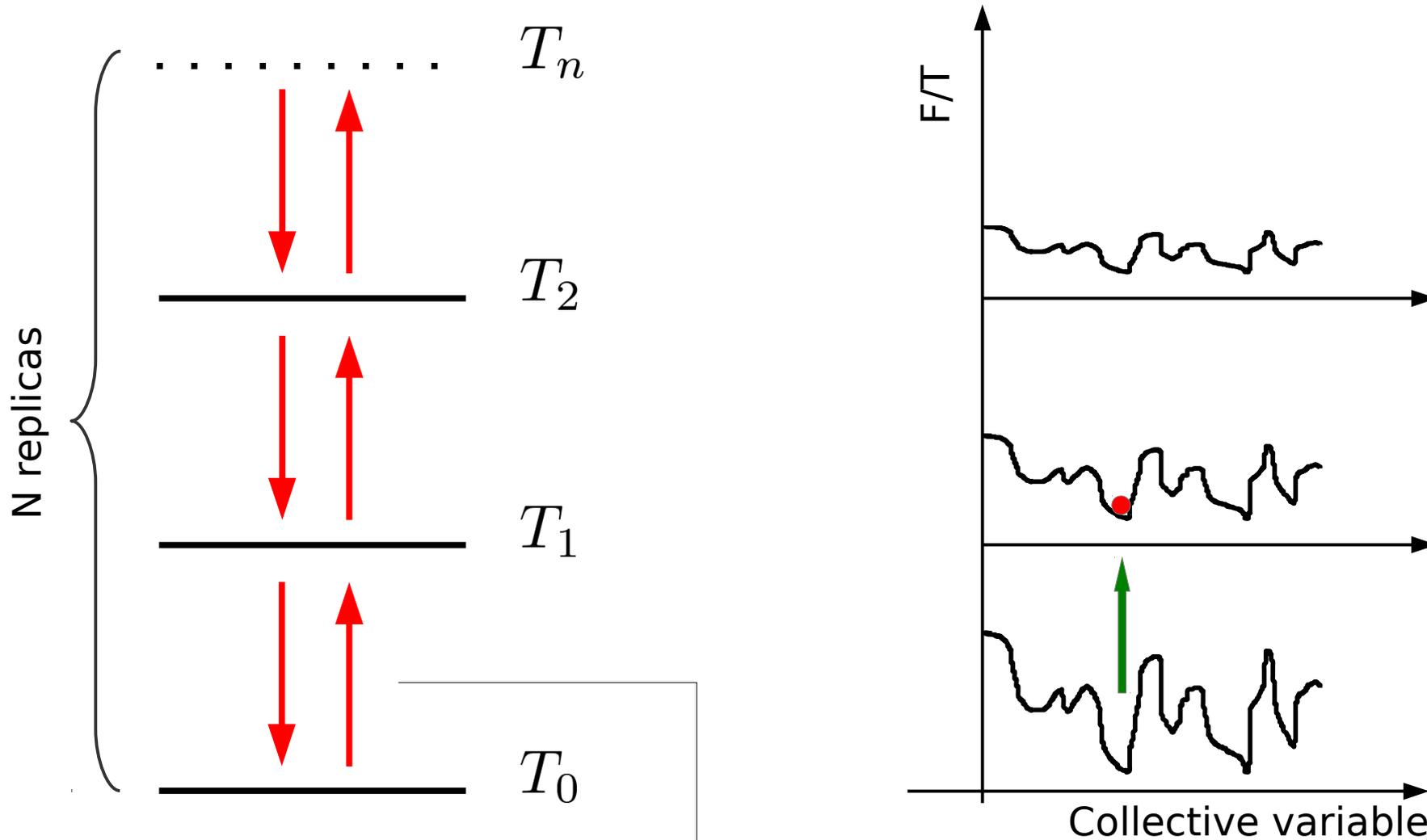
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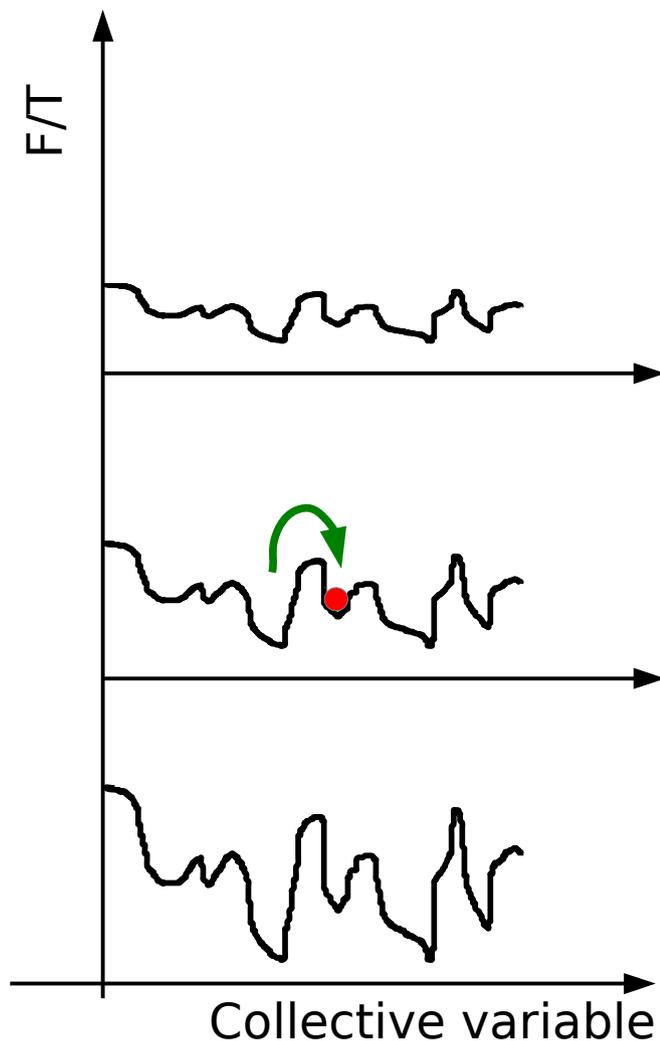
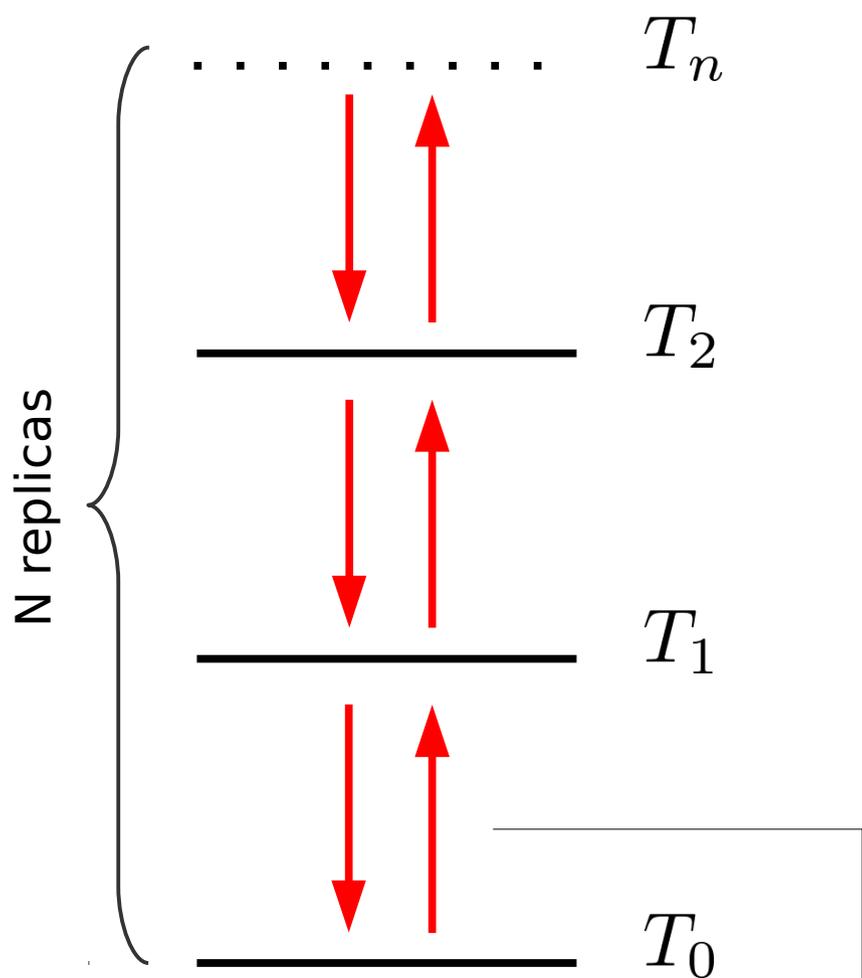
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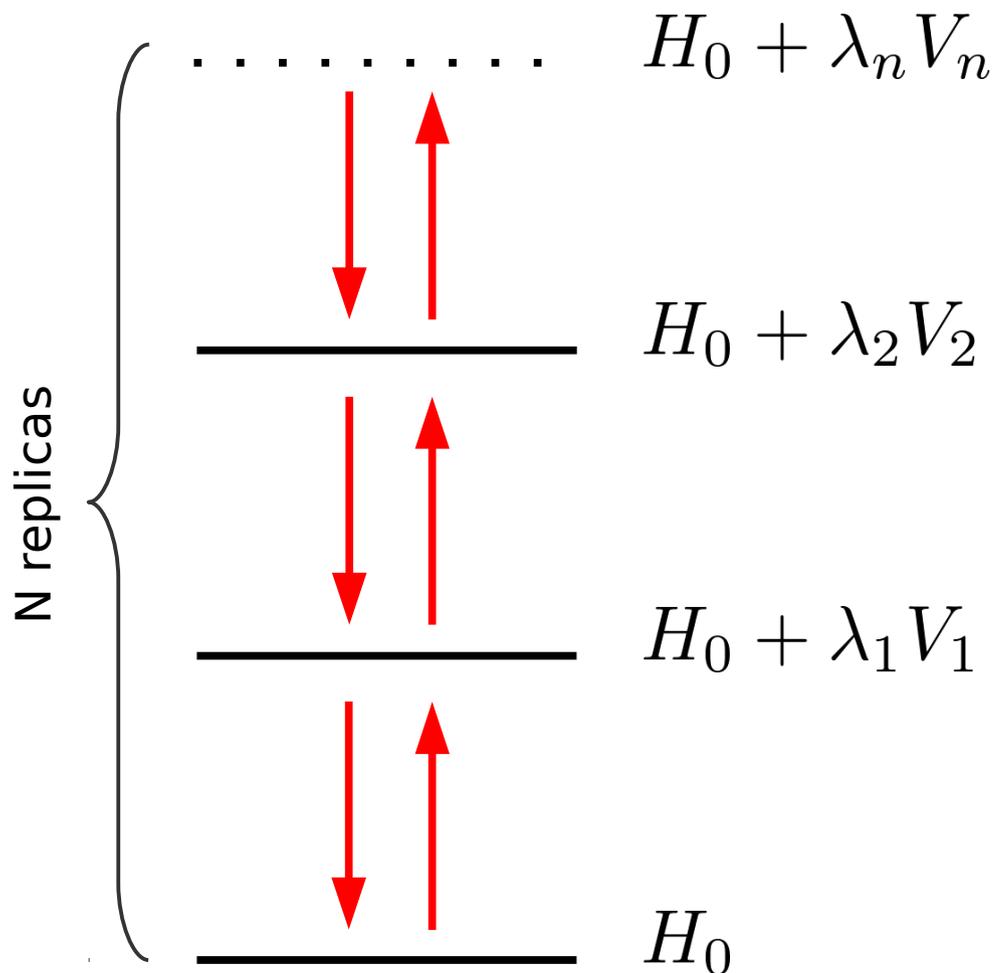
Advanced sampling methods:  
usual replica-exchange scheme



Metropolis criterion  
keeps every replica in its  
canonical ensemble

2

Advanced sampling methods:  
hamiltonian replica-exchange



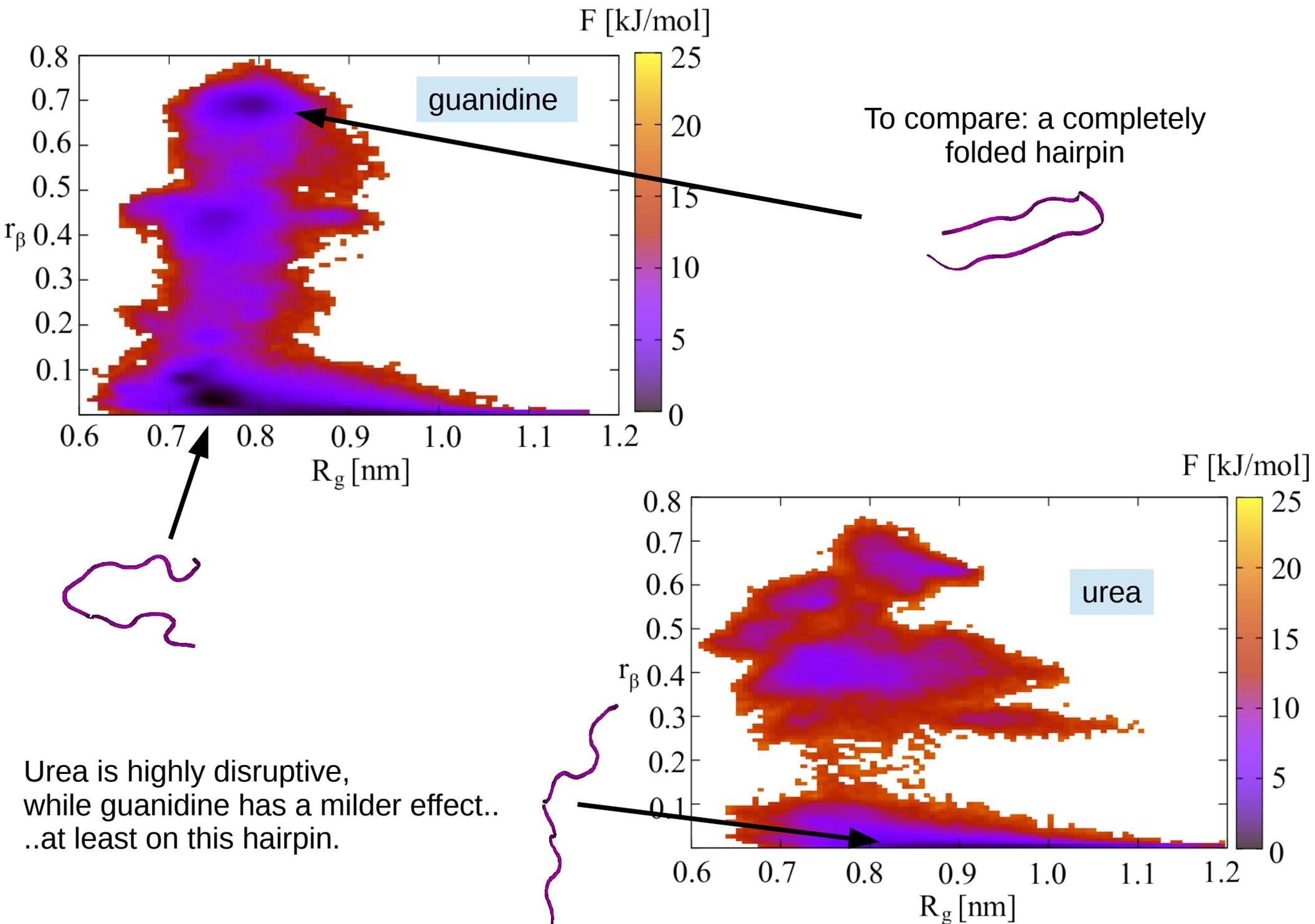
Generally,

$$H = H_0 + \lambda V$$

where

$$V = \frac{1}{2}(\xi - \xi_0)^2$$

$$\xi = \xi(\mathbf{p}, \mathbf{q})$$



3

# Advanced sampling methods: metadynamics



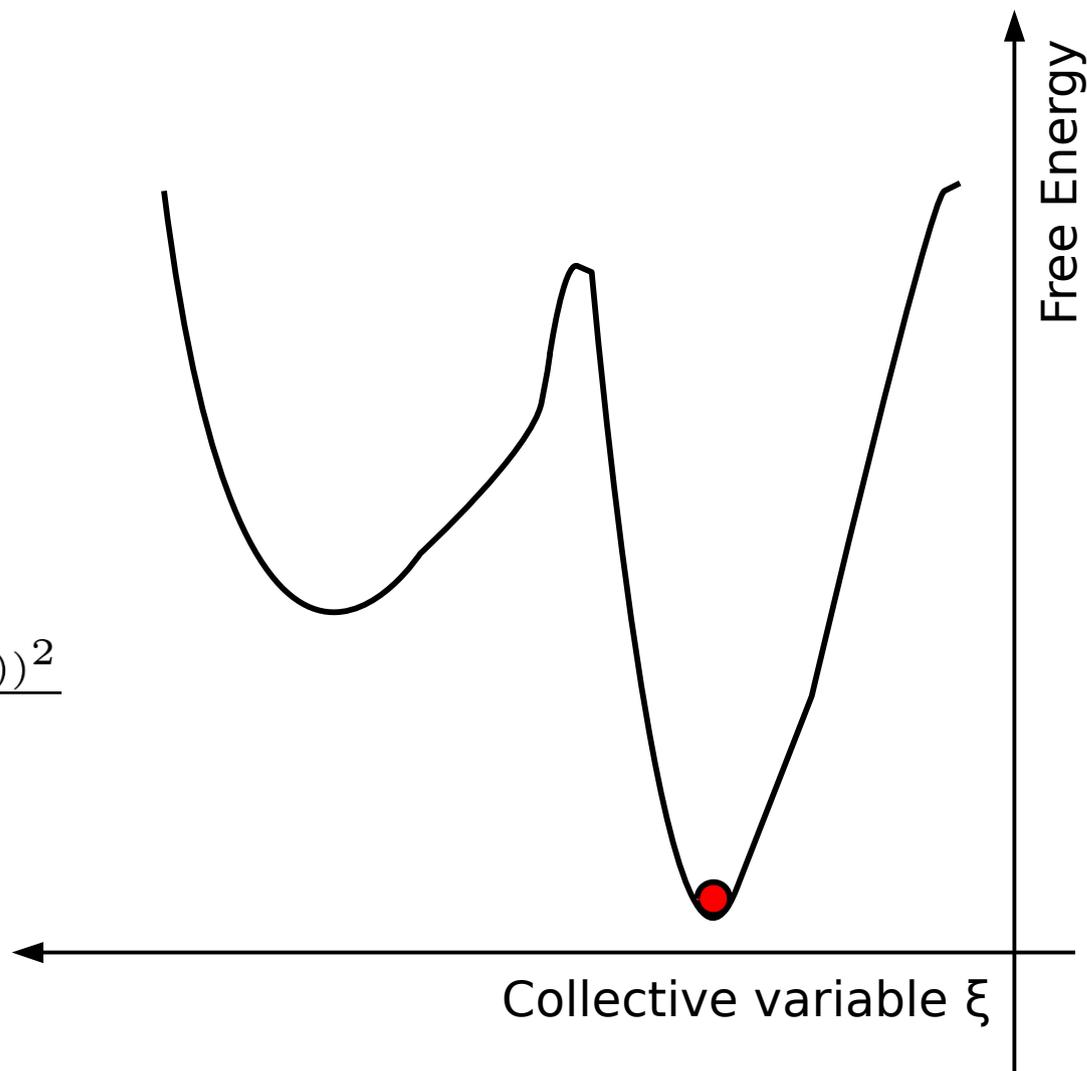
try a new approach:

$$H = H_0 + V(\xi, t)$$

where

$$V(\xi, t) \propto \sum_{t' < t} e^{-\frac{(\xi - \xi(t'))^2}{2\sigma^2}}$$

$$\xi = \xi(\mathbf{p}, \mathbf{q})$$



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# Advanced sampling methods: metadynamics



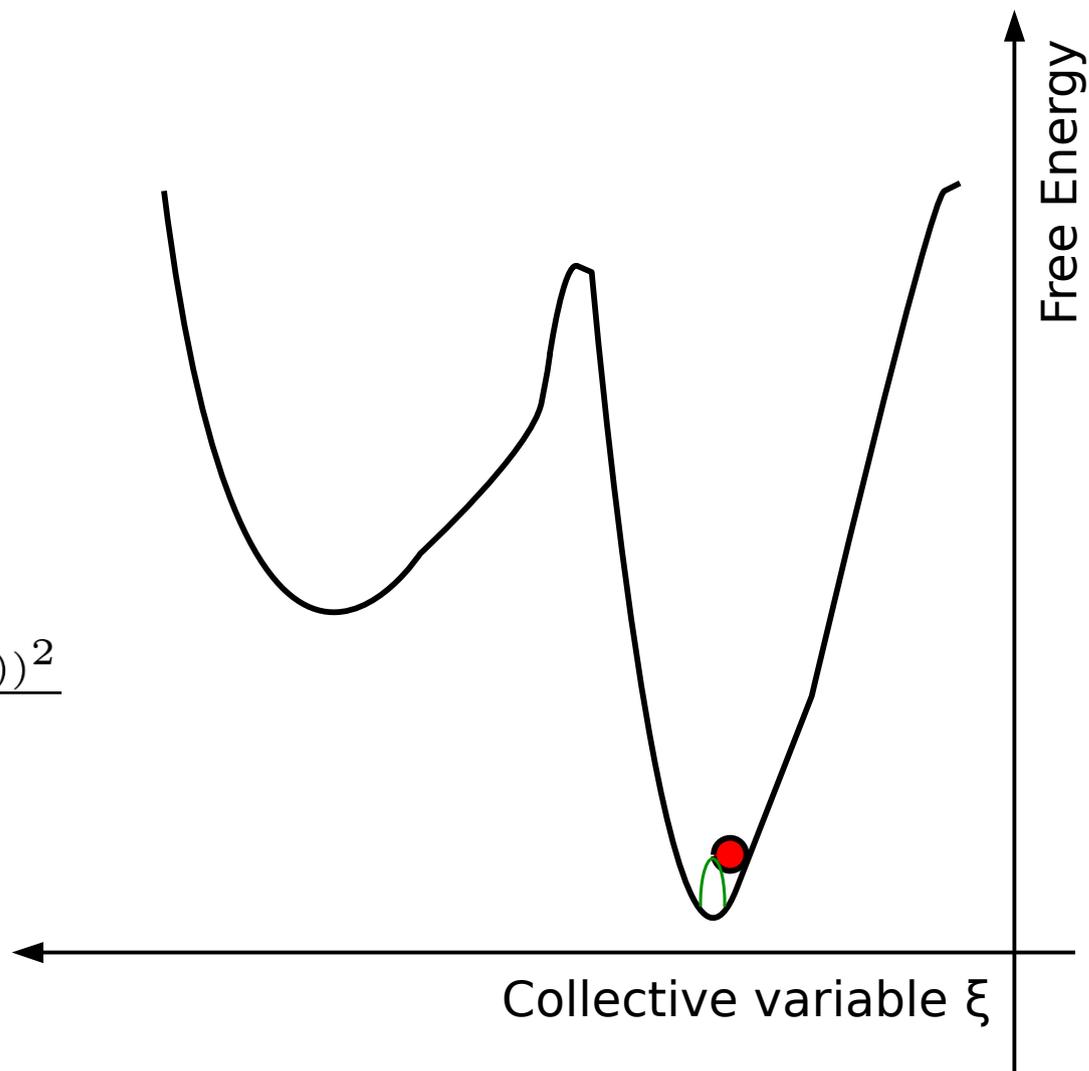
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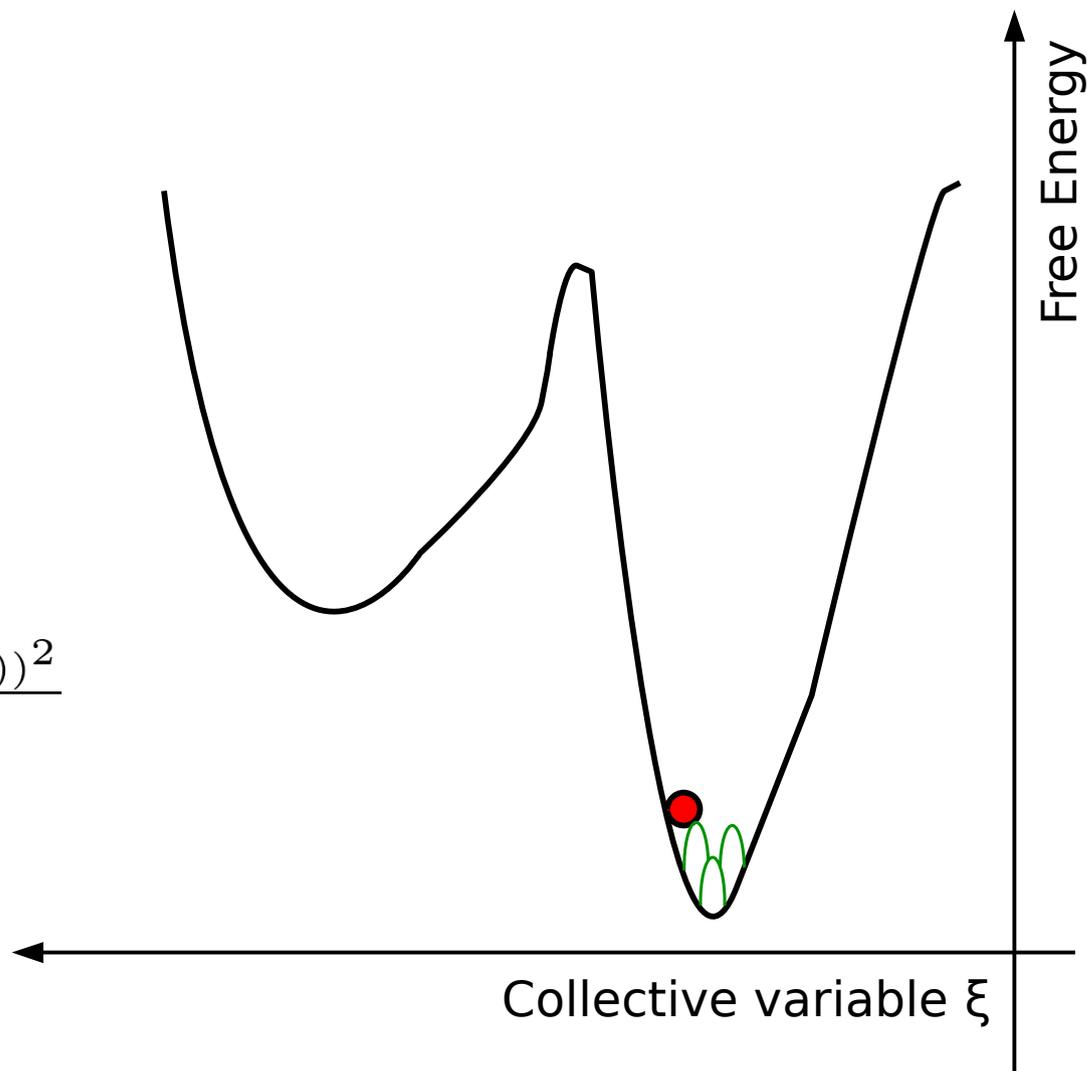
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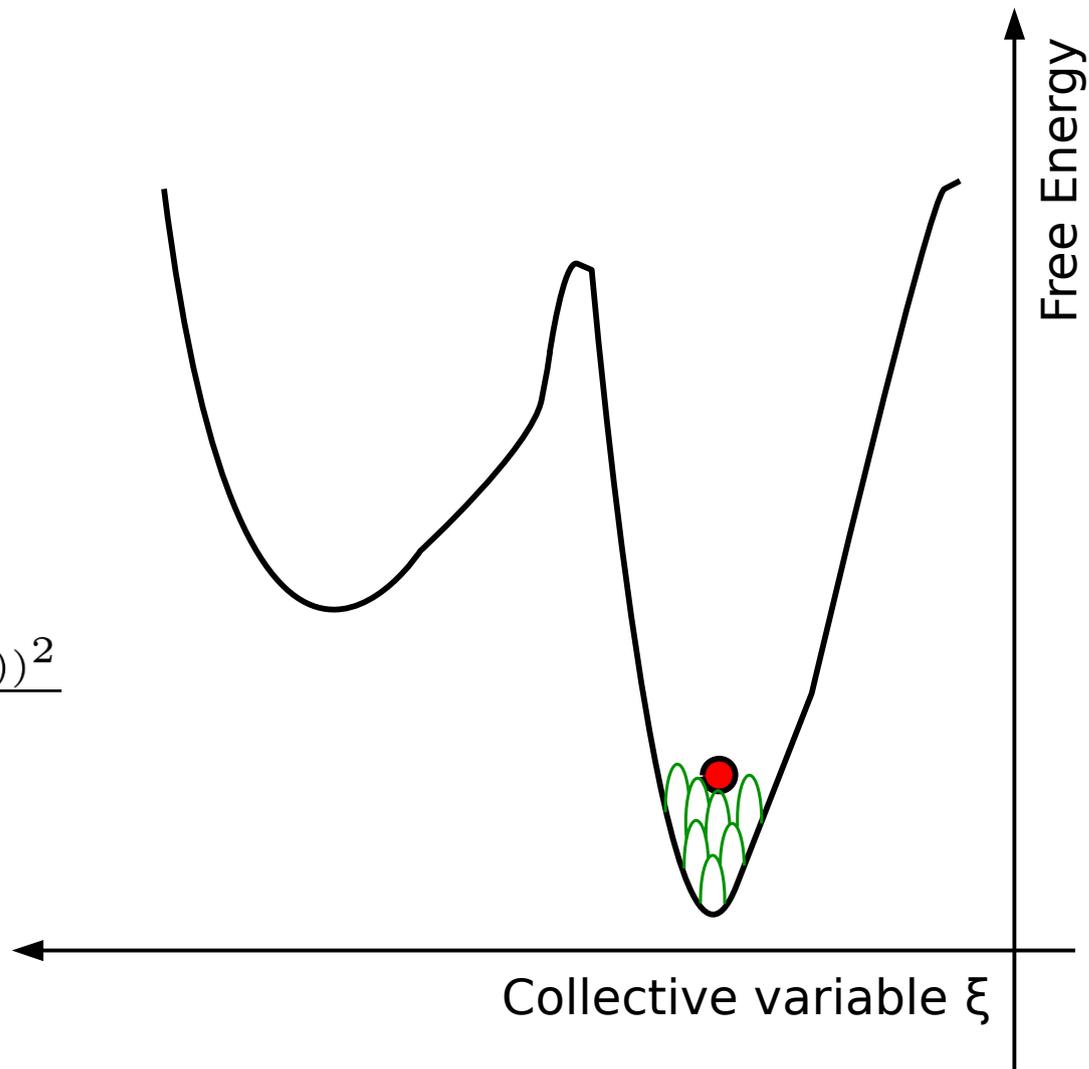
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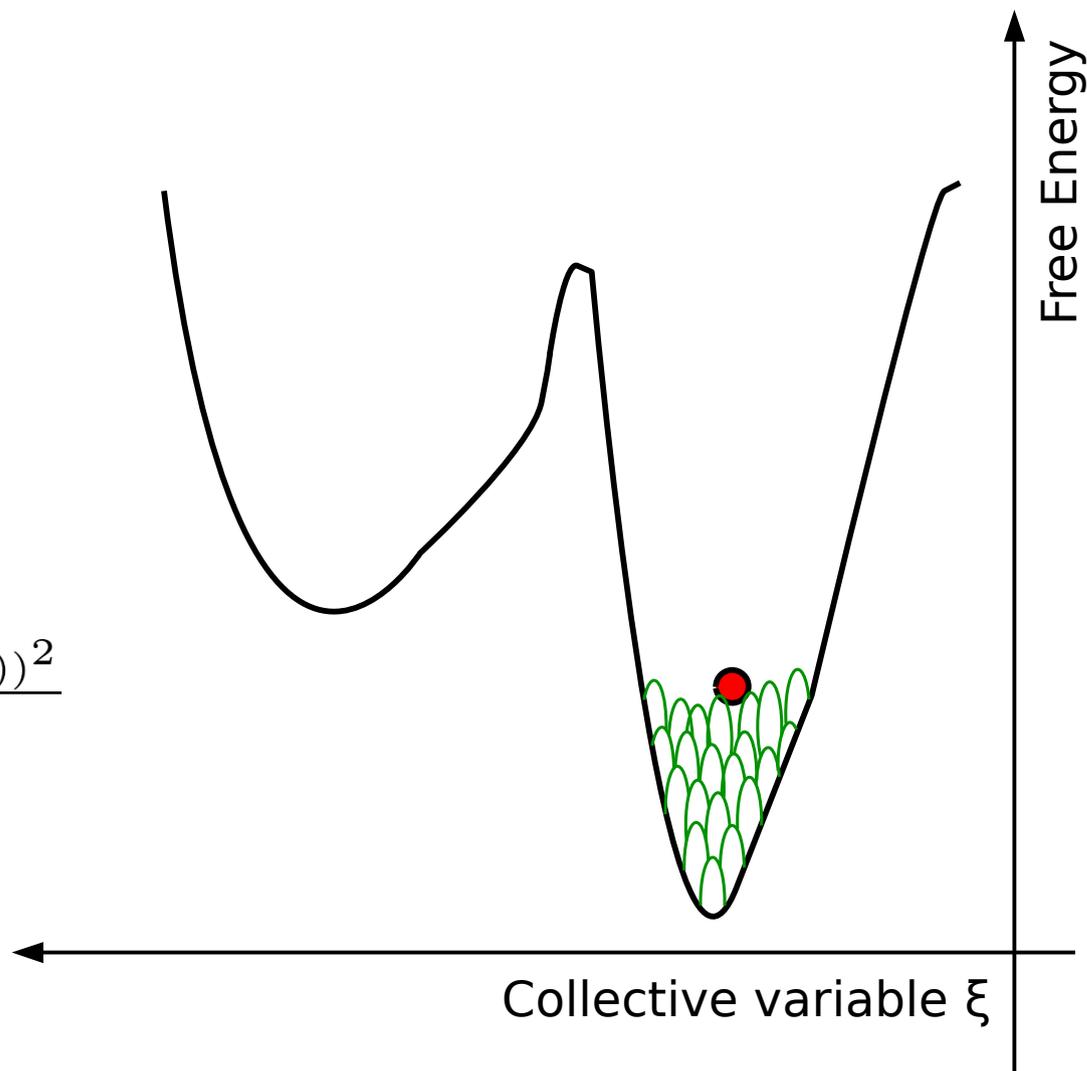
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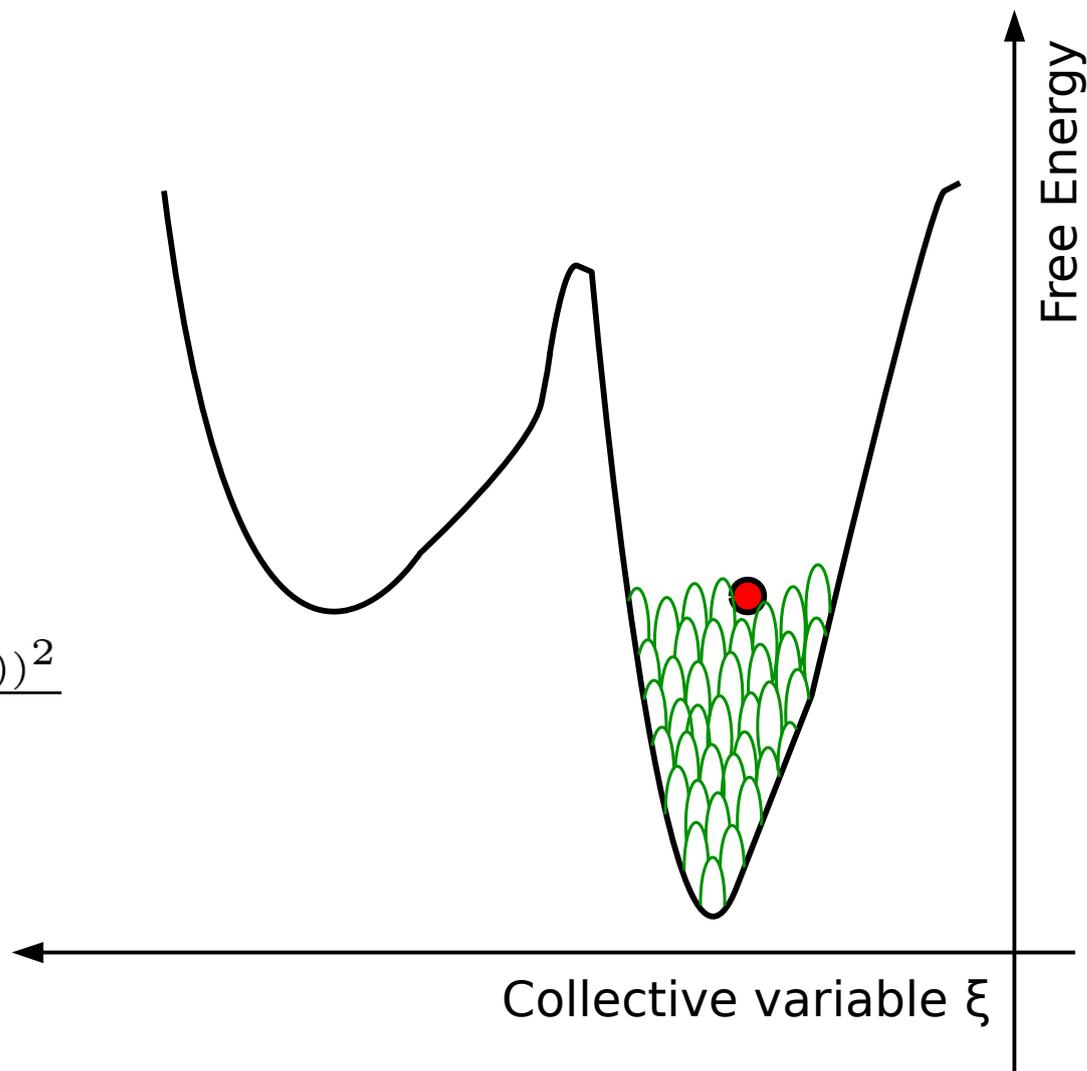
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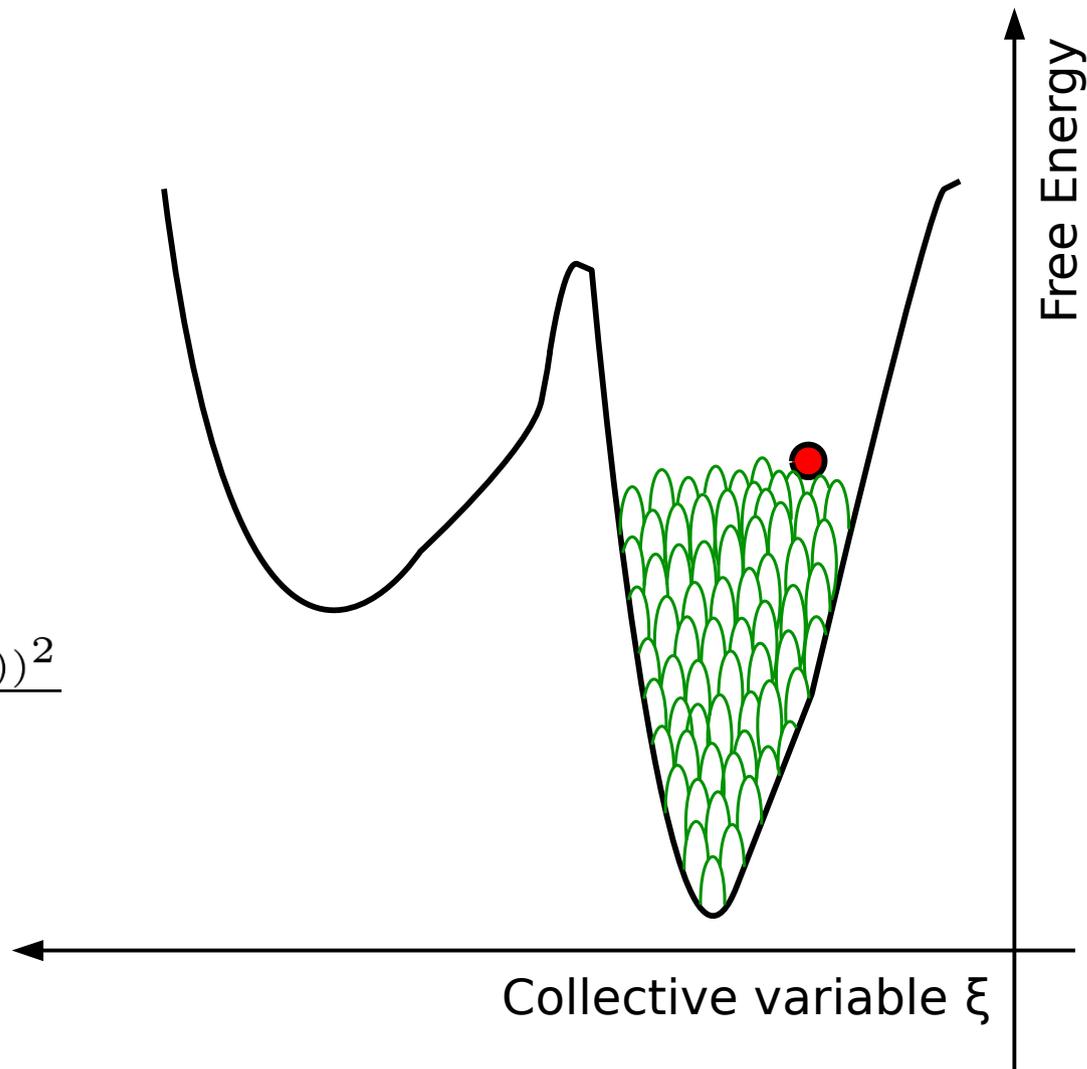
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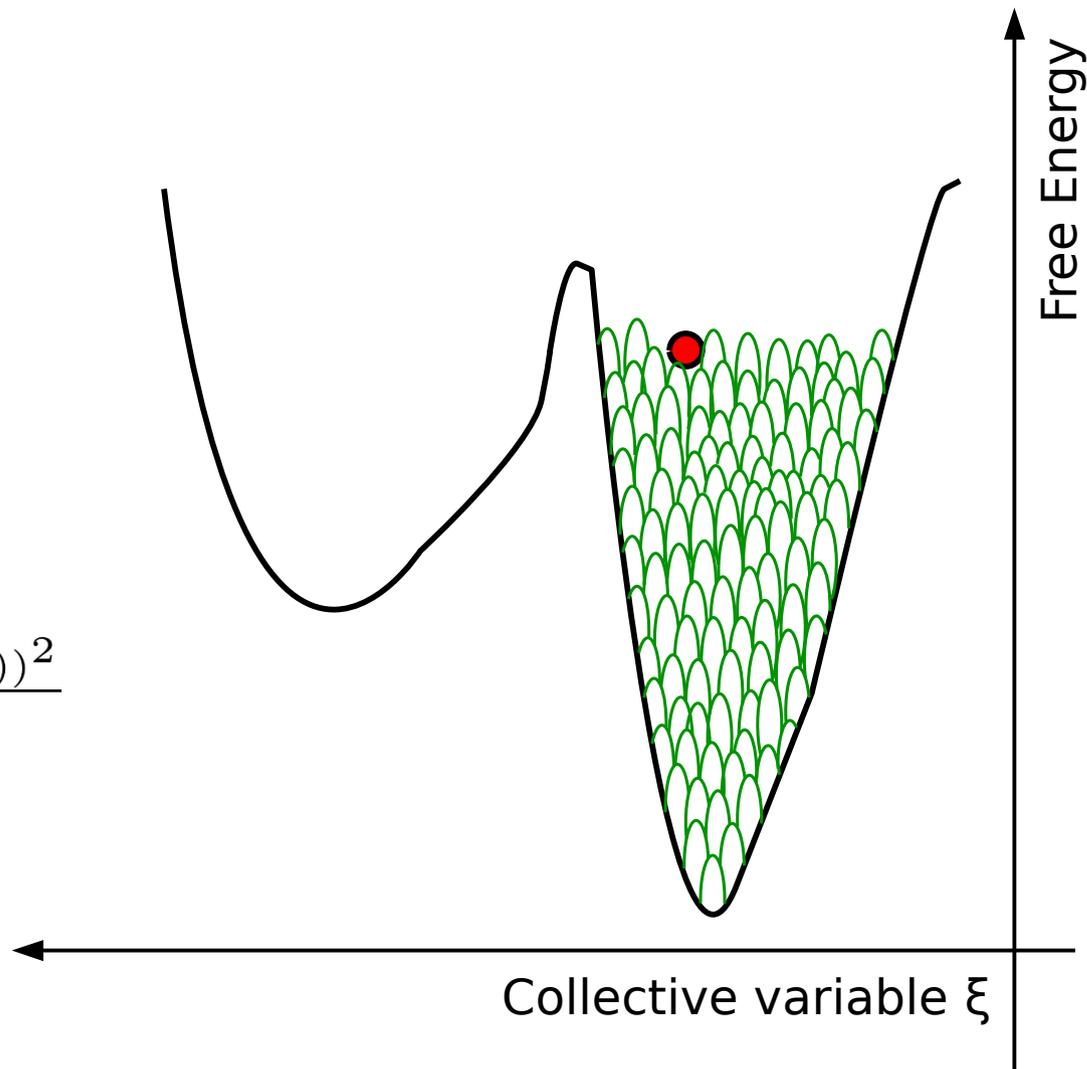
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Advanced sampling methods:  
metadynamics



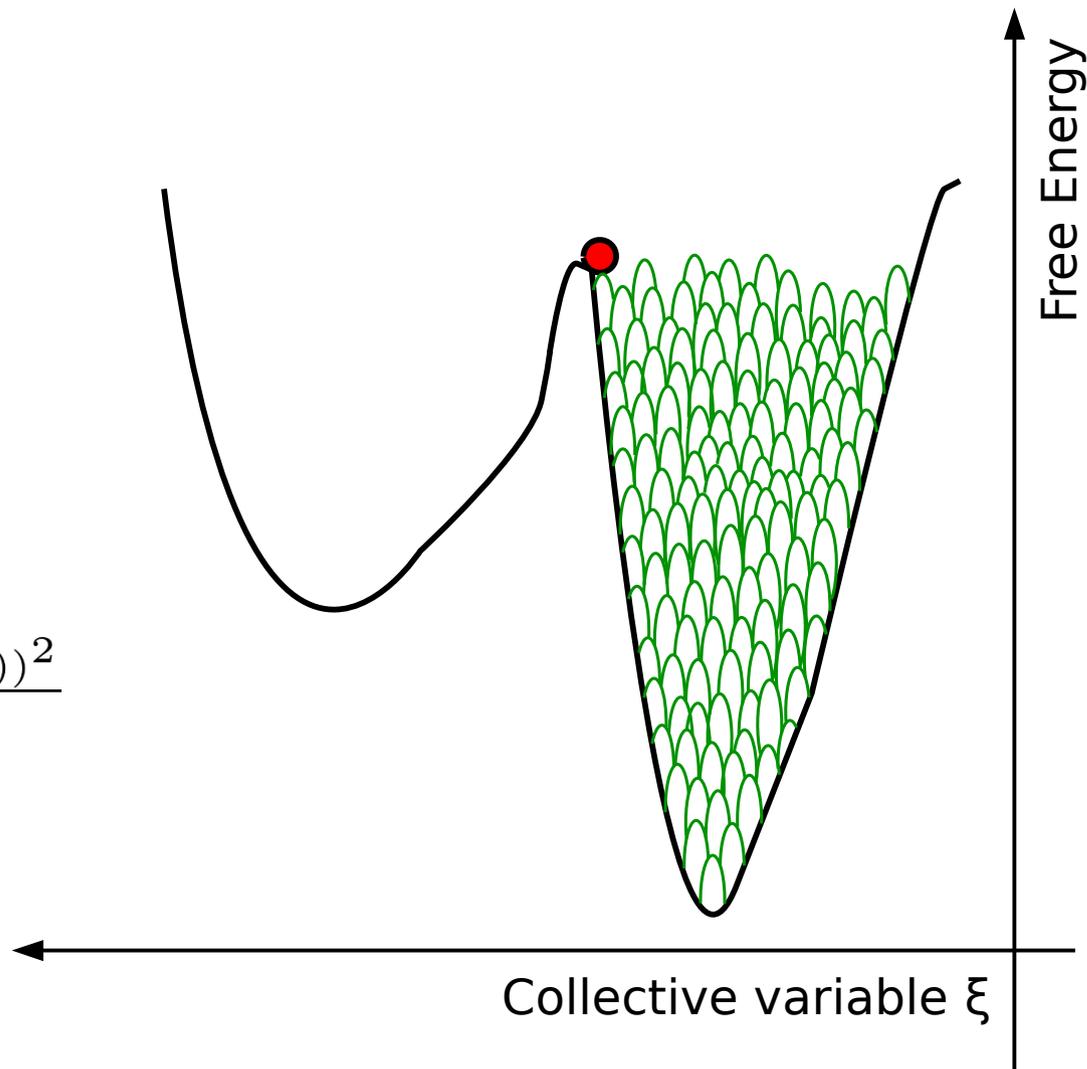
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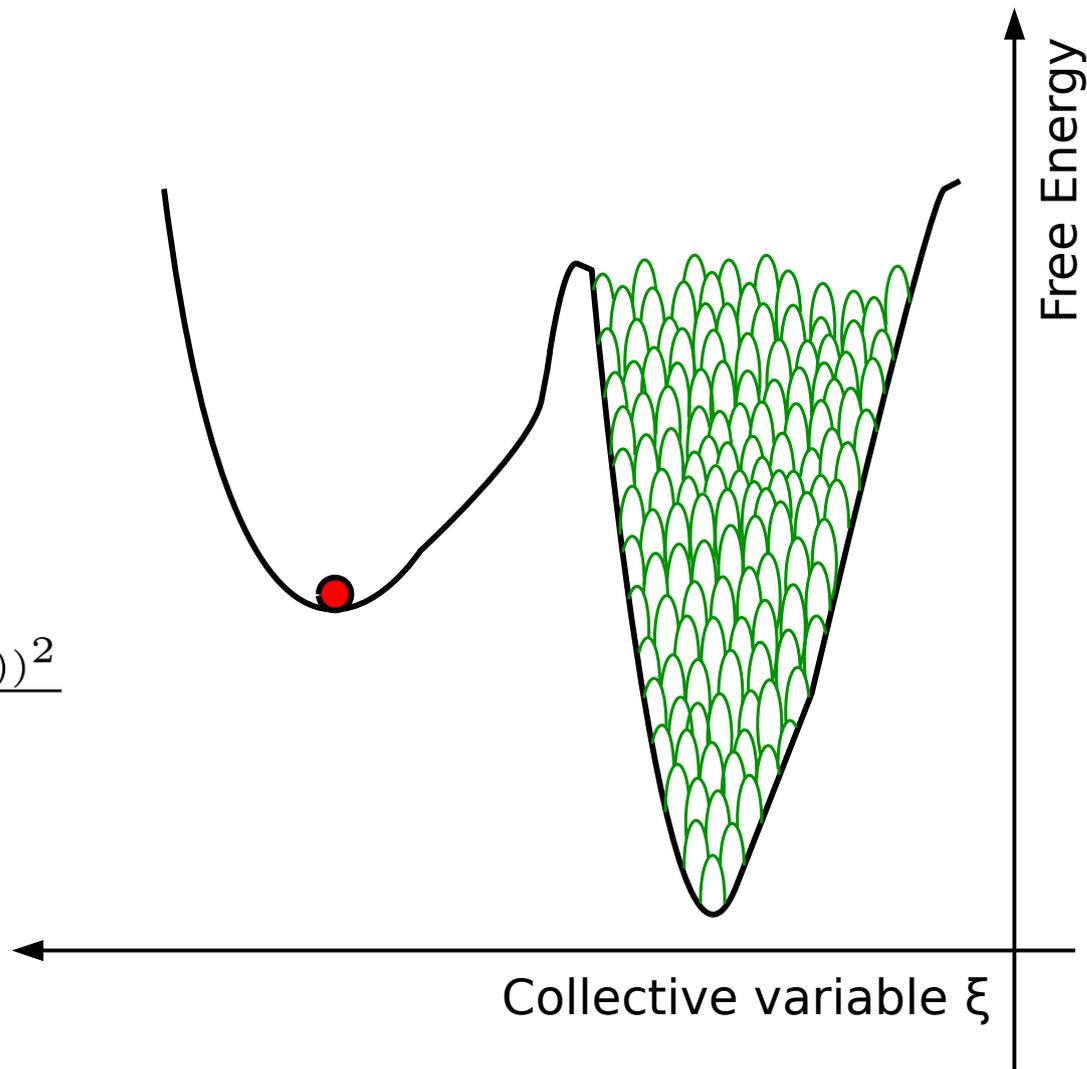
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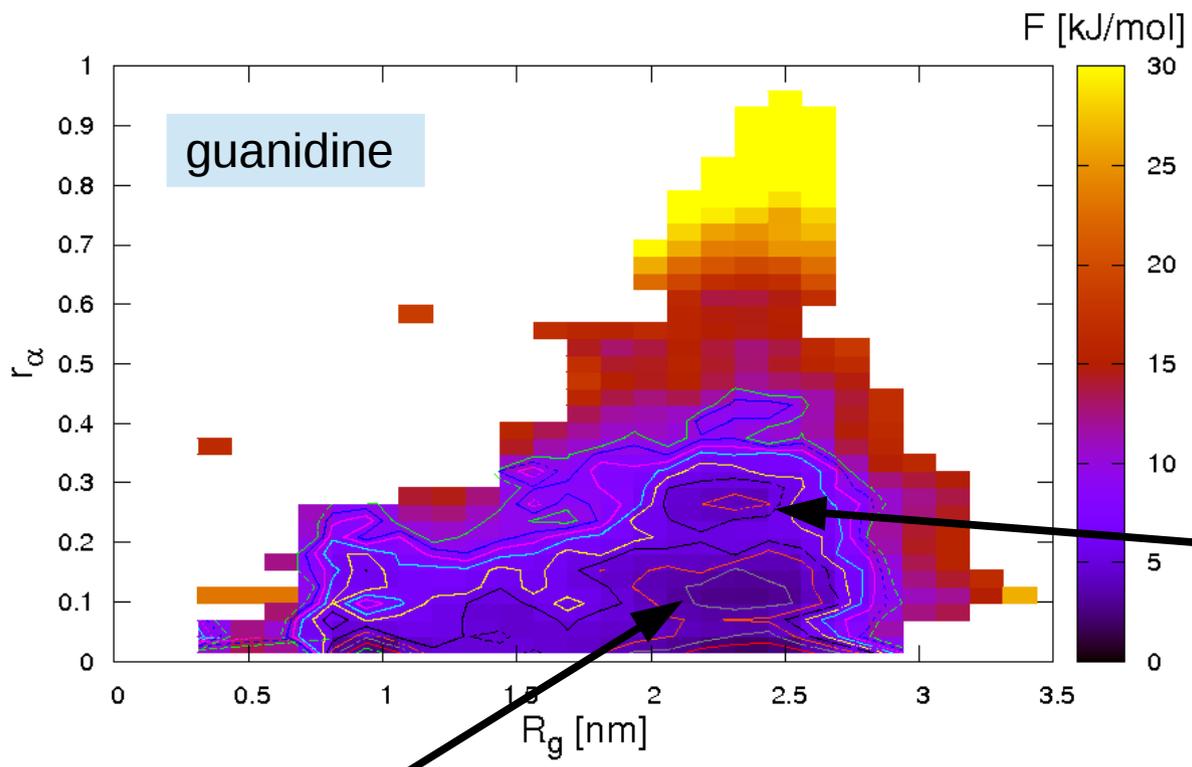
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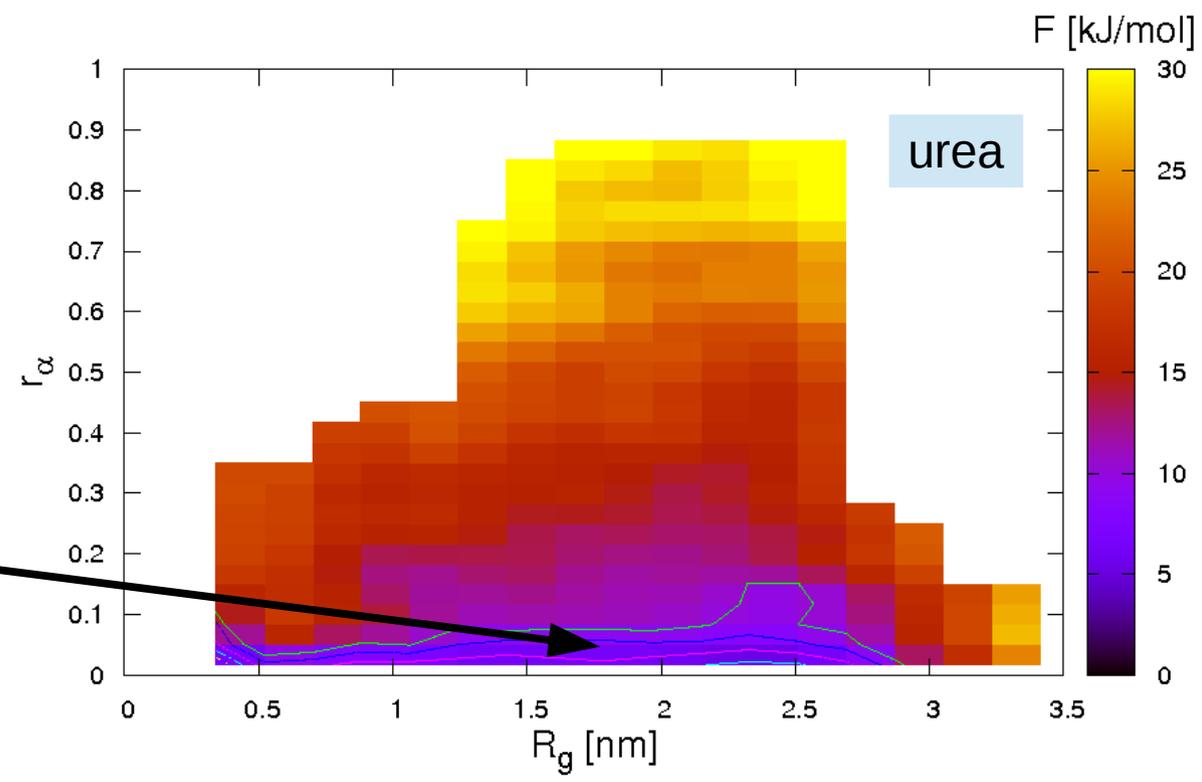




The same effect is observed also on the helix. Urea is able to destroy both the secondary structures, while some residual helicity can be seen in guanidine.



The denaturing effect of guanidine on the helix is stronger than on the hairpin, as the native state now has a very high energy (~27 kJ/mol)



One has to carefully choose the collective variable(s) to perform metadynamics on

The “good” collective variables should be “slow”:  
(time evolution slower than the other degrees of freedom)

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$$\dot{\xi}(t) = h(\xi) + g(\xi)F(t)$$

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The “good” collective variables should be “slow”:  
(time evolution slower than the other degrees of freedom)

$$\dot{\xi}(t) = h(\xi) + g(\xi)F(t)$$

 Search for a criterion to test the slowness of collective variables

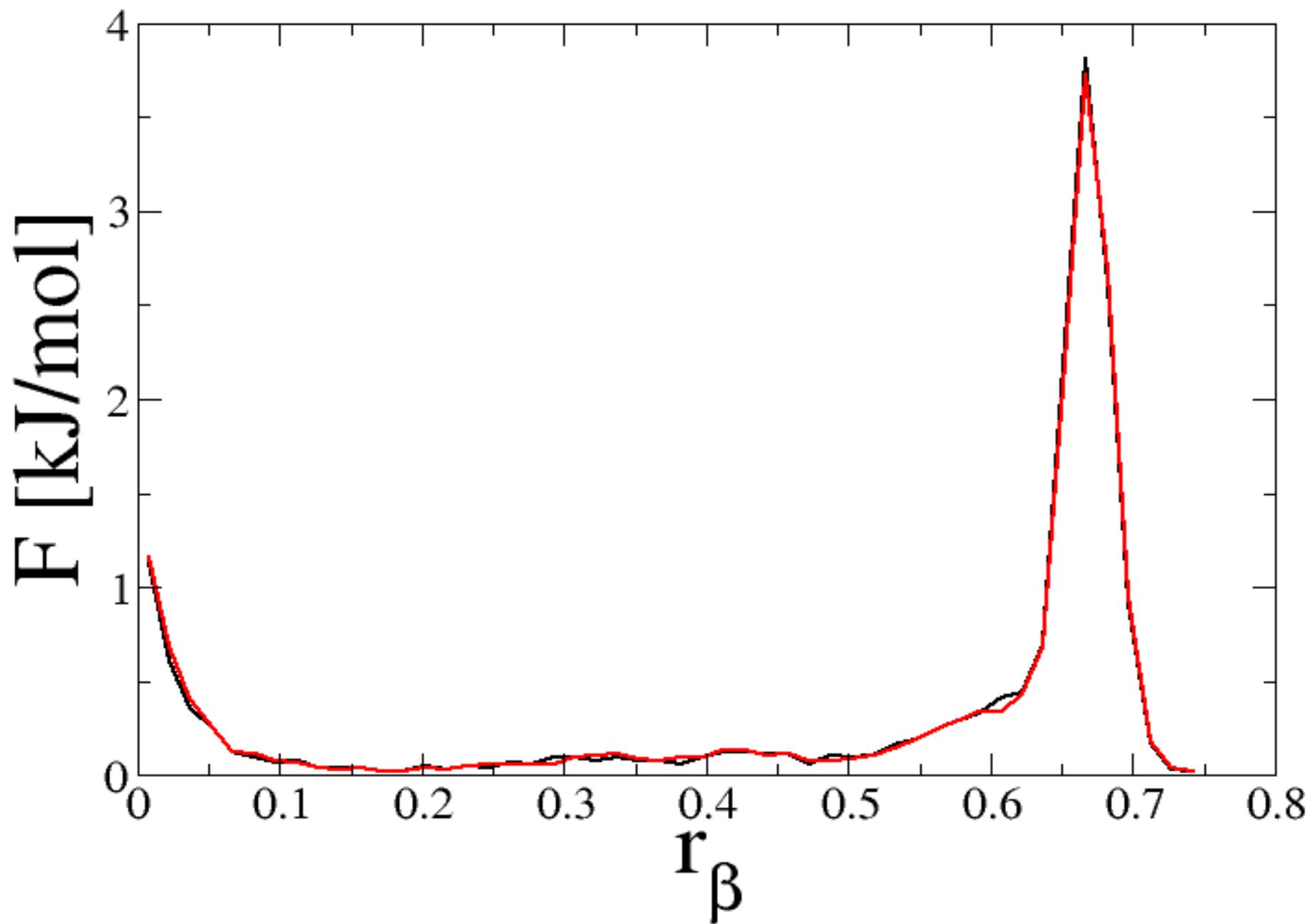
GOAL:

- Test and find good collective variables
- Write a linear combination of them to perform metadynamics
- Optimize their coefficients to better sample the phase space of denatured states

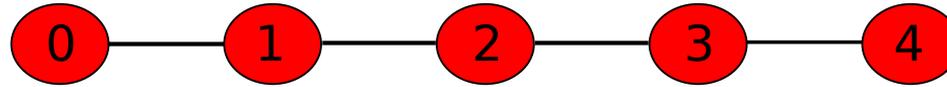
**Thanks for your  
attention**



Detail: comparison between 2nd and 3rd third of simulation after 60 ns



# How a standard replica-exchange works

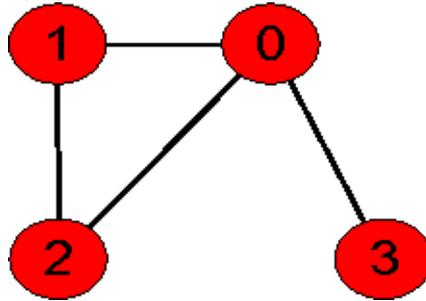


[ 0 1 2 3 4 ]

→ [ 0-1 2-3 4 ]

→ [ 0 1-2 3-4 ]

# How our scheme works



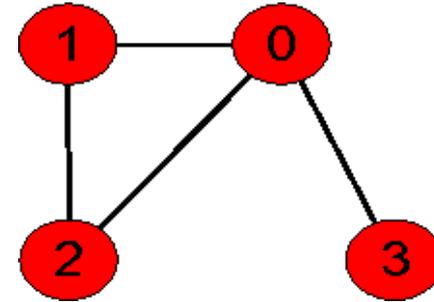
[ 0 1 2 3 ]  
[ 0 2 1 3 ]  
[ 0 3 1 2 ]

→ [ 0-1 2-3 ]  
[ 0-2 1-3 ]  
[ 0-3 1-2 ]

→ [ 0 1-2 3 ]  
[ 0 2-1 3 ]  
[ 0 3-1 2 ]

Generate a neighbour list

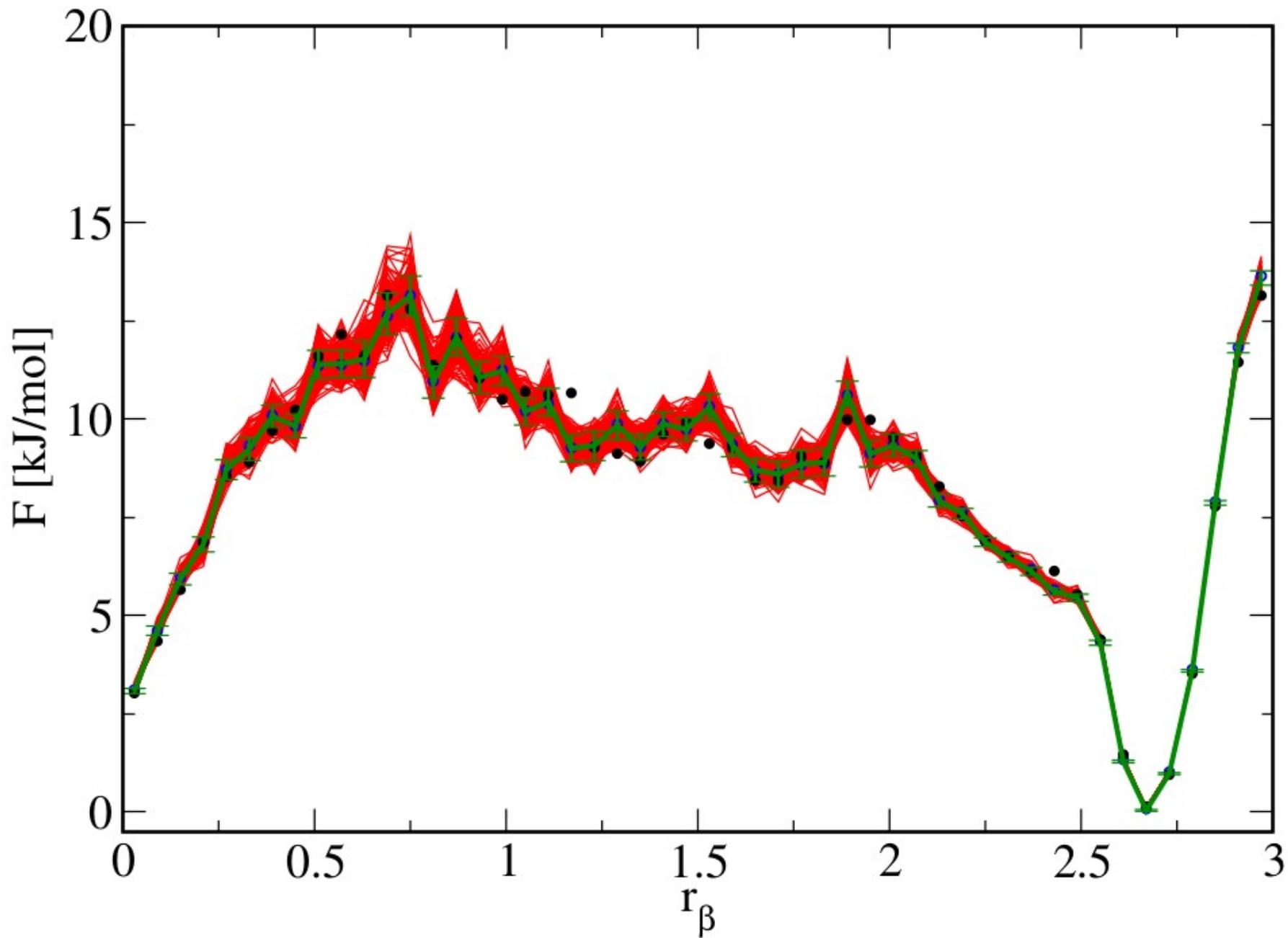
```
#  
NREPLICA 4  
#  
EDGE 0 3  
0 1  
0 2  
0 3  
EDGE 1 2  
1 0  
1 2  
EDGE 2 2  
2 0  
2 1  
EDGE 3 1  
3 0
```



- First extracted is always 0
- Next is extracted from the neighbour list
- If no replicas are available (because already extracted) the lower between those available is selected

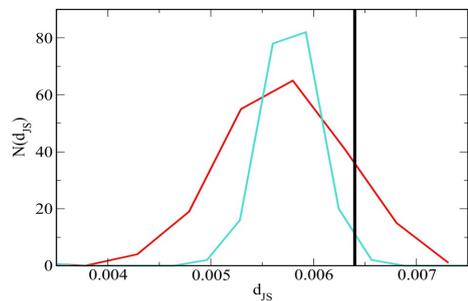
The exchange between two replicas not consecutive in the graph is not wrong

Green line: the original one (e.g. set A).  
Red lines: all the bootstraps of A.  
Black dots: the set B.

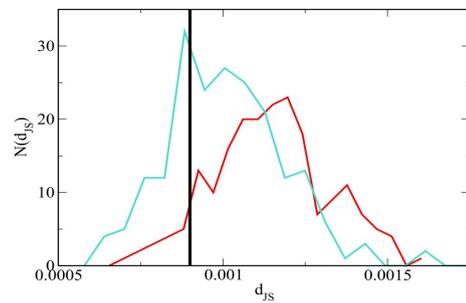


# All the JDSs

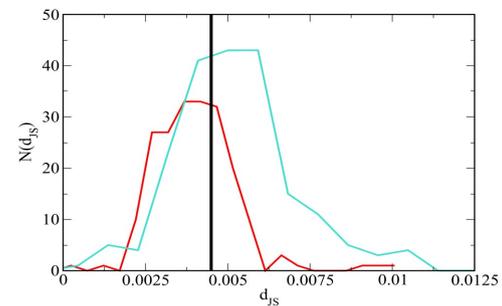
$r_\alpha$



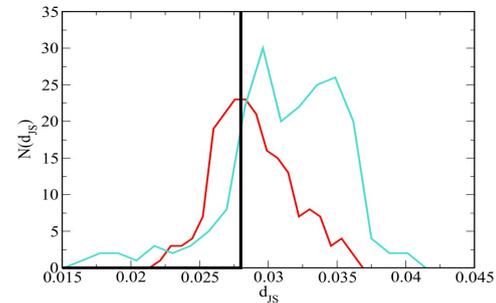
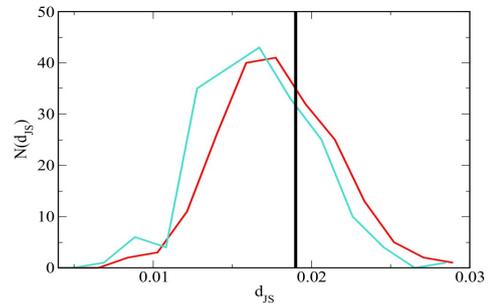
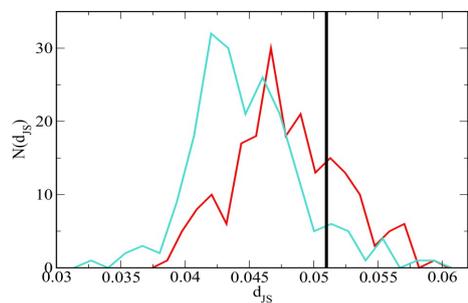
$r_\beta$



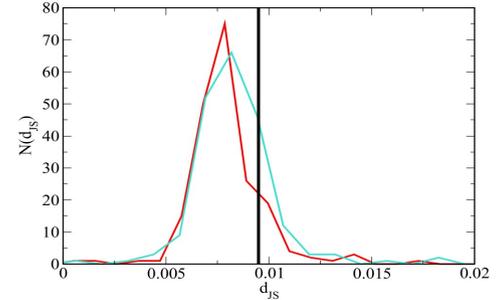
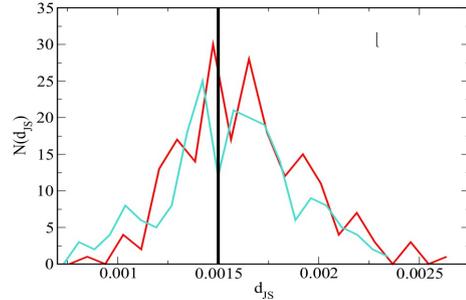
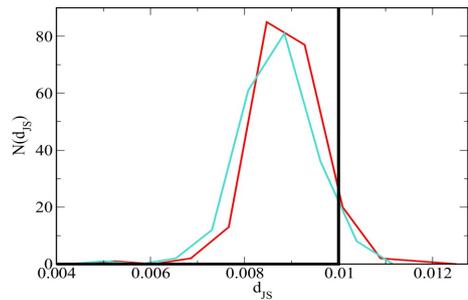
$R_g$



water



urea



guanidine

Both  $r_\alpha$  and  $r_\beta$  have the same functional form:

$r_\alpha$  counts the 6-plets of N-CA-C-CO-CB in  $\alpha$  conformation

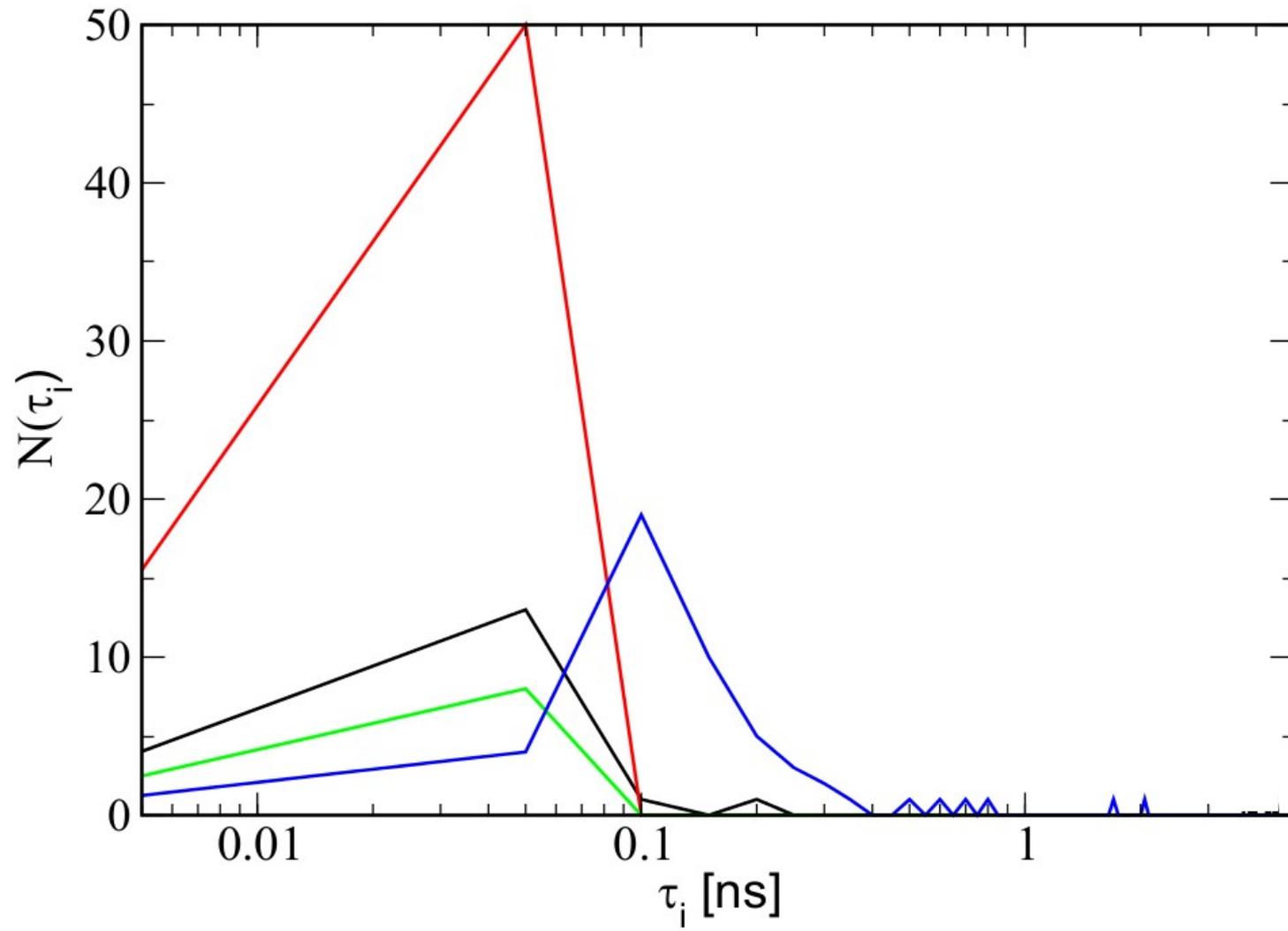
$r_\beta$  counts the couples of 3-plets of N-CA-C-CO-CB in  $\beta$  conformation

In this work, they have been normalized.

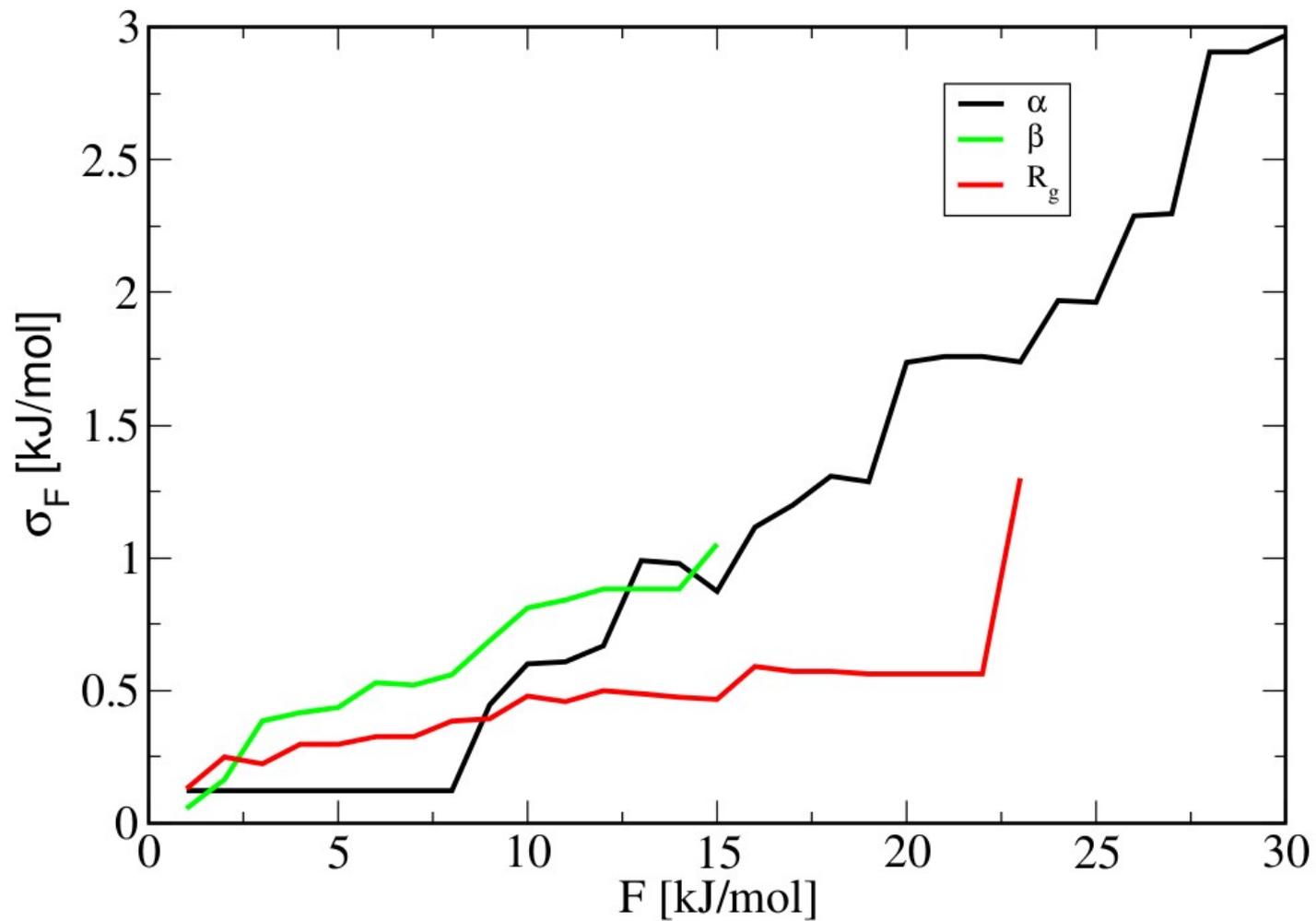
$$s = \sum_i \frac{1 - \left(\frac{r_i - d_0}{r_0}\right)^n}{1 - \left(\frac{r_i - d_0}{r_0}\right)^m}$$

$$n = 8; m = 12$$

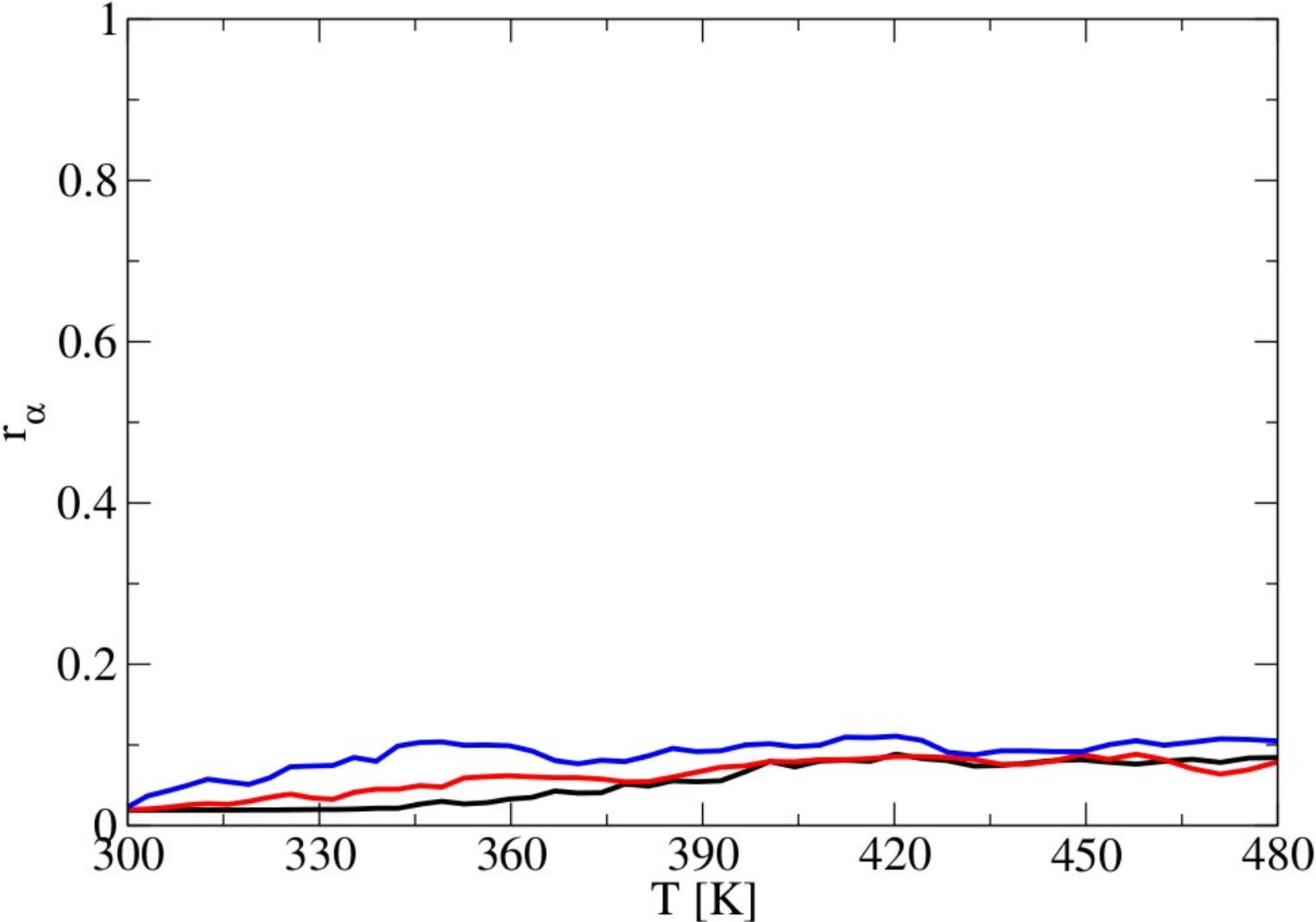
Histogram of autocorrelations of each replica



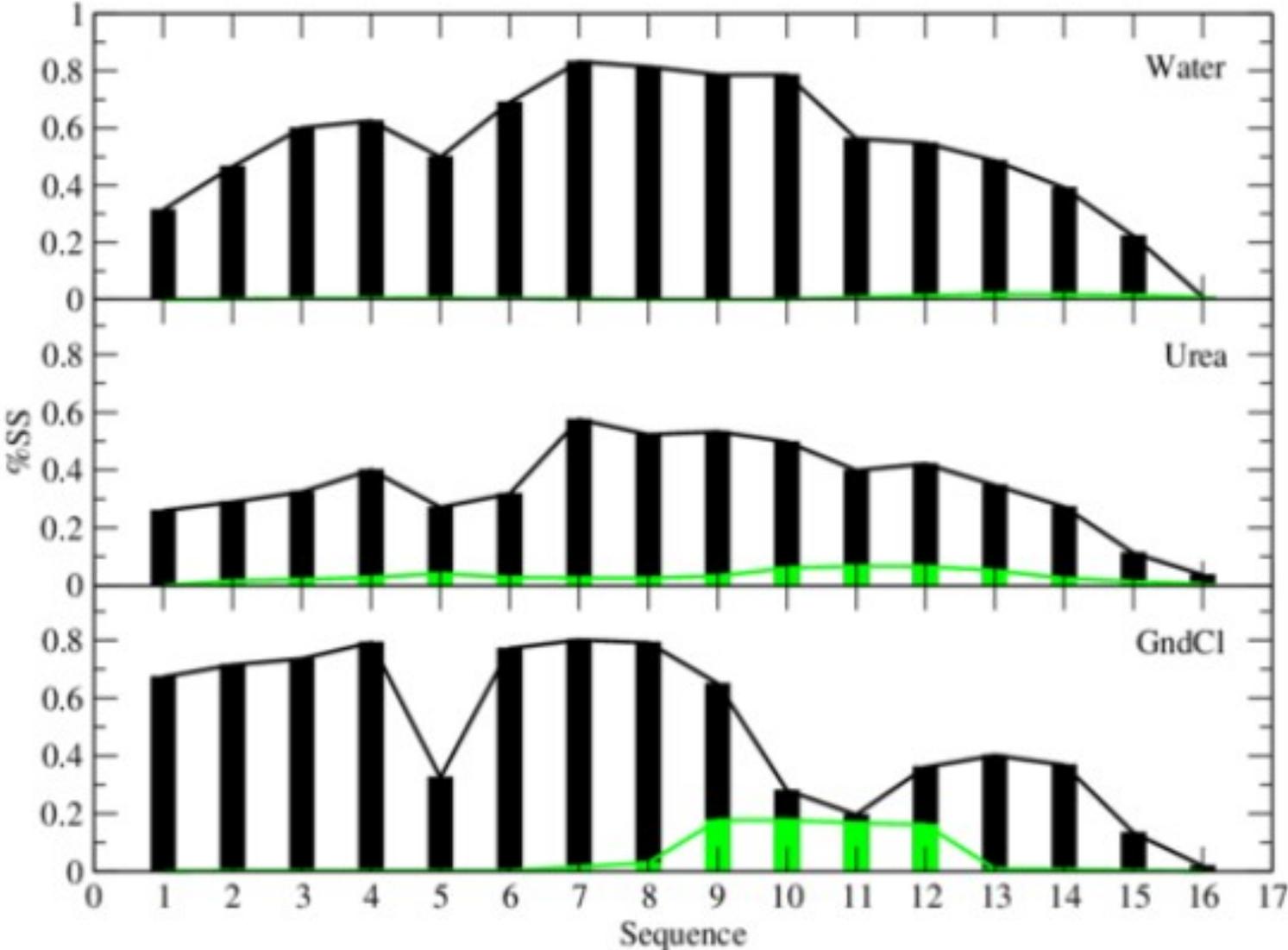
RMSD between 2nd and 3rd third free energy (water) vs Free energy values.  
The lower the free energy, the lower the RMSD that means that at least in the re



Alpha vs temp



Secondary structure (STRIDE. In green: polyproline)



Some other free energy landscapes..

